

## サンプル

- 期間内はずっと交付・不交付のいずれかにあった団体
- 一部道府県の市については1984年の保護率データなし。サンプル規模は435(1984-1986年)と424(1984-1987年)
- 1985年は国勢調査の年、利用可能な変数をコントロール変数として用いる。
- 処置変数をランダム化するために、各年の $\ln(\text{基準財政需要額}/\text{基準財政取入額})$ をコントロール変数に加える。

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## 推定結果

- 別紙ご参照

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## Differences Estimation

- 2つのATE
- パラメトリックな推定
  - ※ →条件無しの平均処置効果
- ノンパラメトリックな推定
  - ※ →閾値付近での条件付き平均処置効果

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## パラメトリック推定

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### 平均処置効果 (Average treatment effect) の推定

- 教科書的なATE推定の延長 (Wooldridge 2002)
- Conditional mean independenceをもたらし方法としてSRDDを利用。
  - 説明変数(生活保護率)の選択変数(需要収入比率)に関する条件付期待値(統制関数)をパラメトリックに特定化することによって、交付税の効果をunconditional ATEとして推定することが可能。
  - 統制関数の特定化を戻ると戻った推定を行うおそれ。

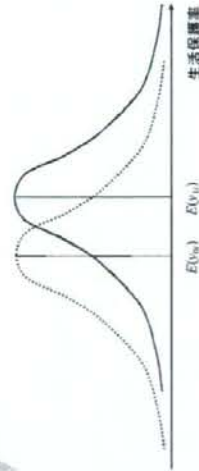
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### 平均処置効果 (Average treatment effect)

- 処置効果  $TE = y_{1t} - y_{0t}$ 
  - $y_{1t}$ : 政策介入があった場合 ( $w_t=1$ ) の保護率
  - $y_{0t}$ : 政策介入がなかった場合 ( $w_t=0$ ) の保護率
- 平均処置効果
  - $\mu_1 = E(y_{1t}), y_{1t} = y_{1t} - E(y_{1t}) \Rightarrow y_{1t} = \mu_1 + \psi_{1t}$
  - $\mu_0 = E(y_{0t}), y_{0t} = y_{0t} - E(y_{0t}) \Rightarrow y_{0t} = \mu_0 + \psi_{0t}$
  - $ATE = E(y_{1t} - y_{0t}) = \mu_1 - \mu_0$

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### 図3. モデル—平均措置効果 (ATE)



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### モデル—平均措置効果 (ATE)

平均処置効果とは？

- 処置を受けた個体
- 処置を受けていない個体
- 処置を受けていない個体が処置を受けたとしたときの状態
- 処置を受けた個体
- 処置を受けた個体が処置を受けなかったときの期待値 (と\*)
- 全ての個体が処置を受けたとするときの期待値 (と\*)

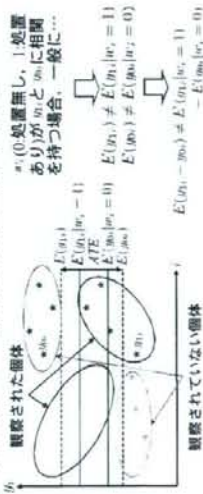
平均処置効果:  $E(y_{1t} - y_{0t}) = E(y_{1t}) - E(y_{0t}) = \mu_1 - \mu_0$   
 なお,  $\mu_1 = E(y_{1t}), \mu_0 = E(y_{0t})$

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## モデル-A TEの推定上の問題

ATEを推定するにあたっての2つの問題点

- 問題点1:  $y_{01}$ と  $y_{00}$ を同時に観察することができない  
 問題点2: ATEの適切な推定量 ≠ 標本平均の差



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## モデル-条件付き期待値の独立性(1)

- 平均処置効果  $E(y_1 - y_0) = E(y_1) - E(y_0) = \mu_1 - \mu_0$  の推定。
- 観察されるデータは

$$y_i = \alpha_1 D_i + (1 - D_i) \alpha_0$$

と表現することが可能である。これは、 $\delta = \mu_1 - \mu_0$ 、 $\alpha_0 \equiv y_0$ 、 $\alpha_1 \equiv y_1 - \delta$  および、 $\epsilon_i \equiv y_i - \mu_i$  とすると、

$$y_i = \mu_0 + \alpha_1 \delta + \epsilon_i \quad \epsilon_i \equiv y_{0i} + \alpha_1 (y_{1i} - y_{0i})$$

となる。

- 一般的に  $\alpha_1$  と  $\delta$  は独立とは考えられないから  
 $E(\epsilon_i | D_i) = E(y_{0i} | D_i) - \alpha_1 [E(y_{1i} | D_i) - E(y_{0i} | D_i)] = 0$  とならず、OLSで  $\alpha_1$  の係数を推定することは不適切。

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## モデル-条件付き期待値の独立性(1)

$(y_1, y_0)$  の  $y_1$  と  $y_0$  に関する条件付き期待値を考える。

$y_1$  の条件付き期待値は  $E(y_1 | x_1, x_2) = \mu_0 + \alpha_1 \delta + E(\epsilon_1 | x_1, x_2)$  と表現できる。ここで、

$$E(\epsilon_1 | x_1, x_2) = E(y_{01} | x_1, x_2) + \alpha_1 [E(y_{11} | x_1, x_2) - E(y_{01} | x_1, x_2)]$$

と表現されることに注意。

$y_0$  が  $x_2$  の要素によって説明されると、

$$y_0 = g(x_2) \text{ と書けるので、} \\ E(\epsilon_1 | x_1, x_2) = E(y_{01} | g(x_2), x_1) = E(y_{01} | x_2), \quad j = 0, 1 \text{ となる}$$

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$$E(y_{01} | x_1, x_2) = E(y_{01} | x_2) = 0$$

## モデル-条件付き期待値の独立性(2)

更に、

$$\epsilon_i \equiv y_{0i} + \alpha_1 (y_{1i} - y_{0i})$$

$$= E(y_{0i} | x_i) + \alpha_1 [E(y_{1i} | x_i) - E(y_{0i} | x_i)] + u_i$$

とすると、

$$u_i \equiv y_{0i} + \alpha_1 (y_{1i} - y_{0i}) - E(y_{0i} | x_i) - \alpha_1 [E(y_{1i} | x_i) - E(y_{0i} | x_i)]$$

であるから、 $E(u_i | x_i, x_2) = E(u_i | x_2) = 0$  となる。

つまり、

$$\mu_1 = \mu_0 + \alpha_1 \delta + E(y_{01} | x_2) + \alpha_1 [E(y_{11} | x_2) - E(y_{01} | x_2)] + u_1$$

からの  $\delta$  の最小自乗推定量はATEの適切な推定量となる

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### 鋭角型回帰非連続設計 (SRDD: sharp regression discontinuity design)

○ ここで処置変数を完全に説明できる別の変数  $x$  を考える。

$$w_j = w(x_j) = 1 \{x_j > c\}, c=0$$

- $w_j$ : 交付団体が否かを表すダミー変数
- $x_j$ : ln(基準財政需要額/基準財政収入額)

→ 鋭角型回帰非連続設計 (SRDD design: sharp regression discontinuity design) となる

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### 統制関数 (control function)

実際に推定する場合、条件付期待値  $E(y_i | x_i)$  を特定化する必要がある

$$E(y_i | x_i) = \theta_0 + x_i \cdot \gamma + \Delta x_i \cdot \eta + \varepsilon_i$$

推定すべき式は

$$\theta_0 = \alpha + w_i \cdot \delta + x_i \cdot \gamma + \Delta x_i \cdot \eta + \varepsilon_i$$

ただし,

$$\alpha \equiv \mu_0 + \theta_0$$

$$\gamma \equiv \delta_1$$

$$\eta \equiv \delta_2 - \delta_0$$

$$\Delta x_i \equiv x_i - E(x_i)$$

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### 推定モデル

- 統制変数には分散を小さくするため、コントロール変数 ( $z_k$ ) を加える。
- 推定式

$$y_i = \gamma + \alpha w_i + \sum_p \eta_{0p} x_i^p + \sum_k \pi_k z_{ki} \\ + w_i \sum_p \psi_p (x_i^p - \sum_k x_i^p / n) \\ + w_i \sum_k \zeta_k (z_{ki} - \sum_k z_{ki} / n) + u_i$$

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- $E(v_{\mu} | x_i)$  - 統制関数 (control function) - の特定

$$E(v_{\mu} | x_i) = g(x_i) = \theta_j + \sum_p \eta_{jp} x_i^p$$

↓

$$E(v_{\mu} | x_i) = \gamma + \delta w_i \\ + \sum_p \{ \eta_{0p} x_i^p + w_i \psi_p [x_i^p - E(x_i^p)] \} \\ \gamma \equiv \mu_0 + \theta_0, \psi_p \equiv \eta_{1p} - \eta_{0p} \\ E(x_i^p) \leftarrow \text{サンプル平均}$$

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## ノンパラメトリック推定

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## 閾値付近の条件付き平均処置効果の推定

- パラメトリックな推定方法 (Thistlethwaite and Campbell 1960, Trochim 1984 and 2006)
- ノンパラメトリックな推定方法 (Imbens and Lemieux 2007) → ここで用いている方法
  - Local Linear Regression (Fan and Gijbels 1996) の応用
  - 帯域幅 (bandwidth) の推定が必要
  - 推定されるのは閾値近傍付近の条件付き平均処置効果 (条件無しの平均処置効果ではない)

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## 推定対象

- 閾値  $x_f = c=0$  近傍での条件付き平均処置効果

$$E(y_{1t} - y_{0t} | x_f = c) =$$

$$\lim_{x_f \downarrow c} E(y_t | x_f = x) - \lim_{x_f \uparrow c} E(y_t | x_f = x)$$

- したがって、閾値での discontinuity (jump) が前提

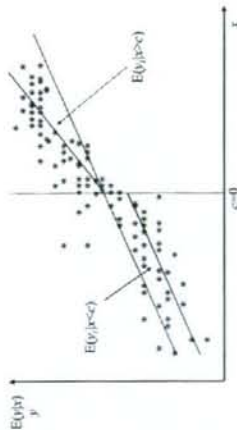
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## 鋭角型の回帰非連続設計: sharp regression discontinuity (SRDD) design

- 閾値 (ここでは、基準財政需要額/基準財政収入額 = 1、もしくは、ln(基準財政需要額/基準財政収入額) = 0) を挟んだ、適合推定量 (matching estimator) の一種。
- 閾値の近傍では、同様の特徴をもつ観測単位が、たまたま、処置 (交付税) を受けたり、受けなかったりしている。したがって、当該閾値の近傍では似通った特徴を有する観測単位にランダムに処置が与えられることになる。

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図5. SRDD: 図説



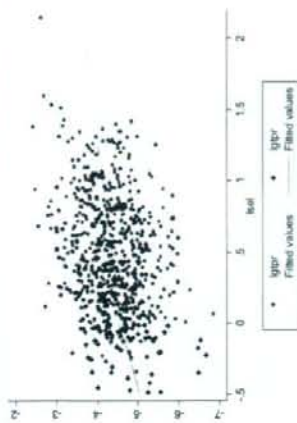
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Local Linear Regression のSRDDへの  
応用(Imbens and Lemieux 2007)

- 手順
  - 帯域幅 (bandwidth) を交差検定 (cross validation) により特定化
  - 特定化された帯域幅内の観測値を標本として、既述のパラメトリック推定で用いたモデルのうち、線形モデルをOLS推定 (+HCCME)。
  - 閾値から離れた観測値の効果を受けない

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図4. 生活保護率と需要収入比率 (2005年全市)



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推定: local linear regression

- モデル ( $c=0$ )
  - (1)  $y_i = \alpha + \beta(x_i - c) - \delta w_i + w_i \gamma (x_i - c) + \sum_k \phi_k z_{ki} + u_i$   
(Imbens and Lemieux 2007)
- カーネルはrectangular (帯域幅に落ちたデータには重み1、他のデータは重み0)
- 推定量はOLS+HCCME

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### CV: 交差検定(Cross Validation)

- ① 観測単位に $x$ の値にしたがって順位をつける(順位は添え字で表す)。
- ② 順位づけられた標本を $x$ の閾値=0を挟んで2つにわけ、それぞれ中央値をもってCVで考察する標本の上限と下限とする。
- ③ 任意の帯域幅 $h$ を所与として観測単位 $j$ に関し、 $x_j < x_j + h$  (もしくは $x_j - h < x_j$ ) となる観測単位をサンプルとして通常の最小自乗法を行い、その切片の推定値を $\alpha(x_j)$  (もしくは $\alpha(x_j)$ ) とする。

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### CV: 交差検定(Cross Validation)

- ④  $\mu(x) = \alpha_+(x)$  if  $x_j > 0$ ,  $\mu(x) = \alpha_-(x)$  if  $x_j < 0$  と定義し、次の値を最小化する $h$ を求める。  

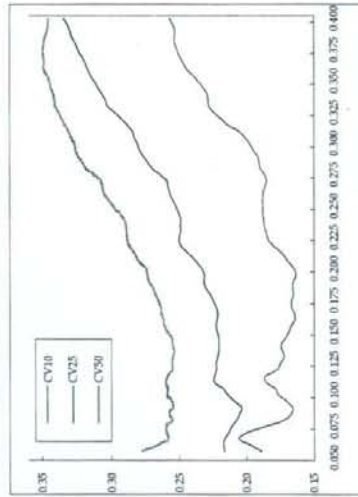
$$CV(h) = N^{-1} \sum [y_j - \mu(x_j)]^2$$
- ⑤ CVで考察する標本規模を絞ることによって選択される帯域幅 $h$ の感度を確認する。
  - CV50:  $e=0$ を挟んだ50%標本のCV( $h$ )
  - CV25:  $e=0$ を挟んだ25%標本のCV( $h$ )
  - CV10:  $e=0$ を挟んだ10%標本のCV( $h$ )

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### 推定結果

- 別紙ご参照

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	CV <sub>50</sub>	CV <sub>25</sub>	CV <sub>10</sub>
最小のCVをむいたらす帯域幅	0.135	0.090	0.195

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## Who Wins, Who Loses and By How Much? Predicting the Current, Future and Spatial Impact of Policy Change Using Microsimulation Models

Presentation to 'National Institute of Population and  
Social Security Research' Seminar Series, Tokyo

Professor Akihiro Hauring

27 January, 2009

## Australian cash transfer system

- Almost all payments are income and asset tested (targeted to those in most need)
- Age pensions, disability, parenting payment single (child < 8)
- 'Allowances' have much harsher income tests & and may be activity tested - Newstart (unemployed), Youth Allowance
- Relatively high cash payments to families with children
- Benefits are **flat-rate**, paid from general revenue
- Quite different to the social insurance (earnings-related) systems of Europe
- Numerous other minor payments (Rent assistance etc)
- Plus 'health' concession cards (passport to concessional pharmaceuticals)

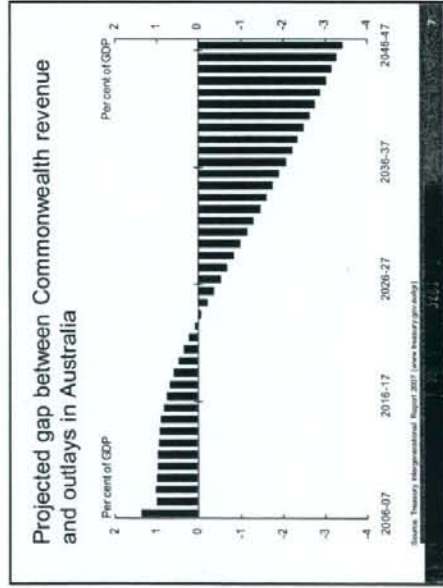
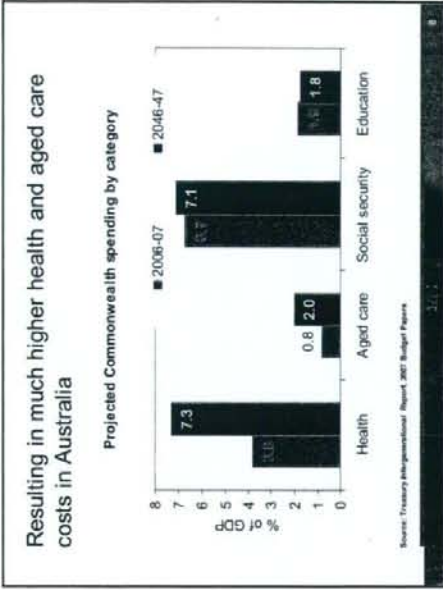
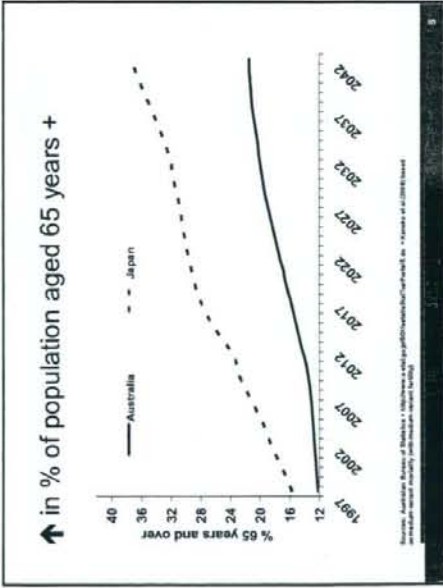
## Income tax side

- 'Progressive' tax schedule means that marginal tax rates increase as income increases
- Top marginal rate of 45c in \$ above \$180,000 + 1.5% Medicare levy
- Also a multitude of tax concessions for specific groups
  - Senior Australians Tax Offset
  - Low Income Tax Offset
  - Mature Australians Tax Offset
  - Pensioner Rebate/Beneficiary Rebate

## Challenges facing Australian welfare state

- Population ageing
- High effective marginal tax rates (work incentives)
- Currently major reviews underway
  - Harmer pension review (reports February 2009)
  - Henry tax review (reports December 2009)





## Using microsimulation models in policy process

## What are microsimulation models?

- **Based on microdata sets**
  - Records of individual people or households
  - Usually large – thousands of records
    - Sample surveys (Australian Bureau of Statistics), or
    - Administrative data
- **Allow detailed assessment of impact of change**
  - On individuals
  - On groups of individuals
  - On whole population
  - On government budgets

## Static models widely used across developed world

- **Static tax-transfer models show *morning after* impact of a policy change**
- **EUROMOD for EU15 (and soon 25)**
- **TRIM model in US (<http://trim3.urban.org/>)**
- **SPSD/IM for Canada**
- **LOTTE for Norway**
- **GLADHISPANIA for Spain**
  - See Gupta and Harding (2007) for summaries of 22 microsimulation models in use across the world

## Static tax-transfer models



### STINMOD – Australian model

- **Static microsimulation model replicating rules of the Australian tax, social security, & family payments systems**
- **'Day after' impact, no behavioural change**
- **Developed by NATSEM, first release STINMOD 94, latest is STINMOD 08**
- **Shows impact of possible policy changes**
  - Fiscal (revenue and expenditure)
  - Distributional (winners and losers)
  - Effective marginal tax rates (EMTRs)



INCOME TAX SCALE PARAMETERS  
Income Tax Scale Steps  
y2008

Step	Income	Marginal Rate
Step One	0	0.00
Step Two	5000	0.15
Step Three	10000	0.20
Step Four	50000	0.30
Step Five	100000	0.45
Step Six		
Step Seven		
Step Eight		
Step Nine		
Step Ten		

DK Refresh Cancel Flat Tax

0 5000 10000 50000 100000

0.00 0.15 0.20 0.30 0.40 0.45

ESTIMATED SIMULATION OUTCOMES  
Impact on 2008-09 of tax changes announced in 2007 election campaign  
y2008

Number of Families	Proportion	\$ Change in Average Weekly Income
Winners : 7,010,000	63.4	18.6
Losers : 0	0.0	0.0
No change : 4,048,000	36.6	0.0
Total : 11,058,000	100.0	11.8

Note: This and the following two tables also include the impact of other tax changes announced in the election campaign.

ESTIMATED ANNUAL PORTFOLIO OUTCOMES  
Impact on 2008-09 of tax changes announced in 2007 election campaign  
y2008

Portfolio	Base Outcome \$m	Simulation Outcome \$m	Difference \$m
Outlays			
FACS	69115.591	69115.591	0.00
DWH	5777.709	5777.709	0.00
Revenue			
TAX OFFICE	106093.743	99308.174	-6785.57
		Net Outcome	6785.57

**Income by Family Type and Income**

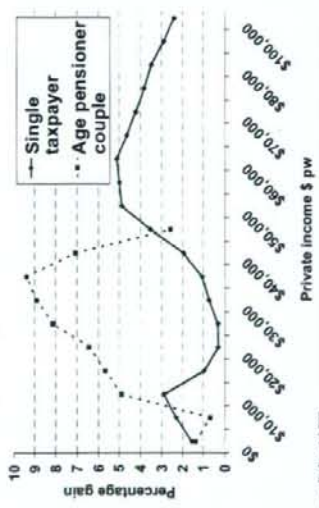
Estimated Change in Family Disposable Income - \$ pw  
 Impact on 2008-09 of tax changes announced in 2007 election comp  
 Outcomes: ALL  
 Population: ALL Recipients  
 y2008

Weekly Taxable Income	Family Type				ALL
	Married no child.	Married + children	Sole Parent	Single Adult	
< 150	0.20	0.58	0.00	0.00	0.05
150-299	0.26	0.33	0.08	0.71	0.56
300-449	0.45	2.09	1.62	5.62	3.32
450-599	1.47	7.03	6.35	8.88	5.59
600-749	1.78	15.86	16.53	19.36	16.53
750-899	2.07	28.53	19.37	28.53	19.37
900-1049	24.27	18.53	19.37	19.37	19.37
1050-1199	21.33	18.82	15.88	12.77	16.69
1200-1349	23.78	20.35	13.47	11.54	17.84
1350-1499	26.20	21.61	13.69	11.54	19.45
1500+	26.45	24.85	15.42	11.54	23.65
TOTAL	13.15	21.07	7.32	7.36	11.80

**The Great Australian tax reform debate, 1998-2000**

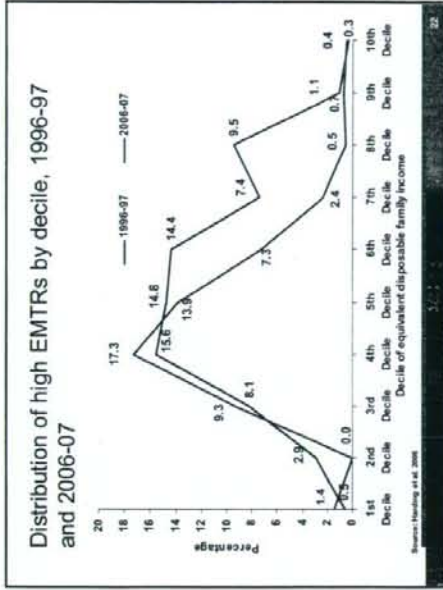
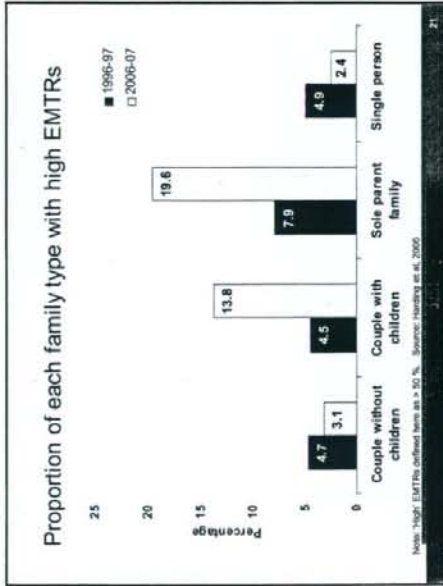
- Introduction of 10% goods & services tax (like VAT)
- Removal of existing inefficient indirect taxes (wholesale sales tax)
- Major cuts in income tax
- Large increases in social security to compensate poor
- Question: how to ensure tax reform package is fair?
- Answer: assess its distributional impact using microsimulation models -> use NATSEM
- Compensation to poor increased after NATSEM analysis

**% gain in disposable income in July 2000 tax reform package**



**Trends in effective marginal tax rates (EMTRs)**

- With ageing population and labour shortages, EMTRs are a major policy issue
- Australia wants to reduce work disincentives - issue being considered in current Treasury Tax Review
- EMTRs measure the proportion of an additional dollar of earnings that is lost to both income tax and the reduction of income-tested government benefits (e.g. Newstart, Aged Pension, Family Tax Benefit (FTB))
- Australian system highly means-tested:
  - In 2006-07, 7.1% of working-age Australians (\$10,000 people) faced EMTRs of 50c in the dollar or more.
  - Up from 4.8% in 1996-97



**NATSEM**  
NATIONAL TAX SIMULATOR  
UNIVERSITY OF LEEDS

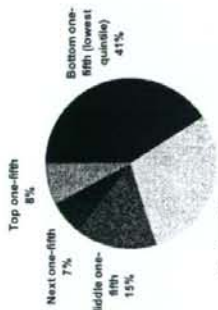
## Health microsimulation models

### MediSim: The Australian Pharmaceutical Benefits Scheme

- PBS aims to provide affordable access to prescription medicines
- Concessional patients – pay up to \$5.00 per script in 2008 (government pays rest)
- General patients – pay up to \$31.30 per script in 08
- Cost Federal govt. \$5.7 bn in 2006-07
- Second Intergenerational Report predicts spending on pharmaceutical benefits to grow faster than other areas
  - 0.7% GDP in 2006-07 to 2.5% GDP in 2046-47



### % of total PBS outlays received by each income quintile



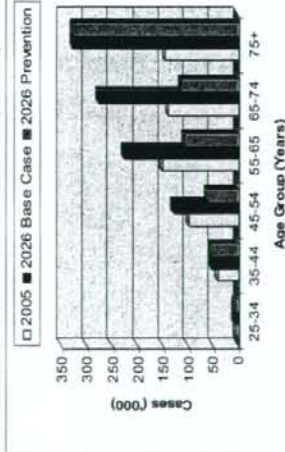
Revised by replacement disposable income of 2001 family unit by year. OECD 2004

Source: Harding et al., 2004

### Other health models

- HealthMod – cost and use of doctors (Medicare)
- HospMod – cost and use of public and private hospitals
- Diabetes model – long-term costs and benefits of diabetes prevention and management strategies
- DYNOPTA – optimising ageing and compressing morbidity – dynamic model of 45+ yr olds
- Dementia modelling
- NHMRC Economics and Financing of Health project
  - With Monash Uni
  - Linking MONASH macro model to NATSEM's micro models

### Estimated Reduction in Diabetes from a Secondary Prevention Program (Males)



Example of the reduction in the number of Australians with Type 2 diabetes in 2026 if a secondary prevention program, designed to halve the incidence of Type 2 diabetes in 2005, was implemented. The 2005 incidence of Type 2 diabetes is 200 per 100,000 population.

### Dynamic models: simulating the future

## History

- Treasury Intergenerational Report highlighted policy changes coming
- Model required to look at equity issues
  - Modelling underlying the IGR is at an aggregated level
  - New modelling capacity required to assess:
    - the distributional impact of future changes
    - the inter-generational redistributive impacts
    - the likely capacity to pay of different groups
- Dynamic microsimulation provides both aggregate and distributional outcomes

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## The Australian Population and Policy Simulation Model (APPSIM)

- 5 year project, started in late 2005
- Funded by the ARC and 12 Commonwealth Govt agencies
- Similar to SESIM (Sweden), DESTINIE (France), MOSART (Norway), DYNACAN (Canada), PENSIM (UK)



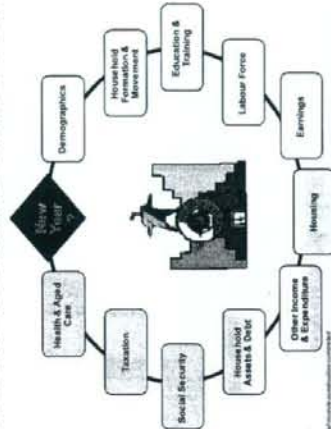
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## APPSIM

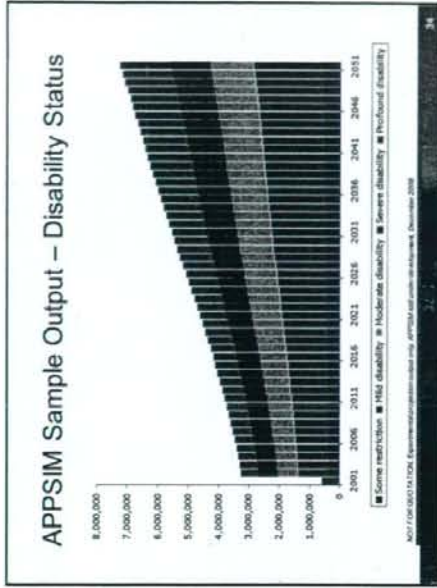
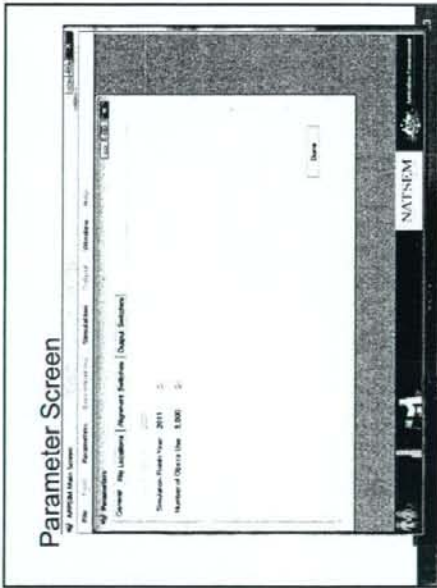
- APPSIM aims to provide snapshot output of the characteristics of the population and government programs as at 30 June each year.
- Base data is 2001 Census one per cent sample file (188,000 people), stored in Microsoft Access database
- Parameters stored in Excel spreadsheets and language is C#
- Full population modal, with individuals being aged to about 2050, discrete yearly time unit
- HILDA panel data being used to estimate transition probabilities
  - 5 years of data, 7000 households, sample size problems
- Alignment required to match ABS population projections and Treasury Intergenerational Report labour force projections

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## Processes to be modelled within APPSIM



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## Spatial microsimulation models

### Spatial Microdata and Microsimulation

- Combine the information-rich ABS survey data with the geographically disaggregated Census data
- Using 'spatial microsimulation' to create detailed unit record data for small areas (synthetic spatial microdata)





### Application 2: Predict spatial impact of a policy change

- Spatial microdata now linked with NATSEM's existing microsimulation models to model the immediate distributional/revenue impact of a policy change
- link synthetic spatial output to STINMOD and model changes to the tax and transfer system for small geographic areas
- Currently modelling changes in Commonwealth Rent Assistance, income tax, social security and family payments
  - spatialMISM and HOUSEMOD models

### Where did the \$5bn of 2005-06 tax cuts go?

2004-05		2005-06	
Tax threshold	Tax rate	Tax threshold	Tax rate
\$6,000	0.17	\$6,000	0.15
\$21,000	0.3	\$21,000	0.3
\$58,000	0.42	\$63,000	0.42
\$70,000	0.47	\$95,000	0.47

### Estimated average tax cut per household per week, Sydney SLAs, 2005-06



### Application 3: Develop needs-based planning indicators

- CAREMOD
  - 'Regionalised' Survey of Disability, Ageing and Carers
  - Simulating current and future characteristics of older Australians
  - At a detailed regional level (SLA)
  - Imputing functional status and thus likely need for different types of care
- Projecting current and future need for services at small area level
  - Given population ageing
- Research partners: NSW, Vic, Qld and ACT





