

指と触知ピンが接触、つまりピンは常に負荷を受けながら振動する状態を設定した。この際、ピンの刺激が知覚できる程度に触知盤に指を押し付けた。(3) 駆動

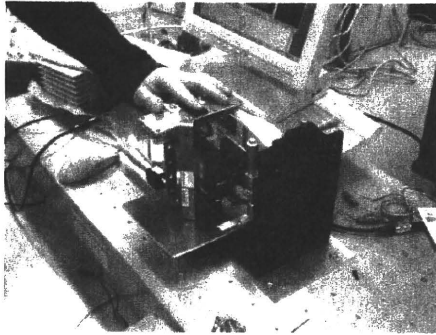


図 7 計測装置  
Fig. 7 Measurement apparatus.

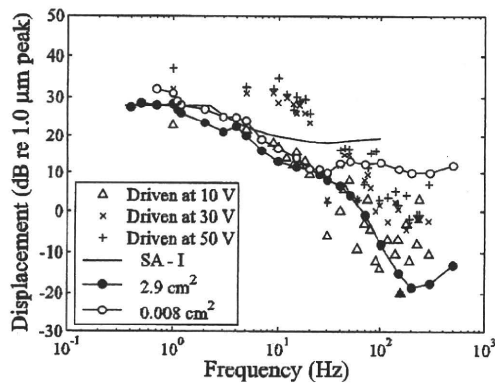


図 8 SA-I と触知ピンの周波数応答  
Fig. 8 Frequency response of SA-I and tactile pin.

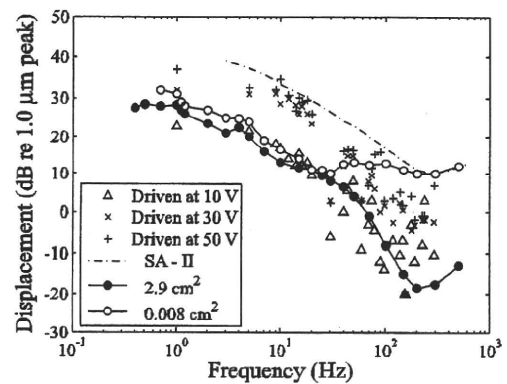


図 9 SA-II と触知ピンの周波数応答  
Fig. 9 Frequency response of SA-II and tactile pin.

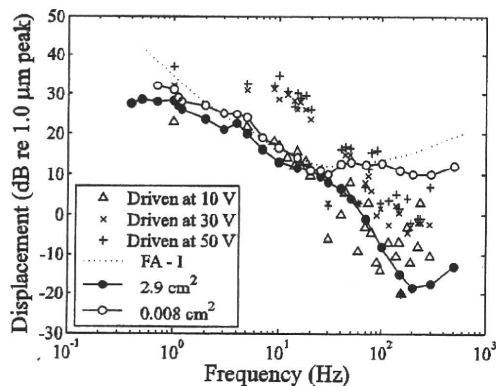


図 10 FA-I と触知ピンの周波数応答  
Fig. 10 Frequency response of FA-I and tactile pin.

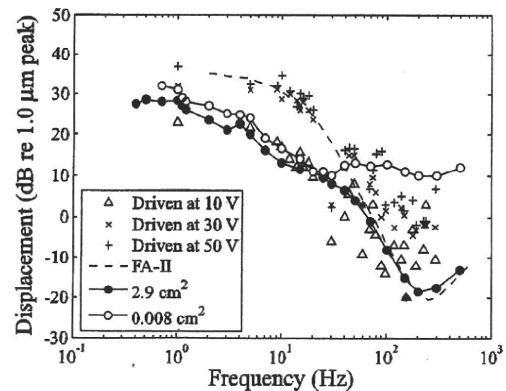


図 11 FA-II と触知ピンの周波数応答  
Fig. 11 Frequency response of FA-II and tactile pin.

周波数、(4) ピンの変位が定常状態に落ち着くまでの過渡期の影響の除去、(5) データの解析方法は 4.1 に準じる。(6) なお、計測は任意に選択した 5 本の触知ピンに対して行い、5 回繰り返し再現性を確認した。

## 5.2 結果と考察

実験で得られた触知ピンの変位データを  $1.0 \mu\text{m}$  ピークの振幅を基準に dB 表示したものと、四つの機械受容ユニットの振動検出しきい曲線との対比を、図 8～図 11 に示す。前掲の Gescheider らによる振動検出しきい曲線も併せて記載する。

本研究の第一の目的であるオプタコン-II の機械特性の明示について、振動数対変位の関係に注目すると、実験を行ったすべての駆動電圧 10 V ( $\Delta$ ), 30 V ( $\times$ ), 50 V ( $+$ ) において、振動数が高くなるにつれて変位は減少し、全周波数帯域での変位の底は駆動周波数 150 Hz となった。これらの結果は Bliss らの計

測結果と異なる。駆動電圧対変位について、駆動電圧を 10 V, 30 V, 50 V と変化させたとき各駆動周波数での変位は比例関係になく、圧電アクチュエータは駆動電圧と変位が比例するとした既知の事実と異なる。原因としてピンは指との接触で応力を受けた状態で振動していることが考えられる。接触応力が変位に及ぼす影響は図 6 下部計測（非接触状態）の周波数特性と図 8～図 11（接触状態）の 30 V の周波数特性が異なることにも現れており、接触状態では非接触状態と比較して全周波数範囲で変位が減少し、高周波数帯で変位の減衰が顕著となる。減衰は皮膚の粘弾性特性の影響であると考えられる。

次に、各駆動周波数における触知ピンの変位と振動検出しきい曲線との対比から触知に關与する機械受容ユニットの特定を行う。仮に図 8～図 11 のような特性を備えたヒトを想定した場合、振動検出しきい曲線より下にある刺激は、対応する機械受容ユニットを介して感知されることはない。図 8 と図 10 から、SA-I と FA-I に対しては、駆動電圧が 30 V 以上であれば 20 Hz 以下の帯域でしきい値以上の振動刺激を与えられることが分かる。図 9 から、SA-II に対しては、全周波数帯域でしきい曲線以上の振動刺激は与えられない。図 11 によれば、FA-II に対しては、120 Hz 以上の駆動周波数であれば印加電圧に関係なく、ほぼ受容されるはずであるが、触知ピンの面積は  $0.0007 \text{ cm}^2$ （図 12）である。これは Gescheider らが例示する接触子面積  $0.008 \text{ cm}^2$  より 1 けた小さいため、対応するしきい曲線は  $0.008 \text{ cm}^2$  のそれより下がることはないと予想できる。いわゆる、FA-II 固有の空間的加重の効果であり、これを踏まえると 120 Hz 以上で  $0.008 \text{ cm}^2$

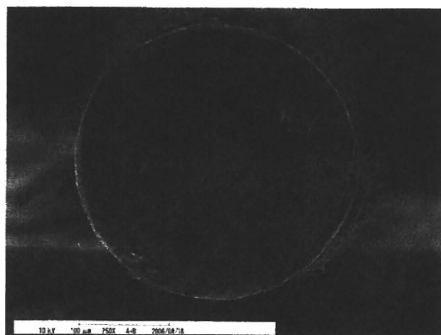


図 12 電子顕微鏡による触知ピン先端形状の撮像  
Fig. 12 Picturization of the tip form of the tactile pin by an electron microscope.

のしきい曲線を超える変位はない。低及び中周波数帯域で、FA-II のしきい曲線近傍に変位がプロットされているが、それが平均値であること、その帯域では他の受容器が優勢であることを考慮すると、FA-II の関与は極めて低いと推測される。

## 6. 指接触下での触知ピン変位計測（間欠刺激）

オプタコン-II で文字を提示する場合、右利きのユーザは左手の示指を触知ピンアレーに乗せ、右手でスキャナを持つ。継続して文字をスキャンする過程で、任意の 1 ピンに注目すると、on と off とが不連続、かつランダムに生成されることになる。このとき指は振動・静止状態の間欠的な刺激を受けており、実際の使用条件ではほとんどがこの刺激であると考えられる。間欠刺激の例として、今、格子状に並べられた触知ピンアレーを 7 行 5 列に単純化してアルファベットの“A”を提示する触知ピンの挙動を考えてみる（図 13）。触覚提示装置の第 3 行 5 列目のピンの挙動に注目すると、このピンは“A”が図の (2)、及び (4) のように撮像されたときに振動する。本実験では触知ピンと指が接触した状況下において、振動・静止状態を間欠的に繰り返す触知ピンの変位を調べた。

### 6.1 実験条件

実験条件として、(1) 駆動電圧を 30 V とし、(2) 指と触知ピンは接触状態とした。この際、ピンの刺激が知覚できる程度に指を触知盤に押し付けた。(3) 駆動周波数は 230 Hz で、(4) 実験開始時からデータを収集し、(5) 掲載データのドリフトは除去した。(6) 計測回数は 5 回行い再現性を確認した。

### 6.2 結果と考察

図 14 に 0.4 s を 1 周期とした間欠刺激信号を送信したときのピンの変位を示す。初期状態から on 期間の開始とともに  $33 \mu\text{m}$  (30 dB) の変位を生じ、その状態から 230 Hz で振動状態となった。ただしその変位は小さく約  $0.8 \mu\text{m}$  (-2 dB) であった。また、off 期

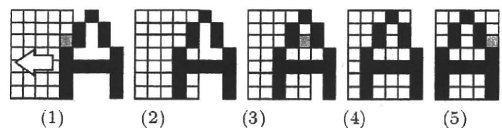


図 13 アルファベット“A”を提示する場合の各ピンの状態  
Fig. 13 State of each pin showing alphabet “A”.

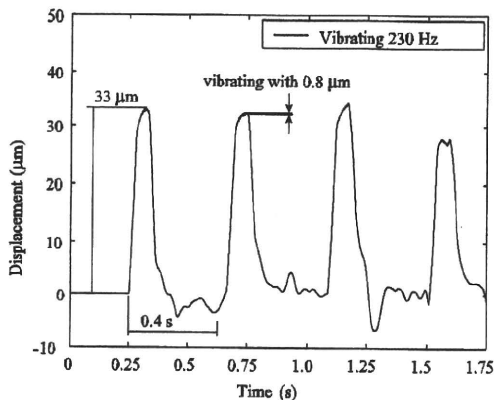


図 14 指接触下での触知ピンの変位計測 (間欠刺激)  
Fig. 14 Displacement measurement of the tactile pin in a finger contact state (intermittent stimulus).

間の開始とともに変位は初期位置に戻った。実験条件から、指は 0.4 s 周期で約 33  $\mu\text{m}$  変位させられる。単位を変換すると、2.5 Hz の振動数で約 30 dB の変位を受ける。これを図 1 に当てはめると、SA-I と FA-I だけが機能する周波数帯、及び変位となり SA-II や FA-II の関与は抑制されている。すなわち、オプタコン-II は空間分解能に優れた SA-I によって提示された形を知覚させることになり、このことは従来の触覚研究の知見とも合致するものである。

## 7. 総 括

オプタコン-II は 230 Hz の高周波数で固定されて駆動されており、かつその変位も微小なものであるとの認識により、FA-II の振動検出チャンネルを用いてユーザに情報を伝達すると漠然と考えられていた。しかしながら、オプタコン-II の触知ピンの接触面積、変位、駆動周波数ではヒトの振動検出チャンネルを刺激できないことが分かった。また、間欠刺激の実験から、オプタコン-II は間欠的に低周波数で出現する触覚的な情報に関して、形を SA-I に与え、低周波数で感度の高い FA-I で形の動きを与えていると考えられる。

実際のオプタコン-II での触読を想定すると、右手で持つスキャナを自らが動かすことにより触読のきっかけを自らが作っており、同時にその動かしている感覚を強調するように、FA-I が触知盤上の形の動きを検出し、提示パターンが変化していることを知覚する。提示パターンが動いているか否かを理解しながら、空間分解能に優れた SA-I で形認識を行い触読を容易に

していると考えられる。加えて、Johnson らが指摘しているように SA-I には形状認識に選択的な感受性が備わっており、エッジやカーブなどの形状認識では一定の背景上に浮彫り様の SA-I 神経イメージを作り出す。オプタコン-II の触知ピン変位調節機構は、こうした SA-I イメージの作成を容易にする。

スキャナの自由な移動速度とユーザに個別に異なる刺激強度の調節が容易に行えるシステム構成であることが、オプタコン-II で触読ができるメカニズムであり、当時視覚障害者の読書支援機器とされた理由であると考えられる。

## 8. む す び

本研究では、感覚代行器としての実績があり、心理物理実験での刺激提示装置として用いられるオプタコン-II の基本特性に注目して検討を行った。レーザ変位計を用いることで、微小である触知ピンの変位を計測し、ヒトの触覚特性との比較からオプタコンの基本特性の評価を行った。このとき、触知ピンが指に加える変位を計測するために、触知ピンの下部から変位を計測する実験装置を構築し、接触しているがゆえに変位している触知ピンの頂点が計測できないとした問題を解消し、計測を可能とした。下部計測では上部計測と同等の計測が行えることを定量的に示し、指と触知ピンが接触している状況下での変位の計測データから 4 チャンネルモデルと対応させ、オプタコン-II が刺激する機械受容ユニットの特定を行った。また、触知ピンの間欠的な挙動に注目し、計測・検討を行うことで、現在まで曖昧にされてきたオプタコン-II を用いて触読ができる根拠を与えた。本研究の知見は神経生理学の分野で触覚提示装置として広く用いられているオプタコン-II の機械的な基礎資料を与える。

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## 付 録

ここでは、6.の実験で用いた実験条件の妥当性を示す。6.では実験条件として間欠刺激を0.4s周期とした。今、オプタコン-IIの触知ピンが間欠刺激0.4s周期で形状呈示しており、ユーザが1回の形状呈示で形を認識できるとすれば毎秒2.5文字、つまり毎分150文字触読できる。Blissの定義に従い1単語をアルファベット平均5文字とすれば毎分30単語触読できることになる。更にBlissの実験結果を引用すると被験者3名のうち1名が17時間、2名が50時間のトレーニングの後、毎分30単語触読可能であったと報告されている。オプタコン-IIを用いた触読で毎分30単語触読する状況は存在しており、本実験で設定した間欠刺激条件は妥当であると考えられる。

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## Development of High Speed and High Sensitivity Slip Sensor

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**Abstract**—Slip detecting tactile sensors is essential to achieving a human-like gripping motion with a robot hand. Up until now, we have developed flexible, thin and lightweight center of pressure (CoP) sensor. The sensor, constructed of pressure conductive rubber sandwiched between two sheets of conductive film, is able to detect the center position of the load distribution and the total load. Recently, detection of initial slip has been shown to be possible. However the detection principles are unclear. Therefore, we carried out verification experiments of the slip detection properties of the CoP sensor and the detection principle. In the results, we found a change in electrical conductivity produced with a shear deformation of the pressure conductive rubber. In this paper, we will discuss the slip detection properties of the CoP sensor and detection principle.

### I. INTRODUCTION

With the aim of achieving a human-like robot hand, or one that is superior to the human hand, much research has been carried out [1][2][3]. Even with eyes closed, humans can grip with minimum force an object with unknowns such as weight and coefficient of friction, etc. We are also able to perform smoothly such motions as handing the object off or setting it down. To achieve these motions with a robot hand requires tactile sensors having slip sense in addition to contact position and load.

Johansson et al. [4][5], in their research regarding the gripping motion of humans, made clear that humans grip objects at the minimum gripping force that is close to producing slip. It was also shown that the initial slip between the skin and the gripping object was essential to this sense. Therefore, up until now various slip sensors detecting initial slip have been proposed. Trembley et al. [6] developed a sensor, arranging acceleration sensors in sets of two inside a spherical silicon rubber with a projection called a “nib”, that detected the vibrations which occur on the surface of the sensor as a result of initial slip. Son et al. [7] developed a sensor with four sheets of PVDF film arranged in a semi-circular silicon rubber tube that similarly detected the vibrations occurring from initial slip. Adding to the findings of Johansson et al., Maeno et al. [8] modelled the structure of the finger pad by means of finite element analysis and made clear the properties of individual tactile receptors. They then imitated the human gripping technique, developing sensors lined up inside a curved elastic surface at regular intervals along a strain gauge [9]. With this, they showed that it was possible to grip an object of unknown weight and

coefficient of friction. Shinoda et al. [11] proposed a slip sensor using Acoustic Resonant Tensor Cell (ARTC). The ARTC is composed of a resonance cavity within the elastic body and ultrasonic receiving probe; the slip direction stress is detected from changes in the ultrasonic wave resonance frequency. Ikeda et al. [12] observed the contact surface between an elastic body and a rigid plate by utilizing a camera, and proposed a technique for estimating slip margin.

As shown above, much research has been conducted regarding slip sensors. However, as yet, a practical slip sensor does not exist. This is thought to be for the following causes. Firstly, there is the problem of reduction in size and weight. The space where sensors can be located for most robot hands is limited from the point of view of mechanism function. Accordingly, structures with devices embedded inside the fingers and thick sensors are undesirable. Secondly, there is the problem of wiring. When sensors using strain gauges or PVDF films are configured over a large area, it is necessary to increase the number of sensing elements and wires. However, excessive wiring becomes a burden on the hand. Finally, there is the problem of response. Especially when cameras are used, response is dependent on the processing time of the data. Since a delay in response time increases the slip displacement of the object, high-speed response is desirable.

Therefore, in this research, our goal is to develop thin, lightweight slip sensors with high-speed response that could be installed on existing robot hands. Until now, we have carried out the research and development of “The Center of Pressure (CoP) tactile sensor” for detecting two-dimensional load distribution with the following properties [13].

- 1) Flexible, thin(approximately 0.7 mm), lightweight(approximately 0.2 g/cm<sup>2</sup>)
- 2) Wire saving(4wires)
- 3) High speed responsibility(1ms)

The CoP sensor can detect the center of the load distribution and the total load added to a surface. In recent experiments, it was found that these could be utilized as sensor to detect the initial slip as well [14]. By using this sensor, we succeeded in holding the glass whose weight changes (as shown in Fig.1). However, the detailed detection mechanism is unclear. In this paper, we will simply mention the slip detection experiment using the CoP sensor, and report on the slip detection properties and mechanism.

### II. CoP TACTILE SENSOR

#### A. Pressure Sensitive Conductive Rubber

Pressure conductive rubber (product of Inaba Rubber Co., Ltd.) has the function of converting pressure into electrical

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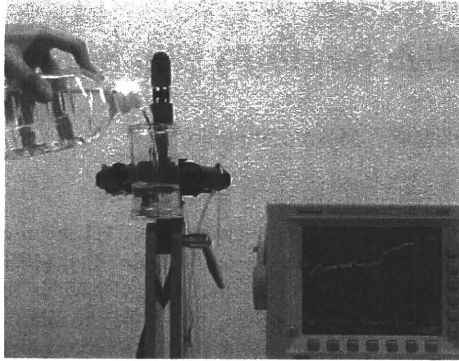


Fig. 1. Grasping force control for the object whose weight change (pouring water into a cup)

resistance. It is a high polymer material primarily composed of silicon rubber, and conductive carbon particles are uniformly distributed. An increase in the pressure causes a decrease in volume, and the carbon particles contact each other forming conduction routes. In other words, due to the deformation of the rubber caused by increasing pressure, there is a change in the distribution of carbon particles inside the rubber. The fluctuation in the number of conduction routes due to the carbon contacts appears as a change in electrical resistance.

#### B. Structure, Theory, and Properties

As shown in Fig. 2, the structure of the CoP sensor is that pressure conductive rubber sandwiched between upper and lower layers of conductive film. At the edges of both layers of conductive film are electrodes ( $S_1, S_2, S_3, S_4$ ). The center position of the load distribution is measured by the center position of the current distribution obtained from the potential difference across the electrodes ( $S_1-S_3, S_2-S_4$ ). The load output is measured by the total electric current flowing to upper and lower layers. Structurally, the CoP sensor is flexible, thin, and lightweight, and may be arranged on a cylindrical surface (Fig. 2, lower-left). The number of wires is four, which is not dependent on the area of the sensor. Moreover, the filter circuit is not used because this sensor is strong in the high frequency noise in practical level like force-feedback control. This sensor has a high-speed response of less than 1 (ms) because the circuit is only an analogue arithmetic circuit. Therefore, this sensor is suitable for the control system of a robot hands.

### III. SLIP DETECTION EXPERIMENT WITH THE CoP SENSOR

In this experiment, we show that the CoP sensor can detect the initial slip. So, we compared the CoP sensor load output with the gripping force measured by a load cell. The experimental apparatus utilized in this experiment is shown in Fig. 3. The CoP sensors were arranged around two cylinders (diameter 18 mm), and fixed face-to-face using a special purpose jig. The height and tilt of the CoP sensors were regulated by a left  $\theta$ -stage and a right XYZ-stage. As

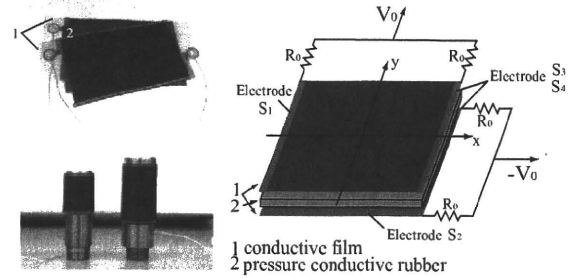


Fig. 2. Structure of the CoP sensor

in the figure, the plastic cylinder (18 mm) was sandwiched by the CoP sensors (Fig. 3-(1)), and this was connected by wire to the tension side load cell (we call "Load cell(Z)" below). Load cell(X) in Fig. 3 denotes the normal vector force (gripping force) and Load cell(Z) denotes the tangential force (tensile force). The gripping force was adjusted to 2 N while seeing Load cell (X) output. When the automatic Z-stage was activated, the gripping object was made to slip downward vertically (Fig. 3-(2)). Since it was possible to regulate the speed of the automatic Z-stage from 1  $\mu\text{m/s}$  to 100 mm/s, we can control the slip velocity of the plastic cylinder. The velocity for this experiment was set at 100 mm/s. The slip displacement of the plastic cylinder was measured by a laser displacement sensor (resolution: 0.1mm).

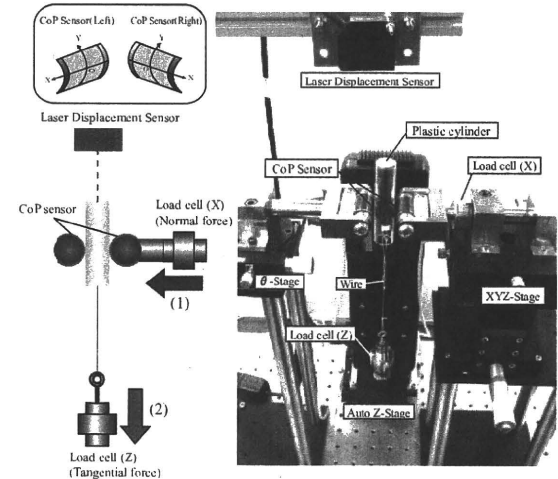


Fig. 3. Experimental apparatus for slip detection using the CoP sensor

#### A. Experimental Results

The results of this experiment are shown in Fig. 4. The graphs show, from top to bottom, (a) the CoP sensor load output, (b) the CoP sensor position output, and (c) two load cells and laser displacement sensor output. As the left and

right CoP sensor position output was the same, only the right side position output of the CoP sensor is shown. From the laser displacement sensor output, the slip displacement occurs from the time of the vertical line shown on the graph.

We compared the CoP sensor load output with the grip force according to Load cell (X). Looking at the grip force, its change was approximately  $0.2\text{ N}$  and increasing just before the occurrence of slip displacement. Slip displacement occurs when a initial slip changed to a global slip. At this point, we can consider the gripping object and sensor surface to be detached for an instant, and that the load in the normal vector direction increased. Meanwhile, looking at the CoP sensor load output, there is a large decrease just before the occurrence of the slip displacement. The right side CoP sensor output decreased by approximately  $4\text{ V}$ . According to the sensor load output characteristics, a decrease of approximately  $1\text{ N}$  was produced. There was a decrease of approximately  $1.3\text{ N}$  at the left side CoP sensor. We can say that the change is not one-sided because there was a simultaneous decrease in left and right outputs. In spite of the increase in the grip force, the CoP sensor's load output of both sides decrease before slip displacement occurs. So, using these changes, it is possible to detect the start of slip (referred to as "initial slip").

Meanwhile, the change in the CoP sensor's position output (Fig. 4-(b)) was extremely small, only about  $0.05\text{ V}$  circumferentially against  $\pm 4\text{ V}$  full scale. This may be considered the change between stick area and slip area produced when the gripping object slips along the sensor surface [10]. This small change was due to the small contact area as a result of cylinder-to-cylinder contact. So, we install a silicon rubber on the CoP sensor surface, and increasing the contact area. Consequently, we were able to increase the change of the CoP sensor's position output two or four times. It is possible to detect the slip direction using the position output change because this change is only produced in the slip direction (circumferential direction in this case).

#### B. Discussion

The above results show that the CoP sensor can detect the initial slip and the slip direction. We expect that the change of the CoP sensor's load output (Which we call "slip output" below) is produced by the following phenomena. Looking at the colored area of Fig. 4-(a) and (c), the CoP sensor's load output begins to decrease at the same instant, and we find that the tangential force (Load cell(Z) output) also begins to increase. From this, we can expect that a shear deformation of pressure conductive rubber occur by the tangential force. On the other hand, the change of the CoP sensor's load output is dependent on the electrical resistance change of the pressure conductive rubber. This indicates that there is some relationship between the shear deformation of the pressure conductive rubber and the change of electrical resistance. So, we conducted an experiment to observe the change of electrical resistance when pressure conductive rubber undergoes a shear deformation.

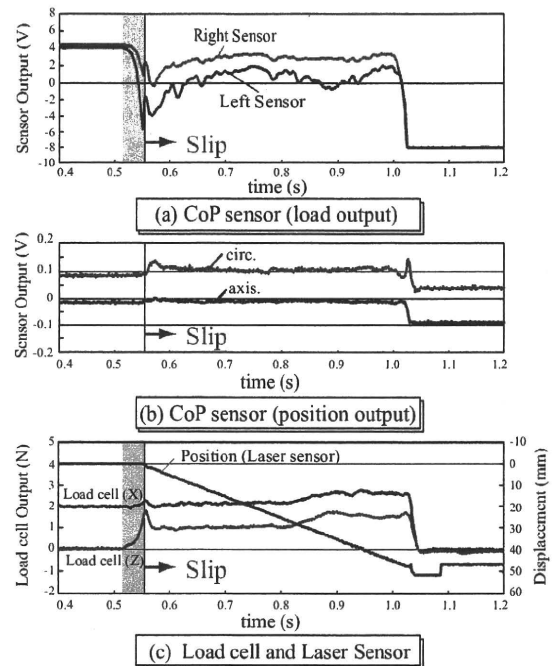


Fig. 4. Result of Slip detection experiment

### IV. PRESSURE SENSITIVE CONDUCTIVE RUBBER SHEAR DEFORMATION EXPERIMENT

#### A. Experimental Method

In this experiment, we reveal why CoP sensor's output change when an object slips on the CoP sensor. So, we inserted pressure conductive rubber electrodes, and measured the voltage between electrodes when it was made to undergo a shear deformation. The experimental apparatus is shown in Fig. 5. The electrodes (gold plated) were attached to acrylic plates, which were aligned facing each other (the circled area of Fig. 5). In the experiment, the electrodes were connected to a regulated power supply through a resistance of  $1\text{ k}\Omega$ , and a voltage of  $5\text{ V}$  was applied.

The X-stage installed on the right side of the experimental apparatus was activated, and the pressure conductive rubber ( $7\text{ mm}^2$ ) was sandwiched between the electrodes (Fig. 5-(1)). This X-stage was equipped with a dedicated actuator, with a travel speed of  $0.1\text{ mm/s}$  and a positioning accuracy of  $0.017\text{ mm}$ . Therefore, the quantity of the normal direction deformation of the pressure conductive rubber could be finely controlled. The X-stage was activated again, and the normal direction load was increased. At this time, the voltage between electrodes was decreased from  $5\text{ V}$  (load cell output :  $0\text{ N}$ ) to  $2\text{ V}$  (load cell output : approximately  $1.7\text{ N}$ ). From now on, this voltage is referred to as initial voltage ( $V_i$ ).

Next, the automatic stage installed on the left side was activated producing a shear deformation of pressure conductive rubber (Fig. 5-(2)). The automatic stage had a positioning

accuracy of  $0.012\text{ mm}$  and its speed could be adjusted from  $1\text{ }\mu\text{m/s}$  to  $100\text{ mm/s}$ . The quantity of the shear deformation of the pressure conductive rubber could be measured by the laser displacement sensor (resolution  $0.1\text{ }\mu\text{m}$ ). In this experiment, the shear deformation of the pressure conductive rubber was set to  $0.3\text{ mm}$ , and the three deformation speeds was set such as  $0.05\text{ mm/s}$ ,  $0.1\text{ mm/s}$ , and  $1\text{ mm/s}$ . The voltage between electrodes and the laser displacement sensor output were measured.

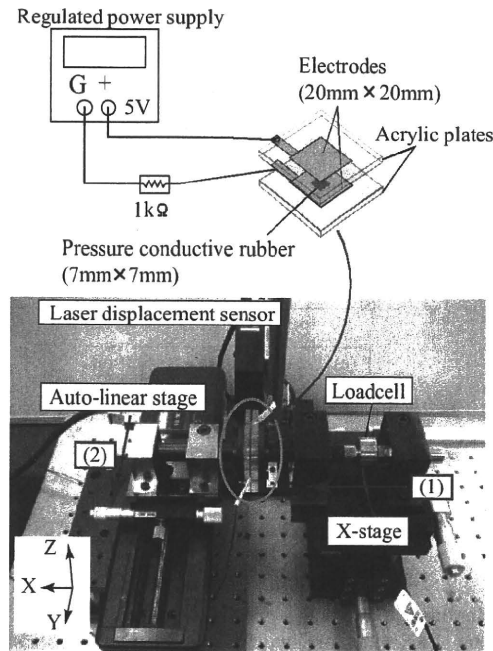


Fig. 5. Experimental system for deformation of pressure conductive rubber

### B. Experimental Results

The results of the experiment are shown in Fig. 6, Fig. 7 and Fig. 8. Time (s) is along the horizontal axis and the voltage between electrodes and laser displacement sensor output (mm) are along the vertical axis. At all deformation speed, the voltage increased, when the shear deformation of the pressure conductive rubber was occurred by the Auto-linear stage. Taking the rise of the voltage at this point as  $\Delta V$ , a summary of the voltage difference  $\Delta V$  is shown in Table I. Moreover, the voltage remained constant during shear deformation of the rubber. When the shear deformation stopped, the voltage gradually decreased and converge to about  $3\text{ V}$ .

TABLE I  
CHANGE OF VOLTAGE BETWEEN ELECTRODES

Shear deformation speed(mm/s)	$\Delta V(V)$
0.05	1.4
0.1	1.6
1	2.1

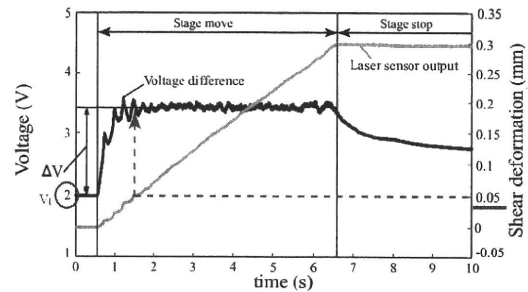


Fig. 6. The voltage difference between electrodes, shear deformation speed :  $0.05\text{ mm/s}$

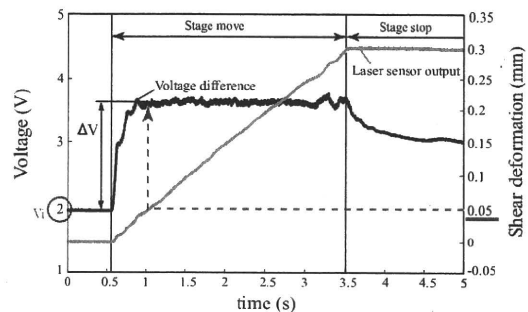


Fig. 7. The voltage difference between electrodes, shear deformation speed :  $0.1\text{ mm/s}$

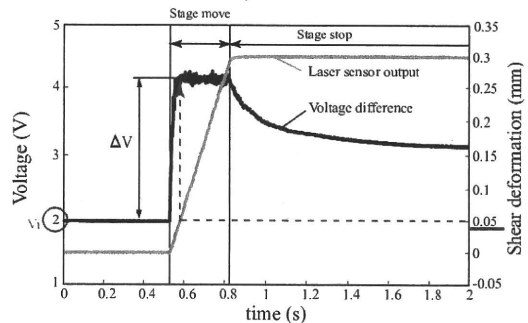


Fig. 8. The voltage difference between electrodes, shear deformation speed :  $1\text{ mm/s}$

### C. Discussion

1) *Change in Electrical Resistance of Rubber:* There was a large rise in the voltage between electrodes at the time of the shear deformation of the pressure conductive rubber. The rise of voltage indicated an increase in the electrical resistance of the rubber. As in the above hypothesis, we found that a change of electrical resistance was produced when a shear deformation of the rubber occurred. This fact was designated as a decrease in the load output of the CoP sensor. Looking at the results of the  $0.05\text{ mm/s}$  trial, the voltage difference  $\Delta V$  raised more than  $1\text{ V}$  with a shear deformation of only  $0.05\text{ mm}$ . This time, there was a large increase in the electrical resistance of the pressure conductive rubber. This was the same in the  $0.1\text{ mm/s}$  and  $1\text{ mm/s}$  trials. This agrees with the large decrease of the CoP sensor load output that occurred before the change

in the laser displacement sensor output utilized in section III. Therefore, it is clear that the slip output of the CoP sensor was generated by the change in electrical resistance of the pressure conductive rubber at the time of its shear deformation.

The rise in the electrical resistance of the pressure conductive rubber can be considered to be due to the following reasons. The pressure conductive rubber was a high polymer material primarily composed of silicon rubber with carbon particles uniformly distributed within. In an unloaded condition, the carbon particles were separated from each other as in Fig. 9-(a), so even if a voltage was applied, electric current would not flow. However, when the pressure was increased, the distribution of the carbon particles inside the rubber changed, and the carbon particles contacted each other as in Fig. 9-(b) forming a conduction route. As mentioned in section II-A, when there is an increase in conduction routes due to contact of carbon particles in pressure conductive rubber, this appears as a change in electrical resistance. Therefore, if we add a shear deformation to pressure conductive rubber as in Fig. 9-(c), the conduction routes fragment, and the number of conduction routes decreases. This situation shows the electrical resistance to increase. When the deformation stops, as in Fig. 9-(d), the conduction routes inside the rubber are restored. So, the electrical resistance seems to gradually decrease. In this experiment, the voltage converge to about 3V (as shown in Fig.6, Fig.7, Fig.8). But the voltage differences don't reach the same final value completely and it takes about 5 seconds to reach the stable value. The cause is regarded as an influence of hysteric of pressure conductive rubber.

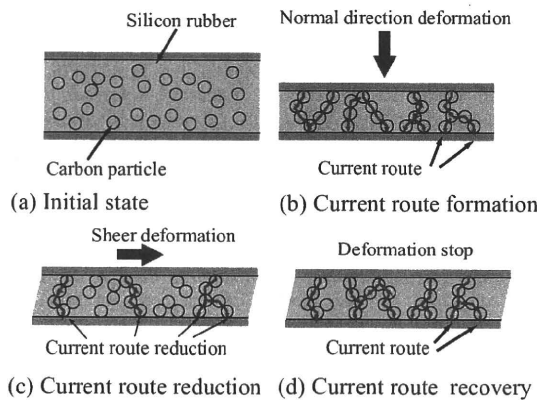


Fig. 9. Structure of Pressure conductive rubber

2) *Speed of Rubber Shear Deformation*: Here we shall discuss the relationship between the shear deformation speed of the pressure conductive rubber and the change of voltage between the electrodes. As shown in Table I, the size of the voltage difference  $\Delta V$  changes according to the deformation speed of the rubber. This change tends to be significant as the deformation speed becomes greater. Accordingly, the shear deformation speed was varied at appropriate intervals from  $10 \mu\text{m/s}$  to  $4000 \mu\text{m/s}$ , and the new voltage differences

were measured. The voltage differences  $\Delta V$  for each shear deformation speed plotted in a double-logarithmic graph are shown in Fig. 10. The voltage differences  $\Delta V$  for initial voltages (initial loads) measured at 3 V (load cell output: approximately 1.0 N) and 4 V (load cell output: approximately 0.5 N) were shown in the same graph. This graph showed a linear increase in voltage difference  $\Delta V$  accompanying increases in the shear deformation speed ( $v_s$ ) of the rubber. Regarding the conductive mechanism of pressure conductive rubber, the following items are to be considered. With slow shear deformation, only deviation in the conduction routes are produced and they are not fragmented. Meanwhile, with rapid deformation, conduction routes that were not fragmented with slow deformation are broken due to the sudden deformation. Therefore, the voltage difference  $\Delta V$  increased more with rapid shear deformation.

Consequently, when we measure the initial voltage ( $V_i$ ) and the voltage difference ( $\Delta V$ ), we find the shear deformation speed ( $v_s$ ) of the rubber. The numerical formula in Fig. 10 conducts power approximation for each of these results with regression equations. Table II shows a constant ( $k$ ) and an exponent ( $n$ ) of the shear deformation speed ( $v_s$ ). The line joining the three is can be represented the following formula:

$$\Delta V = k \times v_s^{0.11} \quad (1)$$

Fig.11 shows a graph with the initial voltage ( $V_i$ ) from Table II along the horizontal axis and the constant ( $k$ ) on the vertical axis. This graph is linear, so we find that the initial voltage ( $V_i$ ) and the constant ( $k$ ) are proportional. The relational expression for these is shown below.

$$k = -0.27V_i + 1.55 \quad (2)$$

From above, the shear deformation speed ( $v_s$ ) of the rubber can be expressed with the following formula.

$$v_s = \left( \frac{\Delta V}{-0.27V_i + 1.55} \right)^{-0.11} \quad (3)$$

This formula shows that if we measure the initial voltage ( $V_i$ ) when pressure conductive rubber is deformed in the normal vector direction and the change of voltage between electrodes ( $\Delta V$ ) when it is made to undergo a shear deformation, we can detect the speed of the shear deformation of the rubber.

TABLE II  
CONSTANT AND EXPONENT OF FORMULA IN FIG. 10

Initial voltage ( $V_i$ )	Constant ( $k$ )	Exponent ( $n$ )
2	0.99	0.12
3	0.75	0.11
4	0.45	0.11

## V. SUMMARY

To investigate the slip detection properties of the CoP sensor, an experiment comparing the outputs of a load cell and the CoP sensor was conducted. The results showed that the CoP sensor's load output varied with slip of the object being gripped. This change was more sensitive than a laser displacement sensor (resolution  $0.1 \text{ mm}$ ), and so it



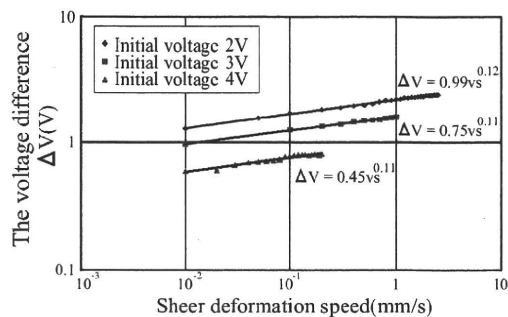


Fig. 10. Relation between the voltage difference of electrodes and shear deformation speed

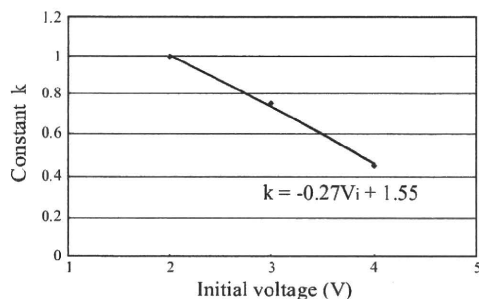


Fig. 11. Relation between constant  $k$  and initial voltage  $V_i$

could be utilized to detect the initial slip. An experiment in which pressure conductive rubber was made to undergo a shear deformation was also conducted to clarify the CoP sensor slip detection mechanism. We found that when the pressure conductive rubber underwent a shear deformation, the resistance greatly increased. It was made clear that the load output change of the CoP sensor depends on the special properties of pressure conductive rubber when an object slipped over the sensor.

It is suggested that, through this experiment, the slip sensor without the CoP sensor could be configured using pressure conductive rubber. For example, when the simplest structure of pressure conductive rubber sandwiched between two electrodes is used, as in this experiment, the object is set on the sensor, made to slip, and simultaneous with it slipping, the voltage between electrodes changes. By measuring this change, it is possible to detect slip very clearly. When pressure conductive rubber is utilized to configure a slip sensor, considering the special properties, it will have the following characteristics.

Since the pressure conductive rubber is thin, approximately 0.5 mm, and light, so even with the electrodes are attached, a thin, lightweight sensor can be configured. As there is a change in the voltage between electrodes with a shear deformation of only 0.05 mm as shown in the shear deformation experiment, it is extremely high sensitivity. The sensor has a high-speed responsibility. As shown in section IV-C.2, if the shear deformation speed of the rubber ( $V_s$ ) and the speed of slip of the object are set equal, the slip speed of the object can be detected from the voltage difference ( $\Delta V$ )

at the time of the shear deformation and the initial voltage ( $V_i$ ), as in formula (3).

Up until now, there have been many slip sensors utilizing PVDF, strain gauges, cameras, etc. These sensors are difficult to detect initial slip without special structures, signal conditioning and filtering. However, our sensor using pressure conductive rubber can detect initial slip easily and clearly. So, we will conduct more detailed experimental analysis regarding the properties of pressure conductive rubber, and apply it to slip sensors.

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# A Net-Structure Tactile Sensor Covering Freeform Surface with Reduced Wiring

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**Abstract**—A tactile sensor is developed with the aim of covering a robot's entire structure, while reducing wiring requirement and ensuring high-speed response. There are only 4 signal wires from the sensor. The sensor response time is nearly constant (within 1ms) regardless of the number of detection elements, their placements or sensor areas. In this paper, the principles behind the operation of this sensor and the results of experiments using the sensor are described.

## I. INTRODUCTION

In recent years, research efforts to develop robots with tactile perception in order to achieve better safety in humans/robot shared environments and to enable effective communication with humans have been progressing[1]-[12]. However, many of these researches encountered some problems requiring resolution, such as those described below.

- 1) Covering free-form surfaces: Most robot bodies have freeform surfaces, making it hard to attach sensors.
- 2) Excessive wiring: A lot of wires are required in attaching multiple detection elements to a robot.

In this study, a net-structure tactile sensor attachable to freeform surfaces and with reduced wiring requirement was developed. The sensor features high response speeds without requiring software processing, is formed into a structure resembling a net, can be attached to freeform surfaces, and can detect the center of the load distribution as well as the overall load on 2-dimensional surfaces.

Fig.1 shows the conceptual schematic diagram of the sensor. There are only 4 signals from the sensor and Internal connection is required only between adjacent detection elements. Since the structure is like that of a net, the system of sensors can cover 3-dimensional freeform surfaces. Sensor response speed is almost unaffected by the number, placement, or sensor surface area of the detection elements. In summary, the sensor features the following:

- 1) Covering freeform surfaces: the sensor can be laid out like a net to cover freeform surfaces
- 2) Reduced wiring: Lines from the sensor consist of 4 wires only regardless of number, surface area, or placement of detection elements
- 3) High-speed response: response time is less than 1 ms regardless of number of detection elements. This means that the sensor is adequate for use in control

loops around 1khz, which is the standard used in robotics control

## II. SENSOR STRUCTURE

Sensor structure is shown in Fig. 2. The sensor is composed of tactile elements laid out on a matrix format. Each tactile element has one pressure-sensitive material  $r_p$  and four resistors  $r$ , as shown in the figure. The electrical resistance of the pressure-sensitive material decreases when load is applied to it. The sensor connects the tactile elements in an  $m \times n$  matrix, and the electrical boundary conditions are imposed at the edge of the resistance network for an upper (layer A) and a lower (layer B), as shown in the figure. Sensor output is the voltage coming from the 4 electrodes  $E_1, E_2, E_3$  and  $E_4$ .

## III. PRINCIPLE OF THE SENSOR

The principle governing the sensor is the same as that for the sensor which we have developed and reported previously[14][15]. In this study, we extended the principle of the previous sensor to apply on discrete analog-network structures. When distributed load is applied to the sensor, the resistance  $r_p$  of the tactile element will change accordingly and the current  $I(i, j)$  which flowing through resistance  $r_p$  will change. Thus, the current distribution in the sensor follows the load distribution. The sensor detects the center position of the current distribution as well as the total current flowing through.

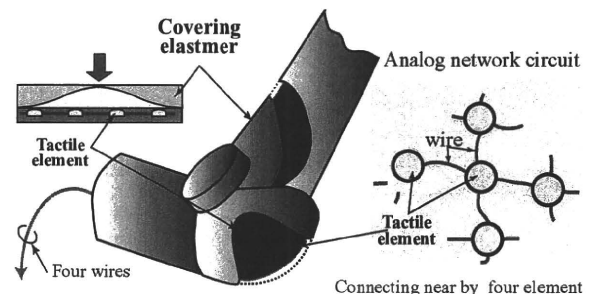


Fig. 1. Conceptual diagram of net structure tactile sensor

### A. Equivalent circuit and basic equation

The equivalent circuit near the tactile element  $(i, j)$  is shown in Fig. 3. The current flowing from layer A into layer B through  $r_p$  is set to  $I(i, j)$ . The voltage  $V_a(i, j)$  and  $V_b(i, j)$  is impressed on the layer A and B respectively. Let us consider layer A. Referring to the equivalent circuit, Eq. (1) is derived from Kirchhoff's current laws as follows;

$$\nabla^2 V_a(i, j) = rI(i, j) \quad (1)$$

where  $\nabla^2$  is the laplacian operator as shown in Eq. (2).

$$\begin{aligned} \nabla^2 V_a(i, j) &= V_a(i-1, j) + V_a(i+1, j) \\ &+ V_a(i, j-1) + V_a(i, j+1) - 4V_a(i, j) \end{aligned} \quad (2)$$

An equation similar to Eq. (1) is obtained for layer B using the same method described above.

$$\nabla^2 V_b(i, j) = -rI(i, j) \quad (3)$$

### B. Tactile element position coordinates

The position  $x_{i,j}$  of each element along the  $x$  direction is defined. This  $x_{i,j}$  is a function of  $j$  only and is taken as an arithmetic series in the direction of  $j$ .  $x_{i,j}$  is determined from Eq. (4) defining the origin which falls at the center of the sensor.

$$x_{i,j} = \frac{2j - (n+1)}{n-1} \quad (4)$$

Eq. (5) is obtained similar to Eq. (4) as follows;

$$y_{i,j} = \frac{-2i + m + 1}{m-1} \quad (5)$$

Since the tactile elements are arranged at equal intervals,  $x_{i,j}, y_{i,j}$  for the tactile elements becomes an arithmetic progression resulting to the following equation.

$$\nabla^2 x_{i,j} = \nabla^2 y_{i,j} = 0 \quad (6)$$

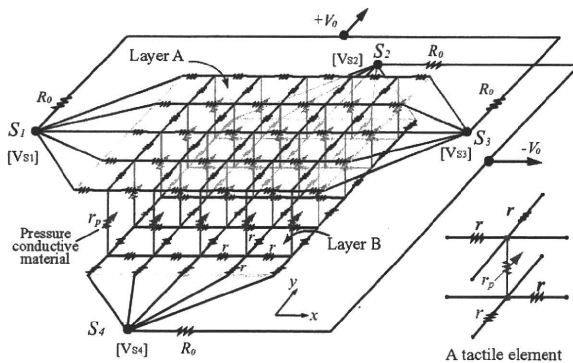


Fig. 2. Structure of the sensor

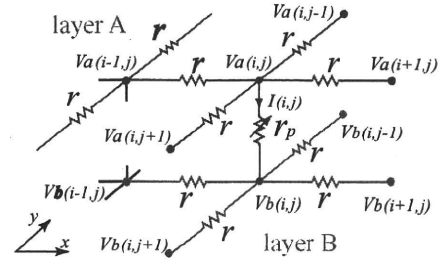


Fig. 3. Equivalent circuit of the sensor

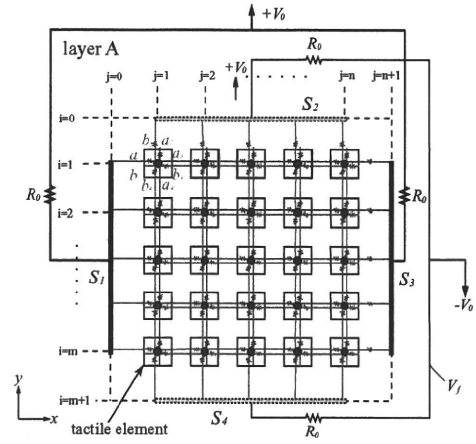


Fig. 4. Connection of tactile elements in layer A

### C. Boundary conditions

Let us consider the boundary condition about layer A. Boundaries  $S_2$  and  $S_4$  are not connected anywhere so that  $S_2$  and  $S_4$  are open terminals. Therefore it become as follows;

$$V_a(0, j) = V_a(1, j), \quad V_a(m+1, j) = V_a(m, j) \quad (7)$$

Considering boundaries  $S_1$  and  $S_3$ , there are tactile elements of layer A that are connected to the electrodes  $E_1$  and  $E_3$  so that currents flows in from the electrodes. Since the total of these currents is equal to the currents which flows through  $R_0$ , the boundary conditions are determined from Eq. (8), (9).

$$\frac{1}{R_0} \{V_0 - V_{E1}\} = \frac{1}{r} \left\{ \sum_{i=1}^m (V_{E1} - V_a(i, 1)) \right\} \quad (8)$$

$$\frac{1}{R_0} \{V_0 - V_{E3}\} = \frac{1}{r} \left\{ \sum_{i=1}^m (V_{E3} - V_a(i, n)) \right\} \quad (9)$$

Moreover, since for the electrode  $E_1$  is  $j = 0$ , and for  $E_3$  is  $j = n + 1$  in the sensor, then the boundary condition becomes;

$$V_a(i, 0) = V_{E1}, \quad V_a(i, n+1) = V_{E3} \quad (10)$$

Using the same methods described above for layer B, equations similar to Eq. (7), (8), (9) and (10) are obtained.

#### D. First-order moments of the current density distribution

The center position of the current distribution is determined by computing the first-order moments of the current distribution with respect to the x-axis. When the pressure-sensitive element is arranged in the shape of a matrix  $m \times n$ , the first-order moments of current distribution is expressed;

$$I_x = \sum_{i=1}^m \sum_{j=1}^n x_{i,j} I(i, j) \quad (11)$$

Considering  $I_x$ , Eq. (1) is applied to Eq. (11), resulting to;

$$I_x = \frac{1}{r} \sum_{i=1}^m \sum_{j=1}^n x_{i,j} \nabla^2 V_a(i, j) \quad (12)$$

Substituting Eq.(2) for Eq.(12) gives Eq. (13). Rearranging Eq. (13) gives Eq. (14).

$$\begin{aligned} I_x &= \frac{1}{r} \sum_{i=1}^m \sum_{j=1}^n x_{i,j} \nabla^2 V_a(i, j) \\ &= \frac{1}{r} \left\{ \sum_{i=1}^m \sum_{j=1}^n x_{i,j} V_a(i-1, j) + \sum_{i=1}^m \sum_{j=1}^n x_{i,j} V_a(i+1, j) \right. \\ &\quad + \sum_{i=1}^m \sum_{j=1}^n x_{i,j} V_a(i, j-1) + \sum_{i=1}^m \sum_{j=1}^n x_{i,j} V_a(i, j+1) \\ &\quad \left. - 4 \sum_{i=1}^m \sum_{j=1}^n x_{i,j} V_a(i, j) \right\} \quad (13) \end{aligned}$$

$$\begin{aligned} I_x &= \frac{1}{r} \left\{ \sum_{i=1}^m \sum_{j=1}^n V_a(i, j) \nabla^2 x_{i,j} \right. \\ &\quad + \sum_{j=1}^n (x_{m,j} V_a(m+1, j) - x_{m+1,j} V_a(m, j)) \\ &\quad + \sum_{j=1}^n (x_{1,j} V_a(0, j) - x_{0,j} V_a(1, j)) \\ &\quad + \sum_{i=1}^m (x_{i,n} V_a(i, n+1) - x_{i,n+1} V_a(i, n)) \\ &\quad \left. + \sum_{i=1}^m (x_{i,1} V_a(i, 0) - x_{i,0} V_a(i, 1)) \right\} \quad (14) \end{aligned}$$

Since  $x_{i,j}$  is equal to the direction of  $i$ , and also using Eq.(6), Eq.(7), the 1st, 2nd and 3rd term of Eq.(14) reduced to zero. Thus Eq. (14) is simplified as follows;

$$\begin{aligned} I_x &= \frac{1}{r} \left\{ \sum_{i=1}^m (x_{i,n} V_a(i, n+1) - x_{i,n+1} V_a(i, n)) \right. \\ &\quad \left. + \sum_{i=1}^m (x_{i,1} V_a(i, 0) - x_{i,0} V_a(i, 1)) \right\} \quad (15) \end{aligned}$$

When the boundary conditions Eq. (8) and Eq.(9), are applied to Eq. (15), and using Eq.(10), Eq.(15) is simplified to Eq. (16);

$$I_x = \frac{1}{n-1} \left( \frac{2m}{r} + \frac{n+1}{R_0} \right) \cdot (V_{E_1} - V_{E_3}) \quad (16)$$

Similarly, the first-order moments of the current distribution with respect to the  $y$  direction is determined as follows.

$$I_y = \frac{1}{m-1} \left( \frac{2n}{r} + \frac{m+1}{R_0} \right) \cdot (V_{E_2} - V_{E_4}) \quad (17)$$

The total current is calculated from the sum of the currents following into the electrodes  $E_1$  and  $E_3$  through resistance  $R_0$  as shown in Eq.(18). The total current following through electrodes  $E_2$  and  $E_4$  are computed likewise.

$$I_{all} = \sum_{i=1}^m \sum_{j=1}^n I(i, j) \quad (18)$$

$$= \frac{2V_0 - V_{E_1} - V_{E_3}}{R_0} = \frac{2V_0 + V_{E_2} + V_{E_4}}{R_0} \quad (19)$$

From the above equations, the center position of current distribution is calculated from Eq.(20)

$$x_0 = (I_x)/(I_{all}), \quad y_0 = (I_y)/(I_{all}) \quad (20)$$

#### E. Measurement of the center of the pressure distribution

The purpose of the proposed sensor is to measure the center of the pressure distribution. Therefore, let us consider the relationship between the current density  $i(x, y)$  and the distributed load  $F(i, j)$ . A pressure-sensitive electro-conductive rubber is used as a load sensing element. Its resistance  $r_p$  changes with load  $F(i, j)$ . The relation between resistance and load is represented by Eq. (21)

$$r_p(i, j) = \frac{1}{f(F(i, j))} \quad (21)$$

Since the resistance  $r$  is much lower than the resistance  $r_p$ , ( $r_p \gg r$ ), the voltage of layers A and B may be considered to be approximately constant. Thus, the following relationship is obtained:

$$\begin{aligned} I(i, j) &= \frac{V_a(i, j) - V_b(i, j)}{r_p(i, j)} = \frac{V_a - V_b}{r_p(i, j)} \\ &= (V_a - V_b) f(F(i, j)) \quad (22) \end{aligned}$$

The relation between resistance and load is assumed to follow Eq. (23), where resistance is in inverse proportion to the load.

$$r_p = \frac{1}{f(F)} = kF^{-1} \quad (23)$$

$k$  in the equation is a constant. The center position of the load distribution  $x_0, y_0$  and the total distributed load are then determined from the following equations.

$$x_0 = \frac{\sum_{i=1}^m \sum_{j=1}^n x_{i,j} \cdot F'(i,j)}{\sum_{i=1}^m \sum_{j=1}^n F(i,j)} = \frac{I_x}{I_{all}} \quad (24)$$

$$y_0 = \frac{\sum_{i=1}^m \sum_{j=1}^n y_{i,j} \cdot F'(i,j)}{\sum_{i=1}^m \sum_{j=1}^n F(i,j)} = \frac{I_y}{I_{all}} \quad (25)$$

$$F'_t = \sum_{i=1}^m \sum_{j=1}^n F'(i,j) = \frac{k I_{all}}{(V_a - V_b)} \quad (26)$$

#### IV. PLACEMENT OF TACTILE ELEMENTS

As described previously, the tactile elements are consist of resistors and a pressure-sensitive material. These tactile elements are arranged in a matrix, as shown in Fig. 5(a). However, a structure without any pressure-sensitive material, is also possible, in which case, the resistance of the pressure-sensitive material is equivalent to infinity.

In structures that do not include any pressure-sensitive material, tactile elements consist of resistors only, so that the structure are extremely compact. Accordingly, this increases flexibility in placement options, as shown in Fig. 5(b).

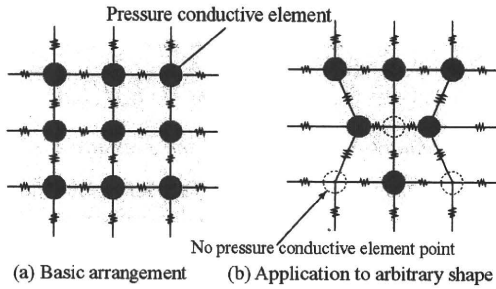


Fig. 5. Arrangement method of tactile element

#### V. PROTOTYPE OF SENSOR

The initial prototype sensor used a pressure-conductive rubber (dimensions  $12mm \times 12mm \times 5.2mm$  thick) manufactured by Inaba rubber CO.LTD, as the pressure-sensitive material. The prototyped sensor is shown in Fig.6. The elements were arranged in a  $3 \times 3$  grid. The resistance value was  $r = 150\Omega$ . As the sensor has a net-structure, it can be mounted on the sphere as shown in Fig. 6(b).

#### VI. EXPERIMENTAL VALIDATION OF CHARACTERISTICS

The sensor is designed to measure the overall load and the central position of the load distribution. To experimentally verify these basic functionalities of the sensor, load-measuring experiments and position-measuring experiments were conducted. As shown in Fig.8(a), each tactile element was numbered from  $T'(1,1)$  through to  $T'(3,3)$ .

##### A. Load-measuring experiment

In this experiment, cycle of pressure was applied to the central tactile element of the sensor  $T'(2,2)$  at a frequency of 0.2Hz using a vibrator(Wilcoxon research, F4/Z820WA), the tip of which was fitted with a load cell. The load cell output

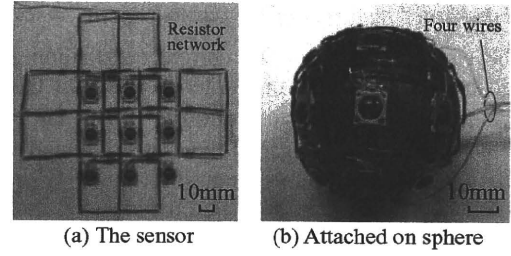


Fig. 6. Initial prototype of the net structure tactile sensor.

and the overall load output were measured. The results of this experiment are shown in Fig.7. A difference in output value due to the influence of hysteresis of the pressure-conductive rubber was observed when pressure was increased or decreased.

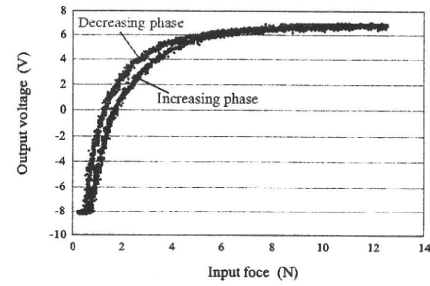


Fig. 7. Experimental result of sensor's total load output

##### B. Position-measuring experiment

When a load is applied to a single point, the sensor outputs the position where the load is applied. When loads are applied to multiple points, the sensor outputs the center position where the multiple points are applied.

1) *Position-measuring experiment for a single-point:* In this experiment, a load was applied to a single point on tactile element and the sensor position output value was measured. Fig.8(b) shows sensor's output ( $v_x, v_y$ ) when load was applied to each element. It was observed that the output's position was very well in agreement with the point of application of the load. The  $x$  component and the  $y$  component of the sensor's output changed at 3V intervals.

2) *Position-measuring experiment when loads are applied to two points:* In this experiment, loads were applied to two points. A constant load of 3N was applied to the tactile element at  $T(2,3)$ , while a load ranging from 0N to 3N was applied to the tactile element at point  $T(2,1)$ . The results of this experiment are shown in Fig.9. It was observed that sensor output changed proportionally with the load applied to the tactile element at  $T'(2,1)$ . It can be seen here that when the load applied to  $T(2,1)$  was at 3N, the sensor output value was 0V, its means the load distribution was centered.

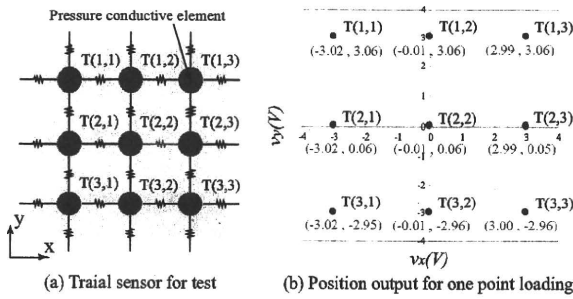


Fig. 8. Experimental results of sensor's position output for one point loading

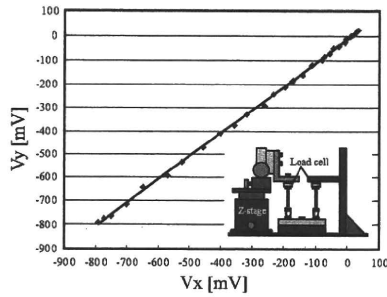


Fig. 9. Experimental results of sensor's position output for two point loading

### C. Position output when an impact load is applied (response time)

An experiment was carried out to clarify the response time of the sensor. In this experiment, an impact load was applied to the sensor using an impulse hammer (Ono sokki, GK-300), and the time until the position output value of the sensor became stable was measured. The experimental result is shown in Fig. 10. The time after adding the impact load until the value of the impact position becomes stable is approximately 0.6ms. Generally, controlling a robot using sensor feedback requires the control cycle time to be within 1ms. Thus, the proposed sensor can be used for such an application. The delay in the response time of the sensor is primarily a result of the delay in the response of the pressure-conductive rubber.

## VII. COVERING

When tactile elements are placed discretely, the load distribution between each element becomes a problem. For example, any load applied between each element cannot be detected. Accordingly, after each element is put in place, the elements must be covered with a flexible material such as silicon rubber. When each tactile element is covered with silicon rubber, any load applied to this cover also applies to the tactile element beneath as indicated by Eq. (27).

$$s(x, y) = \iint g(\xi, \eta) f(x - \xi, y - \eta) d\xi d\eta \quad (27)$$

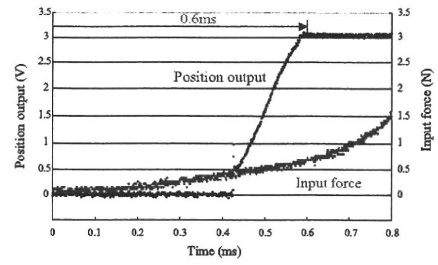


Fig. 10. Time response of the sensor's position output with an impulse load.

here,  $f(x, y)$  is a load applied on the cover,  $s(x, y)$  is pressure distribution on the tactile element,  $g(x, y)$  is the pressure distribution under the cover on whose surface point load  $F \cdot \delta(0, 0)$  is applied[13]. Thus, the load is spread among the individual elements. This is how the sensor is able to output the central point and the overall load. As shown in Fig.11(a), the sensor used in the experiments is covered with a hemispherical styrene foam. When the top surface of the cover was stroked with a finger to draw a circle, the locus of the position output of the sensor was shown in the Fig.11(b).

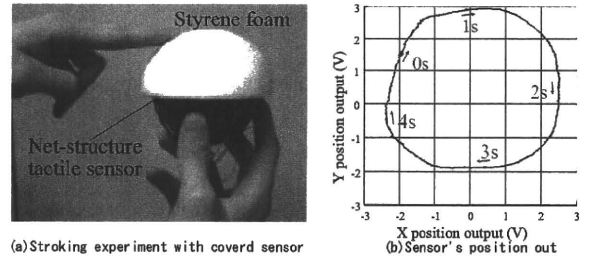


Fig. 11. Stroking experiment with sensor covered by styrene foam.

## VIII. PROTOTYPE OF TACTILE ELEMENT

A prototype tactile element was constructed. As shown in Fig.12, the sensor was formed of a resistor network combined with pressure-sensitive elements. The pressure-sensitive elements consist of pressure-conductive rubber laid down on top of electrodes (spiral shape). When load is applied to the rubber, the resistance of the rubber decreases, and the change in resistance value is measured by the spiral electrodes. The resistors used were chip-resistor.

Fig.13 shows the prototype of the tactile elements, arranged on a  $3 \times 3$  matrix form. The tactile element's dimensions were 10mm per side by 1mm thick. Each element can be cut from the sheet and may be attachable on any surface. Fig.14 shows the tactile sensor arranged to  $25 \times 5$  grid as the example. In this example, the area of sensor was extended and this sensor was used for walk measurement [16]. It was confirmed to operate appropriately when there were many wire like this example.

## IX. SUMMARY

A prototype net-structure tactile sensor was constructed with the aim of developing a sensor capable of covering a

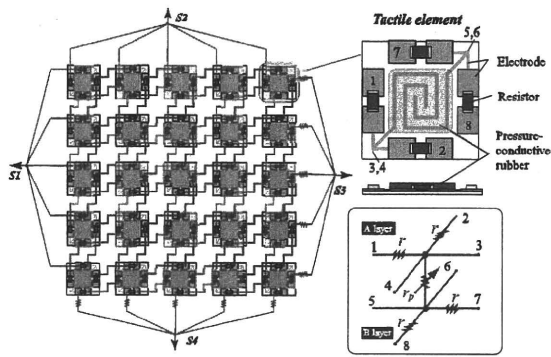


Fig. 12. Sensor using prototype of tactile element an enlarged view of tactile element

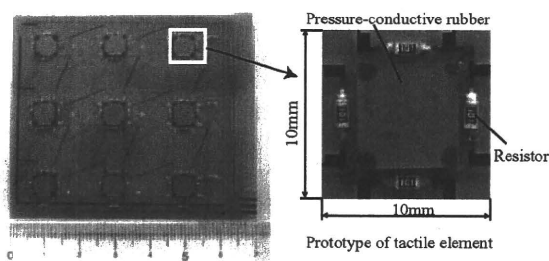


Fig. 13. Prototype of tactile element arranged on  $3 \times 3$  grid. Each element can be cut from the sheet and may be attachable on any surface.

robot's entire structure, including freeform surfaces, while reducing wiring requirement and ensuring high-speed response. The sensor is net-structured, capable of mounted on freeform surfaces, and can detect overall load, as well as the central point of load distribution, on 2-dimensional surfaces. The wiring requirement for multiple detection elements is simplified with only 4 output wires from the sensor. Moreover, the sensor response speed is nearly constant, regardless of the number of detection elements, their placements, or sensor areas. In this paper, the principle of the sensor, the process of constructing the prototype and the results of experiments were described.

## X. ACKNOWLEDGMENTS

We wish to express our thanks to Inaba rubber CO.,LTD for providing us with the prototype of the tactile element.

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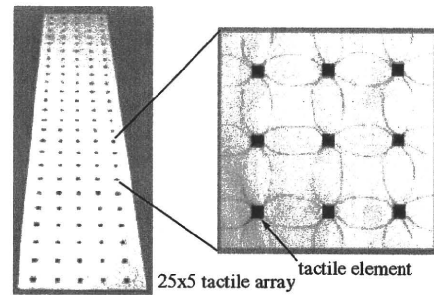


Fig. 14. Part of tactile element arranged on  $25 \times 5$  grid. Each element is cut from the sheet.

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# Knotting Manipulation of a Flexible Rope by a Multifingered Hand System based on Skill Synthesis

Yuji Yamakawa, Akio Namiki, Masatoshi Ishikawa and Makoto Shimojo

**Abstract**—In this paper, we examine the relationship between a knotting process and the individual skills of which a robot hand is capable. To determine the necessary hand skills required for knotting, we first analyzed the knotting action performed by a human subject. We identified loop production, rope permutation, and rope pulling skills. To take account of handling of the two ends of the rope, we added a rope moving skill. We determined the characteristics of these skills using an intersection-based description. The knotting process was examined based on the analysis of knots and the characteristics of the robot hand skills. Finally, we show experimental results of an overhand knot and a half hitch performed using a high-speed multifingered hand system.

## I. INTRODUCTION

Manipulation of flexible linear objects is an important problem in the field of robotics, and the number of studies looking at this problem has been increasing recently.

The authors have developed strategies for the skills required by a multifingered hand in a knotting task [1]. To improve the robustness of these strategies, we proposed high-speed visual and tactile sensory feedback control. We demonstrated successful completion of a so-called overhand knot by sequential application of the individual skills involved.

However, it has not been demonstrated that many knots can be produced using only these proposed skills. Therefore, in this paper we examine this point based on an original knot theory. The goal of this paper is to analyze the knotting process and to define the relationship between the knotting process and the individual skills that can be performed by a robot hand.

Finally, two kinds of knot (overhand knot and half hitch) were realized using a high-speed multifingered hand with tactile sensors and a visual sensor.

In this paper, “task” is defined as one manipulation carried out by the robot, and “skill” is defined as a minimum required element to achieve the task and a meaningful element that changes the rope state. Therefore, one “task” is achieved by the combination of a certain number of “skills”. In order to further develop the manipulation theory, it is important not only to achieve many tasks, but also to integrate the skills that are needed for task realization (Fig. 1(a)).

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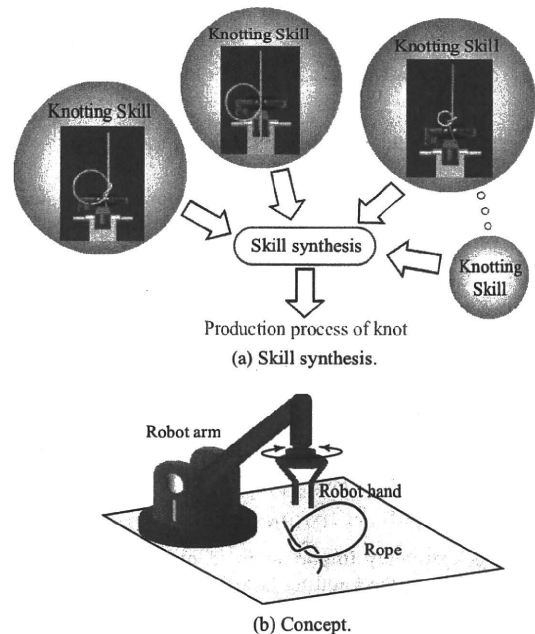


Fig. 1. Purpose of this research.

## II. RELATED WORKS

Some researchers have focused on manipulation of flexible linear objects. For example, Inaba et al. proposed a method of knotting a rope with a manipulator [2]. Matsuno et al. used an imaging system to recognize the shape of a rope and demonstrated knotting using dual manipulators [3]. Mitul et al. suggested a topological motion planner for manipulating flexible linear objects [4]. Morita et al. proposed a knot planning technique by using a system called Knot Planning from Observation (KPO) [5]. Wakamatsu et al. formulated a description of knots and a process of knot manipulation [6].

In this study, we focus on the relationship between the structure of a knot and the individual robot hand skills required to implement the knot, and we propose a new method of producing a knot with a robot hand. In addition, we also propose a new description that takes the type of grasp into account.

Knot manipulation has been demonstrated in numerous studies. These studies generally considered the geometry of the knot and proposed a knotting process; however, they did not match the actual type of manipulation performed by the hand. For example, even if the geometric condition



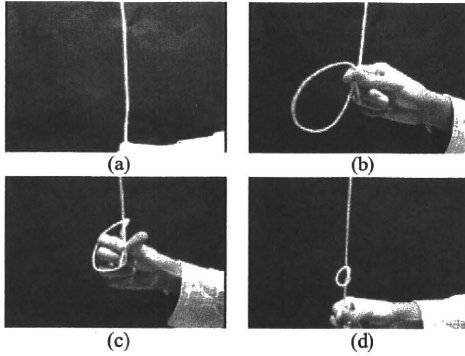


Fig. 2. One-handed knotting by human hand.

of a rope is the same, the knotting process substantially changes depending on the type of grasp (for example, loop production). Thus, to consider the actual manipulation by a robot hand, it is necessary to determine the relationship between the knotting process and the individual manipulation skills of the hand. In addition, a description of the knotting process that is appropriate to the robot hand should be considered.

The aim of this research is to identify the knot manipulation skills required by a general robot arm and robot hand to achieve a knotting process, as shown in Fig. 1(b).

### III. EXTRACTION OF KNOTTING SKILL

It is extremely important to identify the skills that are appropriate to the knotting task. There are two main reasons why the manipulation of a flexible linear object is difficult:

- 1) Deformation of the rope during manipulation, and
- 2) Difficulty of predicting the rope deformation.

To overcome these difficulties, the following strategies are considered:

- 1) Using sensory feedback control by real-time measurement of the rope deformation,
- 2) Identifying a manipulation skill that cancels rope deformation, and
- 3) Identifying a manipulation skill that exploits the rope deformation.

Based on these strategies, in order to identify manipulation skills required for knotting, we analyzed a one-handed knotting process performed by a human hand, as shown in Fig. 2. Fig. 2(a) is the initial state, Fig. 2(b) shows loop production using rope deformation by arm motion, Fig. 2(c) shows rope permutation by finger motion, and Fig. 2(d) shows rope pulling by arm motion. As a result, we identified three skills required to achieve one-handed knotting: loop production, rope permutation, and rope pulling.

Loop production is categorized as a manipulation skill that utilizes the rope deformation. Rope permutation is categorized as a manipulation skill that cancels rope deformation. Rope pulling is a motion required to complete the knot.

In addition, in order to allow handling of the ends of the rope, one more manipulation skill called rope moving

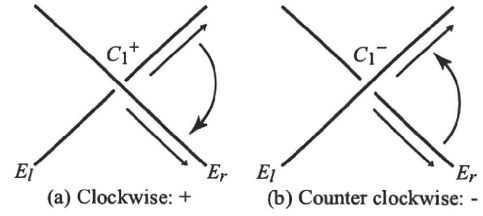


Fig. 3. Intersection sign [6].

is added. In summary, the essential manipulation skills for knotting are:

- 1) Loop production,
- 2) rope permutation,
- 3) rope pulling, and
- 4) rope moving.

### IV. DESCRIPTION OF INTERSECTION AND HAND SKILL

First, we define the description of a rope intersection that constitutes the knot, by referring to the method proposed in [6].

The beginning of a rope is represented by  $E_l$  (or  $l_1$  or  $r_1$ ) as the initial location. In the same way, the end of the rope is represented by  $E_r$  (or  $l_2$  or  $r_2$ ) as the final location. Descriptions of the intersections  $C_i^{+, -}$  ( $i = 1, 2, 3, \dots$ ) are assigned for all intersections from  $E_l$  to  $E_r$ , where  $i$  is an intersection number. The sign “+,” “-” shows the intersection sign. The sign “+” is clockwise, and the sign “-” is counterclockwise, as shown in Fig. 3. As a result, the description of the intersection is defined as shown in Fig. 3.

Moreover, we introduce a new description here. First, the two directions of the rope at “outlets” of the intersection are summed. Second, the line that connects the two fingers grasping the intersection is considered. Finally, the relationship between the summed rope direction and this connecting line is examined. If the relationship is parallel, the description of the intersection shown in Fig. 4(a) is obtained. If the relationship is orthogonal, the description of the intersection shown in Fig. 4(b) is obtained. This description method is used in loop production, in particular.

Next, the characteristics of the identified hand skills are clarified based on the intersection description. In this paper, a skill is defined as a minimum required element to achieve a task. In addition, the objective of this study is to clarify the relationship between the knot production process and manipulation skills. This relationship can be obtained from a description of the knot and analysis of the knot. Thus, recognition of the rope by a visual sensor is not taken into account in this paper.

#### A. Loop Production

Loop production is an operation that makes one intersection. Thus, the description of the intersection is given by:

$$E_l - E_r \longrightarrow E_l - \overline{C_1^{+, -}} - \overline{C_1^{+, -}} - E_r \quad (a)$$

$$E_l - E_r \longrightarrow E_l - \widehat{C_1^{+, -}} - \widehat{C_1^{+, -}} - E_r \quad (b)$$

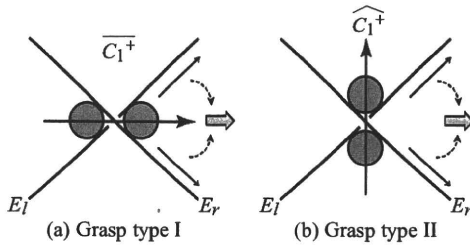


Fig. 4. Grasp type.

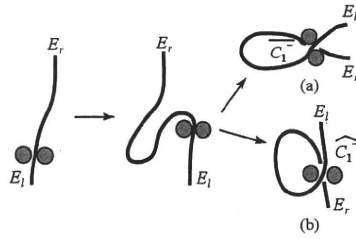


Fig. 5. Loop production.

This skill is equivalent to Reidemeister move I in knot theory. The intersection sign depends on the direction of the loop.

#### Loop production strategy

The process of loop production is shown in Fig. 5. In this skill, a loop that serves as the starting point of the knot is produced on the rope. First, the rope is grasped by two fingers. A loop is produced by the two dimensional translational motion of the hand. There are two different types of loop production depending on the grasp type of the two fingers, as shown in Fig. 5. This difference is important for performing the actual knotting process by robot fingers.

To achieve robust loop production, the hand motion should be controlled by real-time visual feedback [1].

#### B. Rope Permutation

Rope permutation is categorized into two types, depending on the grasp type. In the case shown in Fig. 6(a), the description of the intersection is the following:

$$\begin{cases} E_l - \overline{C_1^{(+,-)}} - \overline{C_1^{(+,-)}} - E_r \longrightarrow \\ E_l - \overline{C_1^{(+,-)}} - C_2^{(+,-)} - C_2^{(+,-)} - \overline{C_1^{(+,-)}} - E_r \end{cases}$$

In the case shown in Fig. 6(b), the description of the intersection is the following:

$$\begin{cases} E_l - \overline{C_1^{(+,-)}} - \overline{C_1^{(+,-)}} - E_r \longrightarrow \\ E_l - \overline{C_1^{(+,-)}} - C_2^{(+,-)} - C_3^{(+,+)} - \overline{C_1^{(+,-)}} \\ - C_2^{(+,-)} - C_3^{(+,+)} - E_r \end{cases}$$

The difference between the two types of rope permutation depends on the grasp type used in the loop production.

#### Rope permutation strategy

The process of rope permutation is shown in Fig. 7. Both fingers are moved while remaining parallel. At some point,

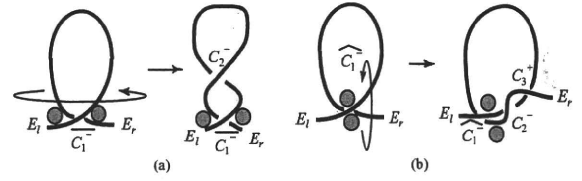


Fig. 6. Rope permutation.

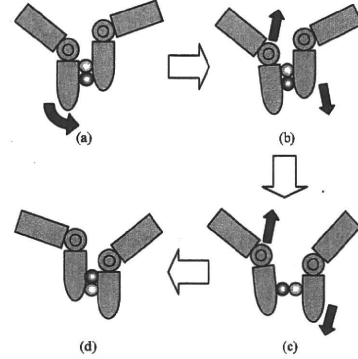


Fig. 7. Rope permutation strategy.

two sections of the rope engage each other by virtue of friction. By continuing to move the two fingers in parallel, the two sections of the rope are permuted (exchange places). At the moment of permutation, the grasp force is increased. In order to achieve smooth permutation, it is necessary to increase the distance between both fingers at this moment. Therefore, grasp force control based on tactile feedback is needed [1].

#### C. Rope Pulling

Rope pulling is an operation that basically removes the intersection, as shown in Fig. 8. This skill is effective when used together with rope permutation. Two effects can be realized by utilizing these two skills: One is the ability to create one intersection. Another is the ability to change the sign of any intersection. When one intersection is produced (Fig. 9), the description of the intersection is:

$$E_l - E_r \longrightarrow E_l - C_1^{(+,-)} - E_r$$

When the sign of an intersection is changed (Fig. 10), the description of the intersection is:

$$\begin{cases} E_l - C_1^{(+,-)} - \dots - C_i^{(+,-)} - \dots - C_1^{(+,-)} - E_r \\ \longrightarrow E_l - C_1^{(+,-)} - \dots - C_i^{(-,+)} - \dots - C_1^{(+,-)} - E_r \end{cases}$$

#### Rope pulling strategy

In general, rope pulling can be achieved by the translational motion of the robot hand.

#### D. Rope Moving

Rope moving is defined as the three-dimensional free motion of the end of the rope without other parts of the rope acting as obstacles. Assuming that the rope is located