### Dual oscillator model of the respiratory neuronal network generating quantal slowing of respiratory rhythm

Amit Lal · Yoshitaka Oku · Swen Hülsmann · Yasumasa Okada · Fumikazu Miwakeichi · Shigeharu Kawai · Yoshiyasu Tamura · Makio Ishiguro

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Abstract We developed a dual oscillator model to facilitate the understanding of dynamic interactions between the parafacial respiratory group (pFRG) and the preBötzinger complex (preBötC) neurons in the respiratory rhythm generation. Both neuronal groups were modeled as groups of 81 interconnected pacemaker neurons; the bursting cell model described by Butera and others [model 1 in Butera et al. (J Neurophysiol 81:382–397, 1999a)] were used to model the pacemaker neurons. We assumed (1) both pFRG

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A. Lal · Y. Oku (⊠) Department of Physiology, Hyogo College of Medicine, Nishinomiya, Hyogo, 663-8501, Japan e-mail: yoku@hyo-med.ac.jp

A. Lal · S. Kawai · Y. Tamura · M. Ishiguro The Institute of Statistical Mathematics, Minato-ku, Tokyo, 106-8569, Japan

### S. Hülsmann

Abteilung Neuro- und Sinnesphysiologie, Zentrum Physiologie und Pathophysiologie and DFG Research Center Molecular Physiology of the Brain, Georg-August-Universität, Humboldtallee 23, 37073 Göttingen, Germany

Y. Okada Department of Medicine, Tsukigase Rehabilitation Center, Keio University, Izu, Shizuoka, 410-3215, Japan

F. Miwakeichi Graduate School of Engineering, Chiba University, Chiba-shi, Chiba, 263-8522, Japan and preBötC networks are rhythm generators, (2) preBötC receives excitatory inputs from pFRG, and pFRG receives inhibitory inputs from preBötC, and (3) persistent Na+ current conductance and synaptic current conductances are randomly distributed within each population. Our model could reproduce 1:1 coupling of bursting rhythms between pFRG and pre-BötC with the characteristic biphasic firing pattern of pFRG neurons, i.e., firings during pre-inspiratory and post-inspiratory phases. Compatible with experimental results, the model predicted the changes in firing pattern of pFRG neurons from biphasic expiratory to monophasic inspiratory, synchronous with preBötC neurons. Quantal slowing, a phenomena of prolonged respiratory period that jumps non-deterministically to integer multiples of the control period, was observed when the excitability of preBötC network decreased while strengths of synaptic connections between the two groups remained unchanged, suggesting that, in contrast to the earlier suggestions (Mellen et al., Neuron 37:821-826, 2003; Wittmeier et al., Proc Natl Acad Sci USA 105(46):18000-18005, 2008), quantal slowing could occur without suppressed or stochastic excitatory synaptic transmission. With a reduced excitability of preBötC network, the breakdown of synchronous bursting of preBötC neurons was predicted by simulation. We suggest that quantal slowing could result from a breakdown of synchronized bursting within the preBötC.

**Keywords** Rhythm coupling • Neuronal networks • Respiratory rhythm generation • Quantal slowing • Numerical simulation

### 1 Introduction

Two putative respiratory rhythm generators, the parafacial respiratory group (pFRG) (Onimaru et al. 1988; Onimaru and Homma 2003) and the preBötzinger complex (preBötC) (Smith et al. 1991), exist in the mammalian brainstem. The two neuronal groups, separately identified, are thought to play important roles in the generation and maintenance of respiratory rhythm (Feldman and Janczewski 2006; Onimaru and Homma 2006; Oku et al. 2007) at least in the neonatal period. although the primary site of the respiratory rhythm generation is still controversial (Feldman and Del Negro 2006). There are a number of neuronal behaviors that characterize the respiratory network in brainstem spinal cord preparations of neonatal rodents. First, the firing pattern of preinspiratory (Pre-I) neurons, a subset of neurons within pFRG, typically consists of three phases: (1) firing preceding the inspiratory phase, (2) suppression of firing during the inspiratory phase, originally referred to as inspiration-related inhibition of the Pre-I firing (IIPI), and (3) firing during the post-inspiratory phase, which is not seen in preBötC preinspiratory neurons (Smith et al. 2007). Second, IIPI consistently disappears after removing chloride-mediated inhibition, resulting in overlapping of Pre-I neuronal firing and inspiratory neuronal firing (Onimaru et al. 1990). Third, opioids do not affect Pre-I neurons but depress preBötC inspiratory neurons (Gray et al. 1999). As a consequence of dynamic interactions between pFRG and preBötC, respiratory periods jump non-deterministically to integer multiples of the control period, and the phenomenon was referred to as quantal slowing (Mellen et al. 2003; Barnes et al. 2007). Synaptic connections and interactions between the neuronal groups to explain the characteristic behaviors have been proposed (Onimaru et al. 1990; Ballanyi et al. 1999). Specifically, the observation of quantal slowing has led to a hypothesis that two rhythmically active networks interact to generate respiratory rhythm and quantal slowing results from transmission failure from pFRG to preBötC networks (Mellen et al. 2003). However, in such a complex dynamic system, it is imperative to evaluate descriptive assumptions by simulating phenomena using a computational model.

In the present study, we demonstrate a computational model consisting of two groups of bursting neurons, representing pFRG and preBötC neuronal groups. We assume that pFRG provides excitatory inputs to preBötC and preBötC provides inhibitory connections to pFRG (Onimaru et al. 1990; Ballanyi et al. 1999). We then analyzed the influences of changes in strengths of excitatory and inhibitory synaptic connec-

tions between the two neuronal groups on the coupling pattern of bursting activities in these groups. Finally, we evaluated the effects of reducing excitability of preBötC neurons on the respiratory period, and considered the mechanism that causes non-deterministic jump of respiratory period to integer multiples of the control periods. Interestingly, we found that the quantal slowing occurs without assuming suppressed excitatory synaptic transmission.

Similar attempts to simulate quantal slowing phenomenon by dynamic interactions between the two rhythm generating networks has been made by Joseph and Butera (2005) and Wittmeier et al. (2008) earlier. In both studies, pFRG and preBötC were represented by only a pair of pacemaker neurons, presuming that any 'lumped' effects of the interaction should apply at the full-blown network level (Wittmeier et al. 2008). Joseph and Butera (2005) used a simple canonical model of pacemaker neurons to represent the pFRG and preBötC. However, it is difficult to correlate cellular properties with model parameters in such a canonical model. Further, in their result, quantal slowing accompanied abrupt changes in firing pattern of Pre-I neurons, i.e., emergence of postinspiratory burst that was absent in the control period, which is inconsistent with experimental findings (Mellen et al. 2003). Wittmeier et al. (2008) adopted a Hodgkin-Huxley type realistic neuronal model described by Butera et al. (1999a) and substituted stochastic synaptic transmission for the deterministic excitatory synaptic inputs to preBötC from pFRG to simulate quantal slowing. However, there is no physiological basis supporting that opioids cause stochastic synaptic transmission. Moreover, if the stochastic nature of synaptic transmission is essential for producing quantal slowing then the phenomenon is not entirely a characteristic of the model under consideration but also of a undefined additional mechanism resulting in stochastic dynamics of the synaptic transmission. In the present study, we have conducted a large scale simulation by modeling both pFRG and preBötC as groups of 81 pacemaker neurons to test whether the essential features of the activity of a rhythm generating network may be adequately captured by replacing it by a single pacemaker neuron, and more specifically, to test whether the quantal slowing phenomenon requires stochastic dynamics of the synaptic transmission. Our simulation predicted that the reduction of excitability in preBötC network could result in intermittent failure of preBötC neurons to produce synchronized bursting and could cause quantal slowing even if we did not assume stochastic dynamics of the synaptic transmission. We suggest that the



quantal slowing phenomenon is an intrinsic characteristic of the rhythm-generating network and stochastic synaptic transmission is unnecessary to explain the quantal slowing phenomenon. Our results are in agreement with the general conception that quantal slowing phenomenon results due to general loss of sensitivity within the preBötC group but, more importantly, they suggest towards the possibility of a different mechanism for its cause.

### 2 Methods

### 2.1 Formulation of dual oscillator model

The model consists of two neuronal groups of bursting neurons, *NeuronGroup1* and *NeuronGroup2*; representing the pFRG and preBötC rhythm generating networks, respectively. We assume that both pFRG and preBötC independently constitute rhythm-generating networks, and pFRG network excites preBötC network, and preBötC network inhibits pFRG network (Fig. 1(a)). In our model, we assume that bursting neurons within each of *NeuronGroup1* and *Neuron-Group2* are mutually coupled by excitatory synaptic connections to form a rhythm generating network. Therefore, the constituent neurons of *NeuronGroup2* are excitatory neurons. It is unrealistic to assume that

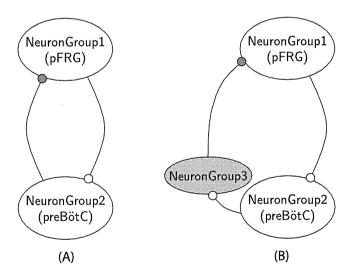


Fig. 1 (a) Dual Oscillator Model: NeuronGroup1 (pFRG) provides excitatory synaptic input to NeuronGroup2 (preBötC) and NeuronGroup2 provides inhibitory synaptic input directly to NeuronGroup1. (b) Three neuronal group model: Similar to Dual Oscillator Model except that an inspiratory interneuron group, NeuronGroup3 is added. NeuronGroup3 receives excitatory inputs from NeuronGroup2 and inhibit NeuronGroup1. Open and closed circles represent excitatory and inhibitory synaptic connections, respectively

the excitatory neurons of NeuronGroup2 inhibit NeuronGroup1. A more realistic model would be a three neuronal group model as depicted in Fig. 1(b); the third neuronal group, NeuronGroup3, is formed of inhibitory neurons, which receives excitatory synaptic input from NeuronGroup2 and provides inhibitory synaptic input to NeuronGroup1 (Kuwana et al. 2006). However, for simplicity, if we assume that the bursting dynamics of NeuronGroup3 follow the bursting activities of NeuronGroup2, then the NeuronGroup3 in Fig. 1(b) essentially becomes a copy of NeuronGroup2. Thus, the need of explicitly incorporating NeuronGroup3 is eliminated and computational effort required is minimized. Therefore, we use the model depicted in Fig. 1(a) as our Dual Oscillator Model.

### 2.2 Formulation of neuronal groups

Both neuronal groups, *NeuronGroup1* and *Neuron-Group2*, were modeled as groups of 81 interconnected pacemaker neurons. The mathematical model of bursting cells described by Butera and others (*model 1* in Butera et al. 1999a) were used to model the pacemaker neurons in our model. We assume that each cell receives excitatory and inhibitory synaptic inputs. Therefore, the rate of change in membrane potential (*V*) of a cell is modified from the original model as:

$$C\frac{dV}{dt} = -I_{\text{NaP}} - I_{\text{Na}} - I_{\text{K}} - I_{\text{L}} - I_{\text{syn(e)}} - I_{\text{syn(i)}}$$
 (1)

where C is the whole cell capacitance (pF), V is membrane potential (mV), t is time (ms),  $I_{\text{NaP}}$  is a persistent Na<sup>+</sup> current,  $I_{\text{Na}}$  is a fast Na<sup>+</sup> current,  $I_{\text{K}}$  is a delayedrectifier K<sup>+</sup> current,  $I_{\text{L}}$  is a passive leakage current,  $I_{\text{syn(e)}}$  is the sum of excitatory synaptic currents, and  $I_{\text{syn(i)}}$  is the sum of inhibitory synaptic currents. C is set to 21 pF (Smith et al. 1992; Butera et al. 1999a). Equations and parameter sets to compute intrinsic membrane currents ( $I_{\text{NaP}}$ ,  $I_{\text{Na}}$ ,  $I_{\text{K}}$  and  $I_{\text{L}}$ ) are those presented in the previous paper (Butera et al. 1999a) unless otherwise noted.

We assume that each neuron receives excitatory synaptic inputs from other neurons belonging to the same group L as well as from neurons belonging to a different group M:

$$I_{\text{syn(e)}} = \left(\sum_{l \in L} g_{\text{syn(int)}}^{l} \cdot s_{\text{int}}^{l}\right) \left(V - E_{\text{syn(e)}}\right) + \left(\sum_{m \in M} g_{\text{syn(ext)}}^{m} \cdot s_{\text{ext}}^{m}\right) \left(V - E_{\text{syn(e)}}\right)$$
(2)

where  $E_{\mathrm{syn(e)}}$  (= 0 mV) is the reversal potential of non-NMDA excitatory amino-acid receptors.  $g_{\mathrm{syn(int)}}^l$  and  $g_{\mathrm{syn(ext)}}^m$  are the synaptic conductances for input from neurons  $l \in L$  and  $m \in M$ , respectively.  $s_{\mathrm{int}}^l$  and  $s_{\mathrm{ext}}^m$  are synaptic gating variables for these synaptic inputs. To reduce computational costs, we assumed that synaptic conductances  $g_{\mathrm{syn(int)}}^l$  and  $g_{\mathrm{syn(ext)}}^m$  in Eq. (2) are uncorrelated to the corresponding synaptic gating variables  $s_{\mathrm{int}}^l$  and  $s_{\mathrm{ext}}^m$ , respectively. Consequently, we simplify Eq. (2) as:

$$I_{\text{syn(e)}} = (\bar{g}_{\text{syn(int)}} \cdot \bar{s}_{\text{int}} + \bar{g}_{\text{syn(ext)}} \cdot \bar{s}_{\text{ext}}) (V - E_{\text{syn(e)}})$$
(3)

where  $\bar{g}_{\text{syn(int)}}$  and  $\bar{g}_{\text{syn(ext)}}$  are overall synaptic conductance for inputs from neurons  $l \in L$  and  $m \in M$ , respectively. The values of  $\bar{g}_{\text{syn(int)}}$  and  $\bar{g}_{\text{syn(ext)}}$  were randomly assigned from a uniformly distributed probability density function ranging between 0 and 10 nS and between 0 and  $\bar{g}_{\text{syn(ext)}\_{\text{max}}}$ , respectively. The rationale for using uniformly distributed probability density function for synaptic conductance is discussed in Section 4.3.  $\bar{s}_{\text{int}}$  and  $\bar{s}_{\text{ext}}$  are mean synaptic gating variables for these synaptic inputs, which are expressed as:

$$\bar{s}_{\text{int}} = \overline{\sum_{l \in L} s_{\text{int}}^l}, \qquad \bar{s}_{\text{ext}} = \overline{\sum_{m \in M} s_{\text{ext}}^m}$$
 (4)

Similarly, synaptic inputs from an inhibitory neuronal group N are expressed as:

$$I_{\text{syn(i)}} = \bar{g}_{\text{syn(inh)}} \cdot \bar{s}_{\text{inh}} (V - E_{\text{Cl}})$$
 (5)

where  $\bar{g}_{\rm syn(inh)}$  is the overall synaptic conductance for inputs from neurons  $n \in N$ ,  $\bar{s}_{\rm inh}$  are the mean synaptic gating variable for inhibitory inputs, and  $E_{\rm Cl}$  (=  $-90~\rm mV$ ) is the equilibrium potential of Cl<sup>-</sup>. The values of  $\bar{g}_{\rm syn(inh)}$  were randomly assigned from a uniformly distributed probability density function ranging between 0 and  $\bar{g}_{\rm syn(inh)~max}$ .

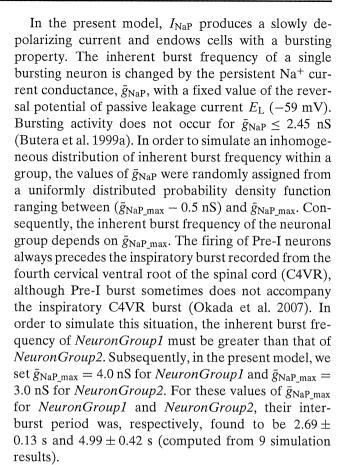
Presynaptic action potentials activate synaptic gating variables. We applied the same, fast (decay time constant  $\tau_s = 5$  ms) kinetics to all synaptic gating variables (Butera et al. 1999b):

$$\frac{ds_i}{dt} = \frac{\left[ (1 - s_i) \cdot s_\infty \left( V_i \right) - s_i \right]}{\tau_s} \tag{6}$$

 $s_{\infty}$  ( $V_i$ ) determines the steady-state postsynaptic receptor activation based on the membrane potential of presynaptic neuron i:

$$s_{\infty}(V_i) = \frac{1}{1 + \exp\left[\frac{(V_i - \theta)}{\sigma}\right]}$$
 (7)

where  $\theta = -10 \text{ mV}$  and  $\sigma = -5 \text{ mV}$ .



We set  $\bar{g}_{\text{syn(ext)}} = 0$  nS for NeuronGroup1 and  $\bar{g}_{\text{syn(inh)}} = 0$  nS for NeuronGroup2.  $\bar{s}_{\text{inh}}$  of NeuronGroup1 was calculated from membrane potentials of NeuronGroup2 neurons and  $\bar{s}_{\text{ext}}$  of NeuronGroup2 was calculated from membrane potentials of NeuronGroup1 neurons. To evaluate the effects of changes in strengths of excitatory and inhibitory synaptic connections on the coupling pattern between pFRG and preBötC bursting activities, we varied  $\bar{g}_{\text{syn(inh)_max}}$  of NeuronGroup1 ranging between 0 and 6 nS and  $\bar{g}_{\text{syn(ext)_max}}$  of NeuronGroup2 ranging between 0 and 2 nS.

### 2.3 Computational details

The differential equations were solved numerically using the fourth-order Runge-Kutta equation with a step size of 0.05 ms. However, the neuronal states were saved at an interval of 0.5 ms, which was sufficient to capture every action potential spikes of bursting neurons, to keep the stored files to manageable size. All algorithms were implemented in double precision routine in C‡.NET language and run on Pentium-based Windows XP computers. We waited for initial 60 s of simulation time for the behavior of the network to stabilize and then the simulated data were saved.



### 3 Results

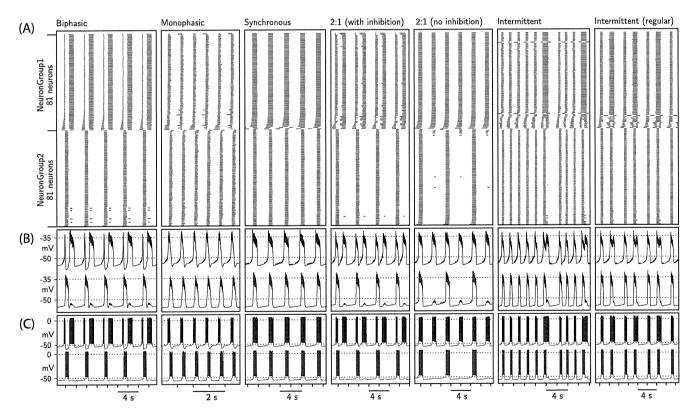
As mentioned earlier, in the dual oscillator model, *NeuronGroup1* and *NeuronGroup2* represents pFRG and preBötC, respectively. However, during the presentation of results and discussion, we restrict the terms *NeuronGroup1* and *NeuronGroup2* to refer to the *modeled* pFRG and preBötC, respectively. Further, throughout the present model study, we define the period where preBötC/*NeuronGroup2* neurons burst synchronously as the inspiratory phase, and the rest of period where a majority of preBötC/*NeuronGroup2* neurons are quiescent as the expiratory phase.

### 3.1 Coupling pattern between pFRG and preBötC

We observed different patterns of coupling between NeuronGroup1 and NeuronGroup2 depending on strengths of excitatory and inhibitory synaptic con-

nections  $(\bar{g}_{syn(ext)_max})$  and  $\bar{g}_{syn(inh)_max}$ , respectively). Figure 2(a) depicts typical raster plots for various coupling modes observed. Horizontal segments in Fig. 2(a) represent bursting periods of all the  $2 \times 81$  neurons constituting the NeuronGroup1 and NeuronGroup2. For each burst of each neuron, the bursting period is defined as the period beginning from the instant when the membrane potential of the neuron rises above -20 mV while delivering the first spike of the burst to the instant when the membrane potential falls below -20 mV while delivering the final spike of the burst. Membrane potential trajectories of a typical neuron within NeuronGroup1 and NeuronGroup2 for the various coupling modes are depicted in Fig. 2(c); averaged population activities of NeuronGroup1 and Neuron-Group2 are depicted in Fig. 2(b).

The coupling modes were classified visually based on the averaged population activity. However, since the population activity and the individual neuron



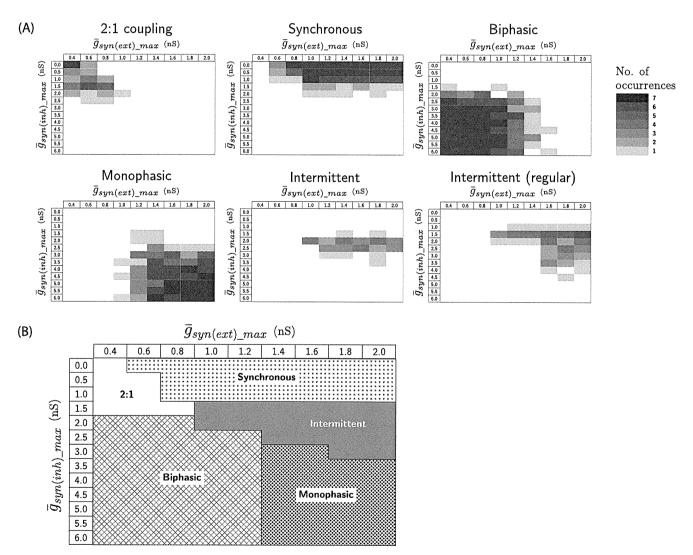
**Fig. 2** (a) Raster plots of various coupling modes—biphasic  $(\bar{g}_{\text{syn(ext)}_{\text{max}}} = 0.8 \text{ nS}, \bar{g}_{\text{syn(inh)}_{\text{max}}} = 4.5 \text{ nS})$ , monophasic  $(\bar{g}_{\text{syn(ext)}_{\text{max}}} = 2.0 \text{ nS}, \bar{g}_{\text{syn(inh)}_{\text{max}}} = 5.0 \text{ nS})$ , Synchronous  $(\bar{g}_{\text{syn(ext)}_{\text{max}}} = 1.2 \text{ nS}, \bar{g}_{\text{syn(inh)}_{\text{max}}} = 0.5 \text{ nS})$ , 2:1 coupling (with inhibition:  $\bar{g}_{\text{syn(ext)}_{\text{max}}} = 0.8 \text{ nS}, \bar{g}_{\text{syn(inh)}_{\text{max}}} = 1.5 \text{ nS}$ ; no inhibition:  $\bar{g}_{\text{syn(ext)}_{\text{max}}} = 0.4 \text{ nS}, \bar{g}_{\text{syn(inh)}_{\text{max}}} = 0.0 \text{ nS})$ , and intermittent  $(\bar{g}_{\text{syn(ext)}_{\text{max}}} = 2.0 \text{ nS}, \bar{g}_{\text{syn(inh)}_{\text{max}}} = 3.0 \text{ nS}$ ; intermittent regular also corresponds to the same values of synaptic strengths)—observed by changing the strengths of excitatory

and inhibitory synaptic conductances. The neurons within each neuronal groups are ranked in ascending order of their bursting activity initiation timings for better visualization. (b) Corresponding averaged population activity of NeuronGroup1 and NeuronGroup2 (top and bottom traces, respectively, in each panel) and (c) Activity of a typical neuron belonging to NeuronGroup1 and NeuronGroup2 (top and bottom traces, respectively, in each panel)



activity within the neuronal groups are well correlated, the coupling mode classification could be based on the activity of a pair of neurons from *NeuronGroup1* and *NeuronGroup2* as well (Fig. 2(c)). Nomenclatures used for classifying the different coupling pattern are as follows:

- The biphasic mode is characterized by activity pattern of *NeuronGroup1* neurons resembling Pre-I neurons—bursting just before inspiratory burst of *NeuronGroup2* neurons, inhibition during inspiratory phase, and post-inspiratory second burst (Fig. 2(c), Biphasic).
- The monophasic coupling mode is characterized by activity of *NeuronGroup1* neurons compris-
- ing two phases—bursting just before inspiratory burst of NeuronGroup2 neurons and inhibition during inspiratory phase (Fig. 2(c), Monophasic). We termed this coupling mode as 'monophasic' because it may be thought of as a reduced form of biphasic coupling where the post-inspiratory second burst of NeuronGroup1 neurons is missing. The bursting frequency of both NeuronGroup1 and NeuronGroup2 neurons are high in monophasic coupling mode; note the magnified time scale used for monophasic coupling in Fig. 2.
- The synchronous coupling mode is characterized by simultaneous bursting activity of both *Neuron-Group1* and *NeuronGroup2* neurons (Fig. 2(c), Synchronous).



**Fig. 3** (a) Domain of occurrence of coupling modes as a function of excitatory and inhibitory synaptic strengths of the dual oscillator model. For each combination of  $\bar{g}_{\text{syn(ext)_max}}$  and  $\bar{g}_{\text{syn(inh)_max}}$ , seven simulations were performed and the frequency of occurrence of various coupling modes are illustrated using the gray

color scale indicated on the *right*. (b) Representative domain of various coupling modes based on maximum occurrence frequency. For simplicity, the occurrence frequency of the two types of intermittent coupling modes were merged together, since their occurrence domain overlaps



- The 2:1 coupling mode is the case where NeuronGroup1 and NeuronGroup2 exhibit bursting activity in 2:1 ratio. 2:1 coupling mode may be further subclassified as (1) 2:1 with inhibition— NeuronGroup1 neuron activity is similar to that of biphasic coupling mode except that its post inspiratory burst is significantly delayed (Fig. 2, 2:1 (with inhibition)), and (2) 2:1 without inhibition— NeuronGroup2 neurons synchronize their bursting activity with every alternate bursting activity of *NeuronGroup1* neurons (Fig. 2, 2:1 (no inhibition)). In both of these 2:1 coupling modes, excitatory postsynaptic potentials (EPSPs) are observed on membrane trajectories of *NeuronGroup2* neurons coincident with the NeuronGroup1 burst during the expiratory phase.
- Intermittent coupling mode shows mixed features of synchronous and monophasic coupling mode but with irregular variation in burst duration and interburst interval (Fig. 2, Intermittent). Frequently, we also obtained a more regular coupling between NeuronGroup1 and NeuronGroup2 for identical values of excitatory and inhibitory synaptic connections, which we termed as Intermittent (regular)—a pattern in which synchronous and monophasic coupling patterns are alternating (Fig. 2, Intermittent (regular)). Since the occurrence domain of Intermittent (regular) overlaps with that of the conventional Intermittent coupling (see Fig. 3, explanation for which is presented in the following paragraph), we decided to treat these two patterns collectively so as to gain some simplicity in the presentation of results.

Figure 3(a) shows the domain of various coupling modes observed as a function of  $\bar{g}_{\text{syn(ext)}}$  max and  $\bar{g}_{\text{syn(inh)}_{-\text{max}}}$ . Seven simulations were done for each combination of  $\bar{g}_{\text{syn(ext)\_max}}$  and  $\bar{g}_{\text{syn(inh)\_max}}$  and the occurrence frequencies of each coupling mode are also shown. The boundaries of various coupling mode domains in Fig. 3(a) cannot be precisely determined, because the coupling modes changed slightly every time with the assignment of random initial values for the various synaptic conductance and  $\bar{g}_{NaP}$  conductance. Figure 3(b) shows the domain of various coupling modes based on their maximum frequency of occurrence. It is remarked that occasionally the coupling patterns obtained in 2:1 coupling domain could not be meaningfully classified. The values of  $\bar{g}_{\text{syn(ext)}}$  max and  $\bar{g}_{\text{syn(inh) max}}$  are low in this region and thus the bursting behavior of NeuronGroup1 and NeuronGroup2 in some simulations were largely uncoupled.

### 3.2 Simulating the effects of decrease in preBötC neuronal excitability

We simulated the effect of decrease in preBötC neuronal excitability by increasing the leak current conductance  $\bar{g}_L$  (used for the computation of leakage current

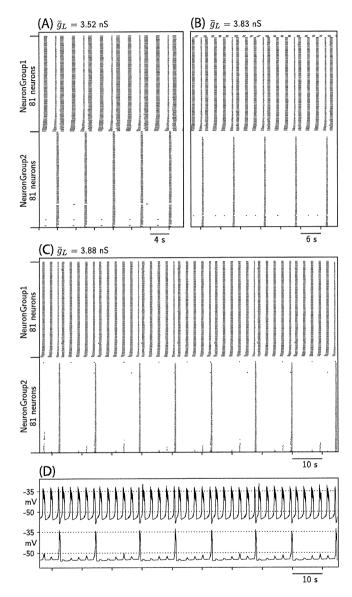
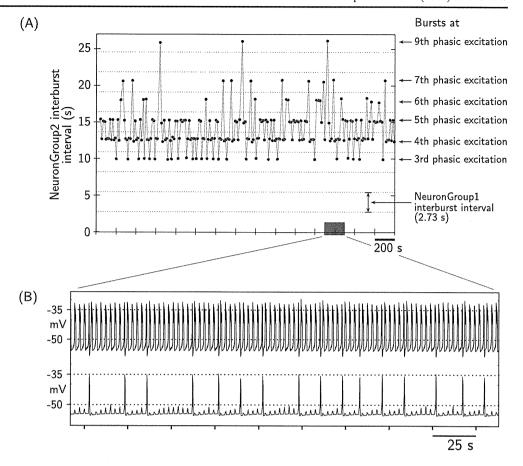


Fig. 4 Effect of increase in  $\bar{g}_L$  value on the coupling mode between NeuronGroup1 and NeuronGroup2. With the successive increase in  $\bar{g}_L$ , the coupling mode which is originally biphasic (Fig. 2(a), biphasic) changes to (a) 2:1 coupling, (b) 3:1 coupling and eventually (c) quantal slowing—NeuronGroup2 exhibits bursting non-deterministically at fourth or fifth phasic excitations from NeuronGroup1. In raster plots, the neurons within each neuronal groups are ranked in ascending order of their bursting activity initiation timings for better visualization. (d) Averaged population activity of NeuronGroup1 (top trace) and NeuronGroup2 (bottom trace) corresponding to the quantal slowing case depicted in (c)



Fig. 5 (a) Plot depicting the non-deterministic variation of interburst interval of Neuron Group 2 with time. The vertical separation between the horizontal grid lines indicates the interburst interval of NeuronGroup1. Neuron Group 2 exhibits bursts, non-deterministically, at the third, fourth, fifth, sixth, seventh and ninth phasic excitatory drives from NeuronGroup1. (b) Population activities of NeuronGroup1 and Neuron Group 2 for the time interval depicted by the thick gray bar in (a). For the above simulation, the values of  $\bar{g}_{\text{syn(ext)}_{\text{max}}}, \bar{g}_{\text{syn(inh)}_{\text{max}}}$  and  $\bar{g}_L$  were 0.8 nS, 4.5 nS and 3.89 nS, respectively



 $I_{\rm L}$  (Butera et al. 1999a)) for the neurons constituting NeuronGroup2 and studied its effect on the coupling pattern using the dual oscillator model. We studied the case when  $\bar{g}_{\text{syn(ext)}_{\text{max}}} = 0.8 \text{ nS}$  and  $\bar{g}_{\text{syn(inh)}_{\text{max}}} =$ 4.5 nS, which consistently produces a biphasic coupling pattern in our simulation (Figs. 3 and 2(a)). When  $\bar{g}_{\rm L}$  is increased, the number of cells with pacemaker property in NeuronGroup2 decreases (Fig. 10). When  $\bar{g}_L$  is increased beyond 3.4 nS, none of the Neuron-Group2 neurons show pacemaker property. In this situation, NeuronGroup1 is the sole rhythm generator, and NeuronGroup2 is the inspiratory pattern generator triggered by NeuronGroup1 due to the excitatory synaptic connection from NeuronGroup1 to NeuronGroup2 ( $\bar{g}_{syn(ext) max} = 0.8$  nS). We observed 2:1 coupling, 3:1 coupling and eventually quantal slowing of bursting rhythms between NeuronGroup1 and NeuronGroup2 (Fig. 4), as the value of  $\bar{g}_L$  was successively increased. In Fig. 4(c), NeuronGroup2 nondeterministically exhibits bursts at the fourth or fifth phasic excitations from the NeuronGroup1. Figure 5 depicts the non-deterministic variability in the interburst interval of NeuronGroup2 for a long duration simulation of quantal phenomenon; the quantal distribution of the interburst interval is readily apparent.

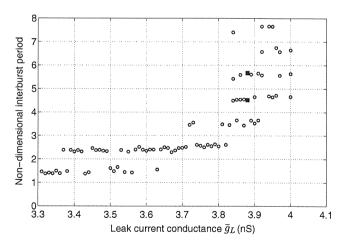
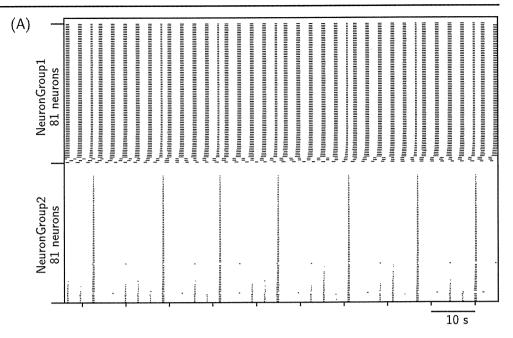


Fig. 6 Interburst interval of NeuronGroup2 as a function of  $\bar{g}_L$ . The interburst interval of NeuronGroup2 is non-dimesionlized to remove the variability in interburst interval of NeuronGroup2 caused by variability in the interburst interval of NeuronGroup1. A new simulation is performed for each value of  $\bar{g}_L$ . For  $\bar{g}_L < 3.84$  nS, we observed single bursting frequency of NeuronGroup2. Quantal slowing was observed in the range 3.84 nS  $\leq \bar{g}_L \leq 4.0$  nS; multiple data points corresponding to the same value of  $\bar{g}_L$  in this range depicts the multiple interburst intervals observed. For example, the two solid squares depicts the the two interburst interval of NeuronGroup2 obtained for the case  $\bar{g}_L = 3.88$  nS shown in Fig. 4(c)



Fig. 7 Quantal slowing observed when  $\bar{g}_{\text{NaP}_{\text{max}}}$  of NeuronGroup2 was reduced to 2.09 nS ( $\bar{g}_{\text{syn(ext)}_{\text{max}}} =$ 0.8 nS,  $\bar{g}_{\text{syn(inh)_max}} = 4.5 \text{ nS}$ ). (a) Raster plots depicting the bursting activity of neurons within Neuron Group 1 and Neuron Group 2, and (b) Averaged population activity within Neuron Group 1 and Neuron Group 2 (top and bottom trace, respectively). In raster plot, the neurons within each neuronal groups are ranked in ascending order of their bursting activity initiation timings for better visualization



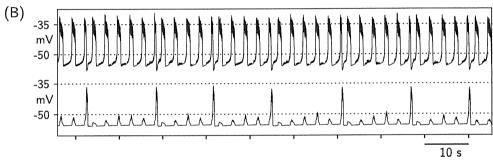
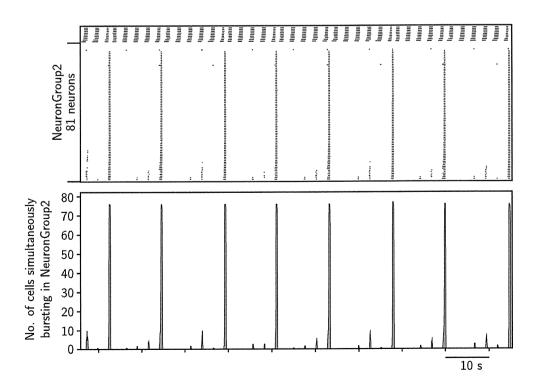


Fig. 8 Histograms showing the number of cells in NeuronGroup2 exhibiting simultaneous bursting during the quantal slowing case depicted in Fig. 4(c)





However, the quantal slowing phenomenon was not observed in every simulation; the occurrence rate was about 70%; in the rest of the cases we obtained regular 4:1 or 5:1 coupling between NeuronGroup1 and NeuronGroup2, similar to the regular 3:1 coupling depicted in Fig. 4(b). This was because, for every simulation, we assigned different random values to  $\bar{g}_{NaP}$ ,  $\bar{g}_{syn(int)}$ ,  $\bar{g}_{syn(ext)}$ , and  $\bar{g}_{syn(inh)}$ ; the occurrence of quantal slowing was sensitive to the variability in bursting property of constituent neurons and distributions of the synaptic conductances.

Figure 6 depicts the interburst interval of NeuronGroup2 as a function of  $\bar{g}_L$ . To make the quantal slowing effect apparent, the interburst interval of NeuronGroup2 is non-dimensionalized with the interburst interval of NeuronGroup1. There is some variability in the interburst interval of the Neuron-Group1 due to their random initialization. Since, at elevated values of  $\bar{g}_L$  for neurons in Neuron-Group2, only NeuronGroup1 is rhythm generator and NeuronGroup2 bursts under the influence of excitatory phasic drives from Neuron Group 1, the variability in the interburst interval of NeuronGroup1 is translated to variability in the interburst interval of NeuronGroup2. Non-dimensionlization eliminates this variability dependence and makes the quantal slowing effect pronounced.

The decrease in preBötC excitability is also simulated by reducing  $\bar{g}_{\text{NaP\_max}}$  value of NeuronGroup2. When pursued this course, setting  $\bar{g}_{\text{syn(ext)\_max}} = 0.8$  nS and  $\bar{g}_{\text{syn(inh)\_max}} = 4.5$  nS in the dual oscillator model, we observed similar changes in coupling mode between NeuronGroup1 and NeuronGroup2 as depicted in Fig. 4 as the  $\bar{g}_{\text{NaP\_max}}$  value was lowered; the coupling pattern successively changed from initial biphasic mode to 2:1 coupling, then to 3:1 coupling which eventually lead to quantal slowing. Figure 7 depicts a typical case of quantal slowing obtained by reducing  $\bar{g}_{\text{NaP\_max}}$  value.

To gain insight into mechanism causing quantal slowing, further investigations were made. The histograms in Fig. 8 show the number of cells in the *Neuron-Group2* simultaneously bursting during the quantal slowing case depicted in Fig. 4(c). Almost all cells in *NeuronGroup1* showed synchronized activity and hence their activity is not shown. Note that a small fraction of neurons in the *NeuronGroup2*, variable in number, exhibited bursting by excitatory phasic drives from *NeuronGroup1* in the interval between successive synchronized *NeuronGroup2* bursting. Next, we removed the interconnections within *NeuronGroup2*, and investigated the number of neurons that exhibit bursting by phasic drives from *NeuronGroup1* under such condition. To do this, we set  $\bar{g}_{\text{syn(ext)},\text{max}} = 0.8 \text{ nS}$ 

and  $\bar{g}_{\text{syn(inh)_max}} = 0$  nS, and for all *NeuronGroup2* cells, we set  $\bar{g}_{\text{syn(int)}} = 0$ .

Consequently, the dual oscillator model was modified as follows: (1) NeuronGroup1 remains unchanged, (2) NeuronGroup2 becomes essentially a group of unconnected 81 neurons, and (3) the excitatory synaptic connection from NeuronGroup1 to Neuron Group 2 is present ( $\bar{g}_{\text{syn(ext)}}$  max = 0.8 nS) but the inhibitory synaptic connection from NeuronGroup2 NeuronGroup1 is absent. Subsequently, we successively increased the value of  $\bar{g}_L$  for neurons in NeuronGroup2 and studied the time history of neurons exhibiting bursting in NeuronGroup2 quantitatively. Figure 9 depicts the details of one representative study when  $\bar{g}_L = 3.85$  nS for neurons in NeuronGourp2. For the elevated value of  $\bar{g}_L = 3.85$  nS, none of the neurons in NeuronGroup2 possess pacemaker property (Fig. 10). However, under the influence of excitatory phasic drives from NeuronGroup1, a total of 19 (out of 81) neurons in NeuronGroup2 exhibit bursting at various instances. Moreover, not all 19 neurons in NeuronGroup2 exhibit simultaneous bursting;

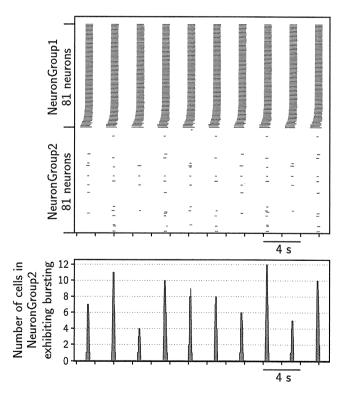
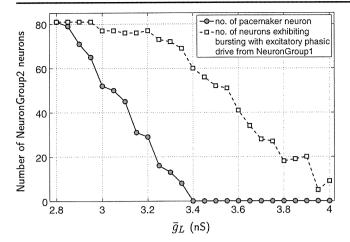


Fig. 9 Variability in the number of neurons in *NeuronGroup2* exhibiting bursting under the influence of excitatory phasic drive from *NeuronGroup1*. The neurons in *NeuronGroup2* are unconnected  $(\bar{g}_{\text{syn(int)}} = 0 \text{ nS})$  for all neurons in *NeuronGroup2*) and  $\bar{g}_{\text{syn(ext)_max}} = 0.8 \text{ nS}$  and  $\bar{g}_{\text{syn(inh)_max}} = 0 \text{ nS}$ . In raster plot, the neurons within *NeuronGroup1* are ranked in ascending order of their bursting activity initiation timings for better visualization





**Fig. 10** Typical decrease in the number of neurons with pacemaker property in NeuronGroup2 as  $\bar{g}_L$  value is increased

the histograms in Fig. 9 show the variation in the number of neurons that exhibit simultaneous bursting at each excitatory phasic drive from NeuronGroup1. A maximum of 12 and a minimum of 4 neurons in NeuronGroup2 exhibit simultaneous bursting, indicating that there is considerable variability. The number of neurons in NeuronGroup2 that exhibit bursting with the influence of excitatory phasic drives from NeuronGroup1 for different values of  $\bar{g}_L$  is shown in Fig. 10.

### 4 Discussion

# 4.1 Coupling modes of pFRG and preBötC rhythm-generating networks

Our model could produce 1:1 coupling of bursting rhythms between pFRG and preBötC with the characteristic biphasic pre-inspiratory and post-inspiratory firing pattern of pFRG neurons. Post-inspiratory burst of *NeuronGroup1* neurons during biphasic coupling, characteristic of Pre-I neurons, is the consequence of recovery from  $I_{\text{NaP}}$  inactivation during inspiration-related inhibition of the Pre-I firing in our model (post-hyperpolarization rebound bursting (Butera et al. 1999a)).

Our results indicated that the coupling modes depend on the strengths of synaptic connections between the two networks. When we view the coupling modes as a function of the strengths of excitatory input from NeuronGroup1 to NeuronGroup2 ( $\bar{g}_{syn(ext)_max}$ ) and inhibitory input from NeuronGroup2 to NeuronGroup1 ( $\bar{g}_{syn(inh)_max}$ ), three major domains are recognized: (1) synchronous coupling domain with a low inhibitory

strength, (2) biphasic coupling domain with a high inhibitory strength and low/moderate excitatory strength, and (3) monophasic coupling domain with high excitatory and high inhibitory strengths (Fig. 3). The changes in coupling mode by the inhibitory synaptic strength are consistent with experimental results. When a GABA antagonist (bicuculline or picrotoxin) or a glycine antagonist (strychnine) is given to the perfusate of brainstem spinal cord preparations, IIPI becomes absent or negligible, and the activity of Pre-I neurons overlaps with the C4VR inspiratory activity (Onimaru et al. 1990). These findings are in agreement with the model prediction when the strength of inhibitory connection from *NeuronGroup2* to *NeuronGroup1* is reduced.

Between the synchronous and biphasic major domains, there exists the domain of 2:1 coupling 'with inhibition' for moderate values of  $\bar{g}_{syn(inh)_max}$  (Fig. 3). The 2:1 coupling 'with inhibition' may be viewed as a precursor to biphasic coupling as the coupling mode transits from synchronous to biphasic with an increase in inhibitory strength. In the case of 2:1 coupling 'with inhibition', the inhibitory strength is not strong enough to cause an immediate post hyperpolarization rebound bursting of NeuronGroup2 as in biphasic coupling; the bursting of NeuronGroup2 is considerably delayed. We observed EPSPs in NeuronGroup2 neuronal membrane trajectories coincident with the rebound bursts of NeuronGroup1. These EPSPs could not evoke NeuronGroup2 burst because of two reasons: (1) low value of  $\bar{g}_{\text{syn(ext)_max}}$ , and (2) the timing of excitatory inputs to NeuronGroup2 from its previous burst is too close. With an increase in the value of  $\bar{g}_{\text{syn(ext) max}}$ , excitatory inputs to the neurons of NeuronGroup2 increase, causing it to burst every time the pFRG bursts, thus transforming the 2:1 coupling to the intermittent coupling mode (Fig. 3).

Likewise, the 2:1 coupling 'without inhibition', which is primarily found to the left of the synchronous coupling domain and for extremely low values of inhibitory strength, may be viewed as a precursor to synchronous coupling. In 2:1 coupling 'without inhibition', the excitatory strength is not strong enough to cause a synchronized bursting of NeuronGroup2 at each phasic excitation from NeuronGroup1; instead it synchronizes at every alternate phasic excitation from Neuron-Group1. It may be noted that the cases of 2:1 coupling 'with' and 'without inhibition' presented in Fig. 2 lie at the two extremities of the 2:1 coupling domain marked in Fig. 3(b); thus, the difference between them is readily evident. However, the transition from 'without inhibition' form of 2:1 coupling to 'with inhibition' form is extremely smooth; therefore, we merged the two cases



together while determining the coupling domains in Fig. 3.

As 2:1 'with inhibition' coupling mode transits to intermittent coupling mode with increase in the value of  $\bar{g}_{\text{syn(ext) max}}$ , biphasic mode transits to monophasic coupling mode with increase in the value of  $\bar{g}_{\text{syn(ext) max}}$ . For the biphasic coupling mode, the value of  $\bar{g}_{\text{syn(ext) max}}$  is relatively low. Consequently, the EP-SPs provided by NeuronGroup1 at the time of its post inspiratory burst to NeuronGroup2 is not sufficient to make it burst again. However, for higher values of  $\bar{g}_{\text{syn(ext)},\text{max}}$ , as in the case of monophasic coupling, the post-inspiratory burst of NeuronGroup1 provides high enough EPSPs to NeuronGroup2, causing it to burst again (Fig. 2, Monophasic). Since the interval between pre-inspiratory and post-inspiratory bursts of NeuronGroup1 is very small, the frequency of bursts in monophasic coupling mode is high. It may be observed that the excitation-inhibition cycle (excitation of NeuronGroup2 by NeuronGroup1 and inhibition of *NeuronGroup1* by *NeuronGroup2*) continues infinitely in monophasic coupling, whereas in case of intermittent coupling, the excitation-inhibition cycle intermittently breaks and restarts again. This suggests that the excitation-inhibition cycle is more stable when both  $\bar{g}_{\text{syn(ext)} \text{ max}}$  and  $\bar{g}_{\text{syn(inh)} \text{ max}}$  are high.

To illustrate the predictive capability of dual oscillator model, it was remarked earlier in this section that biphasic and synchronous coupling modes are experimentally observed cases. In the same regard, it may also be of significance to note that the 2:1 coupling 'with inhibition' as depicted in Fig. 2 and the 2:1 coupling depicted in Fig. 4(a) are also observed in experimental conditions (Okada et al. 2007), which adds to the predictive capability of the model.

### 4.2 Mechanisms of quantal slowing

During quantal slowing, subthreshold phasic drives to preBötC inspiratory neurons are observed coincident with the timing of skipped inspiratory burst. Based on this observation together with non-deterministic jumps of the bursting period to integer multiples of the control period, Mellen et al. (2003) have suggested that opioid-induced quantal slowing results from transmission failure from unaffected Pre-I neurons to depressed pre-BötC networks. In addition, they have also mentioned that noisy mutual coupling between the rhythmically active preBötC and the pFRG networks could be an alternative explanation of quantal slowing. Following this, Wittmeier et al. (2008) simulated the quantal slowing phenomenon by incorporating *stochastic* excitatory synaptic transmission from pFRG to preBötC

and reducing its (mean) conductance by 12.5% of control. Thereby, they reinforced the suggestion that quantal slowing results from both transmission failure and noisy mutual coupling between pFRG and preBötC.

In the present study, however, quantal slowing was observed without assuming transmission failure or noisy interactions. Here we use the term 'transmission failure' specifically as a suppression of excitatory synaptic transmission from pFRG to preBötC. The results of the present study are both new and simple; 'simple' in the sense that the basic dual oscillator model by itself is adequate to simulate quantal slowing without incorporating any additional hypothesis like transmission failure or noisy mutual coupling. Nevertheless, under some experimental conditions, these processes may contribute secondarily to the primary mechanism of quantal slowing as explained in the following paragraph.

The quantal slowing phenomena stems from the fact that the synchronized bursting of NeuronGroup2 is governed by the states of a small fraction of neurons in it that exhibit bursting by phasic excitatory drives from NeuronGroup1 under elevated values of  $\bar{g}_L$  or decreased values of  $\bar{g}_{NaP_max}$  for neurons in Neuron-Group2 (Fig. 10). These small fraction of neurons provide excitatory inputs to the other quiescent neurons of NeuronGroup2 and help them to burst. If the total number of neurons in NeuronGroup2 exhibiting bursting exceeds a 'critical value', it results in a selfsustained chain of events where progressively larger number of neurons of NeuronGroup2 exhibit bursting and eventually all the neurons in NeuronGroup2 exhibit synchronized bursting. On the other hand if the number of bursting neurons in NeuronGroup2 falls short of the critical value, then the neurons in NeuronGroup2 do not exhibit synchronized bursting. Figure 9 depicted variability in the number of neurons in NeuronGroup2 exhibiting bursting by excitatory phasic drives from NeuronGroup1. Though, the case presented in Fig. 9 corresponds to unconnected neurons in NeuronGroup2, it is likely that similar variability, albeit to a different degree, exists even when the neurons in NeuronGroup2 are interconnected through chemical synapses. This is evident if one compares the similarity in the bursting activity of a small fraction of NeuronGroup2 neurons in the interval between synchronized bursting in Fig. 8 (and Fig. 7) with that of the uncoupled neurons in NeuronGroup2 depicted in Fig. 9. Consequently, the number of bursting neurons in NeuronGroup2 exceeds the critical number intermittently and synchronized NeuronGroup2 bursting occurs. This results in quantal slowing of synchronized



bursting of NeuronGroup2. From our simulation study, we observed that a maximum of about 15 neurons in NeuronGroup2 exhibit bursting when NeuronGroup2 fails to exhibit synchronized bursting. Thus, the 'critical number' of bursting neurons that necessarily be surpassed for synchronized NeuronGroup2 bursting may be greater than 15 (out of 81) neurons. The critical number is expected to be fuzzy rather than precisely defined. The fuzziness stems from the fact that the distribution of  $\bar{g}_{NaP}$  and  $\bar{g}_{syn(int)}$  among NeuronGroup2 neurons is randomly assigned. Moreover, the critical number is a function of the network topology as well (see Section 4.3). For a neuronal group where the constituent neurons are interconnected in a different way than what we have considered here, the critical number is different. However, the qualitative aspects of the results, such as intermittent failure of Neuron-*Group2* to exhibit synchronized bursting, are generally expected and could be an underlying mechanism of quantal slowing.

Quantal slowing was not observed in 30% of the simulations. In these cases, the distributions of random values of  $\bar{g}_{NaP}$  and  $\bar{g}_{syn(int)}$  within NeuronGroup2 are such that its constituent neurons are relatively better synchronized. This was evident from visual observation of the raster plots obtained for these cases, which resembled the regular coupling pattern in Fig. 4(b). Consequently, there is no intermittent failure of NeuronGroup2 to exhibit synchronized bursting and hence no quantal slowing is observed. In such cases, the activity of the neuronal groups, both NeuronGroup1 and NeuronGroup2, may be essentially captured by replacing each of them with a single pacemaker neuron. This probably explains why Wittmeier et al. (2008) could not simulate quantal slowing phenomenon with their simplified model unless they incorporated stochastic synaptic transmission. The simplified model lacks the complexity necessary to capture the essential source of (apparent) non-determinism resulting the quantal slowing phenomenon (as discussed in the previous paragraph), which is intrinsic in the neuronal population model that we have considered. It is important to realize that the non-determinism associated with the occurrence of quantal slowing simulation is an 'apparent' one—the dual oscillator model used to simulate quantal slowing is deterministic; it is the nonlinearity present in the bursting behavior of individual neurons within the neuronal groups that result in nondeterministic-like intermittent synchronized bursts of NeuronGroup2. Thus, our results also hint toward the fact that quantal slowing may not necessarily be derived from any stochastic processes but may actually be a deterministic phenomena.

Figures 5 and 6 suggests that the interburst durations of *NeuronGroup2* while exhibiting quantal slowing are not integer multiples of the control period but are instead fractional multiples. Interestingly, this was elucidated by Wittmeier et al. (2008) as well, though they achieved it by incorporating a stochastic synaptic transmission. Consequently, it may be inferred that the fractional nature of quantal slowing is primarily a characteristic of dual oscillator models and is independent of the mechanism inducing the non-determinism.

## 4.3 Relation of preBötC neuronal network topology to quantal slowing

We have assumed that each neuron of *Neuron-Group2* is synaptically connected to every other neuron within *NeuronGroup2* ("all-to-all" connectivity). Consequently, the intra-neuronal group synaptic current  $I_{\text{syn(int)}}$  for individual neurons of *NeuronGroup2* (the first term on the right hand side of Eq. (2)) is:

$$I_{\text{syn(int)}} = \left(\sum_{l \in L} g_{\text{syn(int)}}^{l} \cdot s_{\text{int}}^{l}\right) \left(V - E_{\text{syn(e)}}\right) \tag{8}$$

where L is NeuronGroup2. However, we subsequently reduced the above equation to

$$I_{\text{syn(int)}} = \bar{g}_{\text{syn(int)}} \cdot \bar{s}_{\text{int}} \left( V - E_{\text{syn(e)}} \right) \tag{9}$$

(refer Section 2.2, in particular the reduction of Eq. (2) to Eq. (3)) and then randomly assigned values to  $\bar{g}_{\rm syn(int)}$  from a uniformly distributed probability density function ranging between 0 and 10 nS. Since,  $\bar{s}_{\rm int}$  is the same for all the neurons, it is primarily the variability in the values of  $\bar{g}_{\rm syn(int)}$  across the neurons in *NeuronGroup2*, which contributes to the variability in the intra-neuronal synaptic currents for individual neurons of *NeuronGroup2*. From synchronization perspective, a neuron with low value of  $\bar{g}_{\rm syn(int)}$  may be considered as weakly connected to rest of the neurons within *Neuron-Group2* and vice versa.

It is remarked that the reduction of Eq. (8) to Eq. (9) modifies the intrinsic homogeneity present in "all-to-all" network connectivity. If we randomly assign values to  $g_{\text{syn(int)}}^l$  from a uniformly distributed probability density function of any appropriate range, and perform the summation shown in Eq. (8), the variability in the individual values of  $g_{\text{syn(int)}}^l$  will be equalized resulting in almost homogeneous distribution of  $I_{\text{syn(int)}}$  across the neurons of NeuronGroup2. Homogeneous distribution of  $I_{\text{syn(int)}}$  within NeuronGroup2 would imply that each neuron is connected equally strongly to rest of the neurons within NeuronGroup2. Since this is unlikely to be the case in the real preBötC, we presume that



our way of introducing variability in the distribution of  $I_{\rm syn(int)}$  across the neurons of NeuronGroup2 is qualitatively more realistic. The significance of the usage of uniformly distributed probability density functions for randomly assigning the values to  $\bar{g}_{\rm syn(ext)}$  and  $\bar{g}_{\rm syn(inh)}$  in the model may be interpreted similarly.

Now, since in our simulations, quantal slowing is observed primarily due to intermittent failure of NeuronGroup2 to exhibit synchronized burst, it is remarked that the ability of NeuronGroup2 to exhibit synchronized bursts is intrinsically dependent on its network topology, in particular, the distribution of  $I_{\text{syn(int)}}$  across the neurons of NeuronGroup2. In the quantal slowing simulation, Fig. 4(c) for example, we observe that NeuronGroup2 mostly exhibits synchronized bursts at every fourth phasic excitation from NeuronGroup1 but frequently it skips the fourth phasic excitation from NeuronGroup1 and bursts at the fifth phasic excitation. Thus, once NeuronGroup2 has exhibited a synchronized burst, there is an element of (apparent) non-determinism whether it will exhibit its next synchronized bust at the fourth phasic excitation from Neurongroup1 or not. However, in experimentally observed quantal slowing, preBötC elucidates nondeterminism in its busting at each phasic excitation of pFRG (Mellen et al. 2003). We reason that this discrepancy is probably due to the difference in the neuronal network topology of real preBötC as compared to the one we have incorporated in NeuronGroup2.

Thus, it is remarked that the highlight of the present simulation study of quantal slowing is only its essential qualitative feature—the (apparent) non-determinism associated with bursting of preBötC—and the potential mechanism causing it. The quantitative features of quantal slowing may only be simulated by incorporating a more realistic network topology for *Neuron Group 2*.

### 4.4 Some additional simulation studies

In the model presented above, we introduced variability in bursting frequencies of the constituent neurons of NeuronGroup1 and NeuronGroup2 by providing variability in the allocated value of persistent Na<sup>+</sup> current conductance  $\bar{g}_{NaP}$  of neurons. The variability in bursting frequencies may also be introduced by providing variability in the leakage current conductance  $\bar{g}_L$  of neurons keeping the  $\bar{g}_{NaP}$  value fixed. We pursued this course too and verified that all the qualitative features presented above remains unchanged. For this study, we randomly assigned  $\bar{g}_L$  to neurons of each neuronal group from a uniform probability distribution function ranging from 2.3 to 2.8 nS; we set  $\bar{g}_{NaP} =$ 

3.5 nS for all neurons of NeuronGroup1 and  $\bar{g}_{NaP} = 2.5$  nS for that of NeuronGroup2, so that the bursting frequency of NeuronGroup1 is higher than that of NeuronGroup2.

Further, we used a Gaussian distribution (with a standard deviation of 0.3 nS about the mean values of  $\bar{g}_{NaP} = 3.5$  nS for NeuronGroup1 and  $\bar{g}_{NaP} = 2.45$  nS for NeuronGroup2) instead of the uniform distribution, for allocating the values of  $\bar{g}_{NaP}$  to individual neurons. Again the qualitative features of results obtained were essentially the same as presented above. Thus, it is suggested that the results presented in the manuscript are independent of the mode of introducing the variability in bursting frequencies of the constituent neurons of the neuronal groups.

### 5 Model justification

We assumed that the intrinsic bursting frequency of pFRG is faster than that of preBötC. This is a prerequisite for the consistent firing of pFRG neurons before the burst of preBötC neurons. To our knowledge, this assumption has never been tested experimentally. The intrinsic bursting rhythm of pFRG neurons, separated from preBötC can be monitored from the facial nerve rootlet, however, the inherent bursting frequency of the pFRG is difficult to determine because the rhythm is suppressed by pons or other brain regions with the facial nerve attached (Onimaru et al. 2006). In the dual oscillator model, we simulated by reversing the bursting frequencies of NeuronGroup1 and NeuronGroup2, that is by setting  $\bar{g}_{NaP\_max} = 3.0 \text{ nS}$  for NeuronGroup1 and  $\bar{g}_{\text{NaP max}} = 4.0 \text{ nS for } NeuronGroup2. \text{ We did not obtain}$ the characteristic biphasic coupling for any combination of excitatory and inhibitory synaptic strengths (the range of synaptic strengths considered for this study was the same as that in Fig. 3).

We assumed that the persistent Na<sup>+</sup> current is responsible for rhythmic bursts of pFRG and preBötC neurons. This assumption has been recently contradicted. Pace et al. (2007a) have demonstrated that  $I_{\text{NaP}}$  does not contribute to inspiratory drive potential generation in the vast majority of preBötC neurons. Another intrinsically bursting neuronal group has been identified in the preBötC, which is dependent on a calcium-activated nonspecific cationic current ( $I_{\text{CAN}}$ ) (Peña et al. 2004). However, the relative contribution of pacemaker properties and synaptic inputs to rhythm generation is likely to be dynamic (Johnson 2007). For example, during hypoxia, the respiratory pattern generator is more dependent on pacemaker properties and produces gasping behavior (Paton et al. 2006). Further



recent data of Koizumi et al. (2008) from neonatal rats contradict the data of Pace et al. (2007b) from mice, and show that inspiratory rhythm generation can be  $I_{\text{NaP}}$ -dependent in the isolated preBötC network in vitro. Therefore, although we did not consider  $I_{\text{CAN}}$ , the breakdown of synchronized burst could still be the underlying mechanism of quantal slowing in certain conditions.

It has been shown that glutamatergic excitatory synaptic inputs are required to evoke the  $I_{\rm CAN}$ -dependent inspiratory drive potentials (Pace et al. 2007b), suggesting that the rhythmic burst is generated by a "group pacemaker" mechanism (Feldman and Del Negro 2006) in which rhythm generation is an emergent property of the network. Recently, Rubin et al. (2009) proposed a mathematical model of the neurons exhibiting "group pacemaker" mechanism. However, this model lacks the post-hyperpolarization rebound bursting dynamics which is essential for producing the post-inspiratory burst of pFRG, and thus we cannot use this neuronal model to simulate and study quantal slowing.

We simulated the opioid-induced reduction of excitability in preBötC bursting neurons both by increasing  $\bar{g}_L$  and by reducing  $\bar{g}_{NaP_max}$ . However, we do not know how opioids depress preBötC neurons. Opioids activate a G-protein-coupled inwardly rectifying potassium conductance known as  $G_{irk}$ , resulting in the hyperpolarization of neurons throughout the central nervous system (Williams et al. 1982; Wimpey and Chavkin 1991). Therefore, the depressant effect of opioids on preBötC may be reasonably simulated by an increase in  $\bar{g}_L$ . On the other hand, it is unlikely that opioids directly affect  $\bar{g}_{NaP_max}$  because pFRG bursting neurons, which are  $I_{NaP}$ -dependent (Onimaru et al. 1997), are not affected by opioids (Takeda et al. 2001; Janczewski et al. 2002).

Since the two putative rhythm-generating networks are embedded hierarchically in the central respiratory pattern-generating network in more intact animals (Smith et al. 2007), dynamic interactions among neuronal groups must not be so simple. Opioid-induced quantal slowing has been observed in juvenile (Mellen et al. 2003) and adult (Vasilakos et al. 2005) rats in vivo. These observations can be interpreted as the manifestation of dynamic interactions between fundamental-level networks. However, it has been reported that eupnea of in situ intra-arterially perfused rats persists following the blockade of the two burst-generating currents,  $I_{\text{NaP}}$ and  $I_{\text{CAN}}$  (St.-John 2008). Therefore, whether the dual oscillator configuration is the fundamental-level network component of eupnea or that of gasping remains to be clarified.

In summary, we developed a dual oscillator model to understand the dynamic interactions between pFRG and preBötC neurons. Our model essentially assumes (1) both pFRG and preBötC networks are rhythm generators, (2) preBötC receives excitatory inputs from pFRG, and pFRG receives inhibitory inputs from pre-BötC, and (3) persistent Na<sup>+</sup> current conductance and synaptic current conductances are randomly distributed. Our model could produce the characteristic behaviors observed experimentally in neonatal brainstem spinal cord preparations. The coupling mode depended on the strengths of excitatory and inhibitory connections of the oscillator. In contrast to the earlier suggestions, quantal slowing was observed without transmission failure (suppressed excitatory synaptic conductance) or noisy mutual interactions between the neuronal networks of the oscillator. Our study suggests that quantal slowing may actually be a deterministic phenomena and the non-determinism associated with it may only be an 'apparent' one. We suggest that quantal slowing results from inhomogeneous properties of individual cells within the oscillator and subsequent breakdown of synchronized bursting within the pre-BötC oscillator.

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# Detection and Visualization Method of Dynamic State Transition for Biological Spatio-Temporal Imaging Data

Fumikazu Miwakeichi\*, Yoshitaka Oku, Yasumasa Okada, Shigeharu Kawai, Yoshiyasu Tamura, and Makio Ishiguro

Abstract-In the statistical analysis of functional brain imaging data, regression analysis and cross correlation analysis between time series data on each grid point have been widely used. The results can be graphically represented as an activation map on an anatomical image, but only activation signal, whose temporal pattern resembles the predefined reference function, can be detected. In the present study, we propose a fusion method comprising innovation approach in time series analysis and statistical test. Autoregressive (AR) models were fitted to time series data of each pixel for the range sufficiently before or after the state transition. Then, the remaining time series data were filtered using these AR parameters to obtain its innovation (filter output). The proposed method could extract brain neural activation as a phase transition of dynamics in the system without employing external information such as the reference function. The activation could be detected as temporal transitions of statistical test values. We evaluated this method by applying to optical imaging data obtained from the mammalian brain and the cardiac sino-atrial node (SAN), and demonstrated that our method can precisely detect spatio-temporal activation profiles in the brain or SAN.

Index Terms—Biomedical optical imaging, brain mapping, innovation approach, time series analysis.

### I. INTRODUCTION

R ECENT progress in techniques to record biological signals offers detailed spatio-temporal information in the brain through various methods, e.g., functional magnetic res-

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- \*F. Miwakeichi is with the Department of Statistical Modeling, The Institute of Statistical Mathematics, Tachikawa, Tokyo 190-8562, Japan (e-mail: mi-wake1@ ism.ac.jp).
- Y. Oku is with the Department of Physiology, Hyogo College of Medicine, Nishinomiya, Hyogo 663-8501, Japan (e-mail: yoku@hyo-med.ac.jp).
- Y. Okada is with the Department of Physiology, Hyogo College of Medicine, Nishinomiya, Hyogo 663-8501, Japan (e-mail: yasumasaokada@1979.jukuin. kejo.ac.ip).
- S. Kawai is with the Department of Data Science, The Institute of Statistical Mathematics, Tachikawa, Tokyo 190-8562, Japan (e-mail: s-kawai@zpost.plala.or.jp).
- Y. Tamura is with the Department of Data Science, The Institute of Statistical Mathematics and the Department of Statistical Science, School of Multidisciplinary Sciences, The Graduate University for Advanced Studies, Tachikawa, Tokyo 190-8562, Japan (e-mail: tamura@ism.ac.jp).
- M. Ishiguro is with the Department of Statistical Modeling, The Institute of Statistical Mathematics and the Department of Statistical Science, School of Multidisciplinary Sciences, The Graduate University for Advanced Studies, Tachikawa, Tokyo 190-8562, Japan (e-mail: ishiguro@ ism.ac.jp).

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onance imaging (fMRI) and optical recording. The structure of fMRI data is four-dimensional, three of them are for space and one is for time axis. In other words, a time series corresponds to each spatial three-dimensional grid (voxel). The statistical significance of the brain activation can be evaluated by regression analysis or cross correlation analysis between the time series on each voxel and the reference function. This method is implemented in statistical parametric mapping (SPM) and has been widely used as a standard tool for analysis [1]. Then the distribution of test values such as t-values corresponding to regression coefficient or correlation coefficient is expressed on a certain slice of an anatomical image.

An optical imaging technique using a voltage-sensitive dye enables us to measure membrane potential changes in excitable tissue. The technique converts membrane potentials of cells to intensities of fluorescence emitted from the cells. Then the changes in fluorescence on the surface of certain regions of a brain preparation can be recorded using a high-speed high-sensitivity camera [2]-[4]. The structure of optical imaging data is three-dimensional, two of them are for space and one is for time axis. Although the structure of optical imaging data is similar to that of fMRI data, there has been no widely used method for data analysis. Respecting to this situation, Oku et al. [2], [3] and Okada et al. [4] applied time-lagged correlation analysis to optical imaging data to elucidate the mechanism of respiratory rhythm and pattern generation in the rat and frog brainstem. In the studies of rat brainstem [2], [4], they used fouth cervical spinal cord ventral root (C4VR) output signals that are equivalent to phrenic inspiratory burst activity as the reference function, and found appearances of earlier and simultaneous activities relative to the output signals in the regions of respiratory rhythm generators.

The advantage of regression analysis or cross correlation analysis is that the significance of the coefficients can be statistically evaluated. Moreover, the test values can be mapped on an anatomical image and it gives spatial information. However, still there have been several problems in these analyses. The regression or correlation analysis evaluates only the morphological resemblance between a time series and a reference function. If there is some activation pattern that does not resemble the reference function, then it cannot be detected. More seriously, in the case that the reference function cannot be defined, the data can hardly be analyzed by these methods.

In the field of time series analysis, innovation approach has been efficiently applied to detect the changes in signal dynamics. The dynamical properties of stationary time series, whose statistical properties, e.g., mean value and variance, do not depend on time, can be identified using mathematical models such as autoregressive (AR) model and autoregressive moving average (ARMA) model. Let us suppose that we prepare two time series; one is used as a test time series for model identification, and the other is for filtering with the identified model. If new time series is filtered through the identified model, unpredictable signals remain in residuals. The residuals are called innovations. If the amplitude of innovations of filter output becomes significantly higher than the innovation of test data, the state is detected as a phase transition of dynamics in the system. This approach has been applied in various fields, e.g., plant monitoring system [6]–[10].

In the present study, we applied the innovation approach to optical imaging data obtained from the mammalian brain and the cardiac sino-atrial node (SAN), and attempted to detect biological activation in innovations. In addition, we propose a new method of statistical evaluation for the data set that is recorded in repeated measurement and a method for visualizing spatio-temporal distribution of the statistical test values.

### II. METHODS

### A. Innovation Approach

The autoregressive (AR) model for a time series  $\eta(t)$ ,  $t=1,\ldots,S$ , is defined as a linear combination of the past values with a prediction error  $\varepsilon(t)$  and a constant  $\beta$ 

$$\eta(t) - \beta = \sum_{i=1}^{p} \alpha(i)\eta(t-i) + \varepsilon(t)$$
 (1)

where p denotes the model order and  $\alpha(i)$  are AR coefficients. The linear dynamic properties of the system can be identified with a parameter vector  $\boldsymbol{\vartheta} = \{\alpha(1), \dots, \alpha(p), \beta, \sigma_{\varepsilon}^2\}$ , here  $\sigma_{\varepsilon}^2$  is a variance of  $\varepsilon(t)$ . The innovations result from the residual time series can be estimated as

$$\varepsilon(t) = \eta(t) - \hat{\eta}(t) = \eta(t) - \left(\sum_{i=1}^{p} \alpha(i)\eta(t-i) + \beta\right) \quad (2)$$

and the signals that cannot be predicted by the linear AR process remain in the innovations. In other words, innovations are filter outputs through a linear AR process.

Considering an exogenous input  $\gamma(t)$ ,  $t=1,\ldots,S$ , the AR model can be generalized to an AR model with exogenous inputs (ARX) denoted as

$$\eta(t) - \beta = \sum_{i=1}^{p} \alpha(i)\eta(t-i) + \sum_{j=1}^{q} \phi(j)\gamma(t-j) + \varepsilon(t). \quad (3)$$

Suppose the measurement points of the imaging data are on the two dimensional pixel that are labeled by an index v=(l,m) and only the influences of nearest neighbor upon each pixel are considered as exogenous inputs, the ARX model will be specialized as

$$\eta^{v}(t) - \beta^{v} = \sum_{i=1}^{p} \alpha^{v}(i)\eta^{v}(t-i)$$

$$+ \sum_{u \in \mathcal{N}(v)} \sum_{j=1}^{q} \delta^{u}(j)\eta^{u}(t-j) + \varepsilon^{v}(t) \quad (4)$$

where N(v) is a set of indices of the neighbor pixels to the pixel at v=(l,m). Suppose neighbor pixels are restricted to the pixels, which contact with the edge of the pixel at the point v, a set of indices of neighbor pixels will be

$$N(v) = \{(l+1, m), (l, m-1), (l, m+1), (l-1, m)\}.$$
 (5)

The ARX model with the restricted neighbor pixels will be referred as nearest neighbor autoregressive model (NNAR) in this paper. The innovations for the pixel at  $\boldsymbol{v}$ 

$$\varepsilon(t)^{v} = \eta^{v}(t) - \hat{\eta}^{v}(t)$$

$$= \eta^{v}(t) - \left(\sum_{i=1}^{p} \alpha^{v}(i)\eta^{v}(t-i)\right)$$

$$+ \sum_{u \in \mathcal{N}(v)} \sum_{j=1}^{q} \delta^{u}(j)\eta^{u}(t-j) + \beta^{v}$$
(6)

contain the signals which cannot be predicted by a linear AR process even though the spatial influences from the neighbors are taken into consideration.

### B. Statistical Evaluation of Innovations and Graphical Representation

In the case imaging data are repeatedly recorded, we obtain multiple time series  $\eta^{w}(t)$ , t = 1, ..., S, for each pixel (w = (l, m, n), l and m are the indices of a pixel, n is the index)of the repetition,  $1 \le n \le N$ ) (Fig. 5). Suppose the NNAR model is identified with a limited period  $t_1 \le t \le t_2$ , any arbitrary selected other period  $t_1' \leq t \leq t_2'$  can be filtered through the identified NNAR model. Let the innovations corresponding to the period for the NNAR model identification and for filtering  $\varepsilon^{1,\boldsymbol{w}}(t)$  and  $\varepsilon^{2,\boldsymbol{w}}(t)$ , respectively. The amplitude level of  $\varepsilon^{2, \mathbf{w}}(t')$  will increase at the time point t' when the unpredictable signals arise. Then the statistical significance can be evaluated by comparing the mean value between the innovations at t',  $N^{-1}\sum_{n=1}^N \varepsilon^{2,(l,m,n)}(t')$  and whole innovations within the period  $t_1 \leq t \leq t_2$ ,  $(N(t_2-t_1))^{-1}\sum_{t=t_1}^{t_2}\sum_{n=1}^N \varepsilon^{1,(l,m,n)}(t)$ by some statistical test. In this study, we employed standard t-test for this purpose. By shifting time point t', time-dependent t-values can be computed. Then time-dependent activation t-map, which shows dynamic state transition, can be obtained by repeating this procedure for all pixels.

This method detects not only biological activation as dynamic state transition but also some artifact inevitably. Some procedure for artifact discrimination has to be considered. There are mainly two types of artifacts. One is stationary oscillatory noise such as those caused by electric power supply (hum noise) and mechanical vibration of measurement system. This sort of artifacts can be identified by AR-type model, and then  $\varepsilon^{1,\boldsymbol{w}}(t)$  will be close to Gaussian white noise. Therefore the oscillatory noise will not appear in  $\varepsilon^{2,\boldsymbol{w}}(t')$ , because these artifacts consist of predictable signals. The other is caused by nonstationary sporadic noise, and it will appear in  $\varepsilon^{2,\boldsymbol{w}}(t')$  because it cannot be predicted by the identified AR-type model. This sort of artifact can be partly removed from final results such as activation t-map by setting a threshold for spatial cluster size and/or duration.

### C. Time-Lagged Cross Correlation Analysis

The time-lagged cross correlation analysis provides temporal information of the appearance of the signals in the imaging data whose wave forms resemble predefined reference function [2]. Suppose  $\eta^{\boldsymbol{v}}(t)$  is a time series of imaging data for a pixel v=(l,m) and  $\varphi(t)$  is a predefined reference function, the lagged cross correlation can be denoted as

$$R^{v}(\tau) = \eta^{v}(t)\varphi(t-\tau)/\sqrt{\overline{(\eta^{v})^{2}}}\sqrt{\overline{\varphi^{2}}}$$
 (7)

where  $\tau$  is a relative time lag. A lagged correlation coefficient can be straightforwardly converted to a t-value. Then time dependent correlation t-map can be obtained if this procedure is repeated for all pixels. In the case  $\tau=0$ , it will be ordinary cross correlation analysis.

### D. Simulation

We intended to illustrate the effectiveness of the proposed method in this section with simulated data. The simulated data consist of sinusoidal and triangle waves that represent physiological activations superposed on a background oscillation. The background oscillation is generated by AR process defined as (1). The model order p, AR coefficients, constant level  $\beta$ and sampling frequency Fs are set to p = 2,  $\alpha(1) = 1.84$ ,  $\alpha(2) = -0.98$ ,  $\beta = 0$  and Fs = 50 [Hz], respectively, in order to generate 3 Hz background oscillation that can be observed in actual data sets. The sinusoidal wave is defined as a cosine curve  $-0.5 \cdot \cos(2\pi f \cdot (t - \delta)/\text{Fs}) + 0.5 (f = 0.5 \text{ Hz}, \delta = 1.0 \text{ s},$ 1.0 s < t < 2.0 s), which imitates the C4VR respiratory activity [Fig. 4(c)], and was used as the reference function for the time-lagged cross correlation analysis. The triangle wave is for an example of the signal whose waveform does not resemble the reference function. The onset time of triangle wave was set on the origin of the time axis, and the offset time was set on 0.52 s. the onset and offset time of sinusoidal wave were set on 1.0 s and 3.0 s, respectively [Fig. 1(a) and (b)]. We prepared 30 simulated data with generating different background oscillation. Fig. 1(c) and (d) show one of the simulated data with different values of the variance of prediction error in (1) ( $\sigma^2 = 0.0025$  and 0.0256, respectively).

The AR model was identified on the period between -5.0 s and -3.0 s (101 time frames). Subsequently, the period between -1.0–4.24 s (263 time frames) was filtered through the identified AR model. Fig. 3 shows the temporal transition of the amplitude of innovations for all repetitions. The area A is a set of the innovations within the period for model identification  $(\varepsilon^{1,\boldsymbol{w}}(t))$  and the line B is a set of innovations of filter output  $(\varepsilon^{2,\boldsymbol{w}}(t'))$  at the time t'. We evaluated the statistical significance of the difference of mean amplitude of the innovations in the area A and on the line B using standard t-test, and repeated the same procedure for the simulated data instead of the innovations. Fig. 2(a) and (c) displays the temporal transition of t-values of simulated data and innovations, respectively. The horizontal line in each figure corresponds to the significance level (p=0.05).

In case the variance of prediction error is sufficiently small ( $\sigma^2 = 0.0025$ ), the t-values correspond to the triangle and sinusoidal waves exceed the significance level for both the sim-

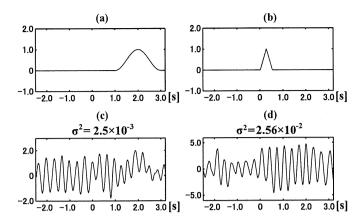


Fig. 1. The sinusoidal wave (a) and triangle wave (b) representing physiological activations. The simulated data with sinusoidal and triangle waves were superposed on the background oscillation generated by AR processes with different values of the variance of the prediction error (c), (d) ( $\sigma^2 = 0.0025$  and 0.0256, respectively).

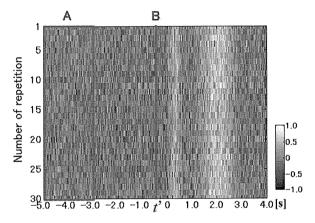


Fig. 2. Temporal transition of the amplitude of innovations for all simulated data (30 repetitions). The area A is the set of the innovations within the period of model identification and the line B is the set of the innovations of filter output at the time t'. The mean amplitude of innovations for each repetition was normalized between -1 to 1.

ulated data and innovations. As the variance of the prediction error is raised to 0.0256, the t-values of simulated data, which even do not correspond to these waves exceeds significant level, that is, it causes false positive error (Fig. 3(a) right). On the contrary, the t-values of innovations only which correspond to these waves exceed significance level (Fig. 3(c) right). It can be said that the false positive rate is well controlled in the t-test with the innovations.

The results of the time-lagged correlation analysis between averaged simulated data and the predefined reference function [Fig. 1(a)] are shown in Fig. 3(b). Since a correlation coefficient can be computed with a relative time lag, the time axis indicates the relative time lag  $\tau$  rather than the absolute time. And it is a natural consequence that the t-values have a maximal peak with  $\tau=0$ . The t-values have also another peak at -1.74 s, which corresponds to the peak of the triangle wave. However it does not exceed the significance level, that is, it causes false negative error.

These algorithms were implemented in MATLAB 2006a and run on Windows XP computer (CPU: Intel Core2 Extreme Q6850 3 GHz, RAM: 3.25 GB). The computation time is about

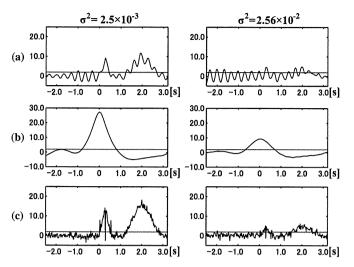


Fig. 3. Temporal transition of t-values for simulated data with different values of the variance of the prediction error (a), correlation coefficient with time lags (b), and innovations (c). The horizontal lime in each figure corresponds to the significance level of v = 0.05.

30 minutes for innovation approach and about 10 minutes for cross correlation analysis with actual imaging data, except for the process for graphical representation.

#### III. DATA ACQUISITION

We selected the same imaging data set from 2 day and 0 day old rats (corresponding to data1 and data2 respectively in this study) that was used in the study of developmental aspects of the respiratory neuronal activation in the rat brainstem [2] in order to evaluate our method by comparing its outputs with those of the time-lagged cross correlation analysis. Additionally, we analyzed the imaging data set from the rabbit cardiac sino-atrial node (SAN) as an example of the application of our method to other types of preparations (data3). These data were taken from the article that reported inhomogeneous action potential characteristics as a cause of pacemaker shift in the SAN [5].

The recording chamber was mounted on a fluorescence macro zoom microscope (MVX-10, Olympus Optical, Tokyo, Japan). Preparations stained with a voltage-sensitive dye were illuminated with a tungsten-halogen lamp (150 W) through a band-pass excitation filter ( $\lambda = 480$ –550 nm). Epifluorescence through a long-pass barrier filter ( $\lambda > 590$  nm) was detected with a CMOS sensor array (MiCAM Ultima L-camera, Brain-Vision;  $100~\mu m \times 100~\mu m$  pixel size,  $100 \times 100$  pixel array). Optical signals were sampled at 50 Hz (20 ms/frame) for data1 and data2, 500 Hz (2 ms/frame) for data3.

Analog signals of raw and integrated C4VR activities were recorded at 1 kHz for data1 and data2. The analog signal of electrical field potential of the SAN was recorded at 10 kHz for data3 with a pair of fine metal electrodes placed on both edges of the preparation. These analog signals were amplified and digitized, then stored in a hard disk together with optical signals. Analog signals were window-discriminated to yield transistor-transistor logic (TTL) pulses and used to trigger the optical recording system. Total number of recorded time frames were 1024/256/1024, the recording was started at 768/64/768 frames before the trigger signal, and repeated 30/34/71 times

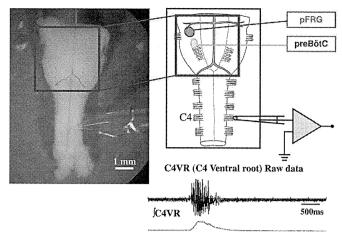


Fig. 4. (a) Ventral brainstem area for optical imaging (surrounded by the red square). (b) Schematic representation of anatomical structure of the brainstem and the recorded area. (c) Raw output signal from C4VR. (d) Integrated C4VR output signal.

for data1/data2/data3, respectively. Among these repetitions, 29 and 27 repetitions, which were contaminated with relatively small artifacts, were selected for data1 and data2, respectively. In the case of data3, all repetitions had high enough quality, because SAN generated signals with high S/N ratio resulted from its highly synchronized activation. In order to set similar numbers of repetitions for all data sets, 30 repetitions were selected among 71 repetitions for a fair comparison with data1 and data2.

The change in fluorescence intensity  $(\Delta F)$  relative to the initial intensity of the fluorescence  $(F_0)$  in each pixel was calculated. To normalize the difference in the amount of membrane-bound dye and illumination within the preparation, background fluorescence intensity at each pixel was divided by the maximum background fluorescence, and then the ratio of  $\Delta F$  to the normalized background fluorescence intensity (F), i.e., the fractional change in fluorescence intensity  $(\Delta F/F)$ , was calculated at each pixel in each frame. If F was less than 0.25, then  $\Delta F/F$  was set to be zero [2]–[5]. Then the linear trend of imaging data associated with photobleaching was eliminated and z-transformed.

Fig. 4 shows the recorded area in the brainstem, which contains two putative rhythm generators reported as the para-facial respiratory group (pFRG) [12] and the pre-Bötzinger complex (preBötC) [13]. Inspiratory-related respiratory activity was monitored from the C4VR with a suction electrode. The raw nerve signal was amplified, band-pass filtered from 15 Hz to 3 kHz, full-wave rectified, and integrated with a decay time constant of 100 ms. This integrated signal was used as the reference function for the cross correlation analysis.

#### IV. RESULTS

Background stationary oscillations were identified by a NNAR model on the period sufficiently before or after the respiration onset. In this study four neighboring pixels, which contact with edge of a pixel of interest were employed for the NNAR model for saving the computational cost. The parameters in the NNAR model were estimated using the least square method. Then the rest part of the data was filtered through the