## Ability of Polyvinylpyrrolidone and Polyacrylic Acid to Inhibit the Crystallization of Amorphous Acetaminophen

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ABSTRACT: The inhibition of crystallization of amorphous acetaminophen (ACTA) by polyvinylpyrrolidone (PVP) and polyacrylic acid (PAA) was studied using amorphous solid dispersions prepared by melt quenching. Co-melting with PVP and PAA decreased the average molecular mobility, as indicated by increases in glass transition temperature and enthalpy relaxation time. The ACTA/PAA dispersion exhibited much slower crystallization than the ACTA/PVP dispersion with a similar glass transition temperature value, indicating that interaction between ACTA and polymers also contributed to the stabilizing effect of these polymers. The carboxyl group of PAA may interact with the hydroxyl group of ACTA more intensely than the carbonyl group of PVP does, resulting in the stronger stabilizing effect of PAA. Dielectric relaxation spectroscopy showed that the number of water molecules tightly binding to PVP per monomer unit was larger than that to PAA. Furthermore, a small amount of absorbed water decreased the stabilizing effect of PVP, but not that of PAA. These findings suggest that the stronger stabilizing effect of PAA is due to the stronger interaction with ACTA. The ability of PAA to decrease the molecular mobility of solid dispersion was also larger than that of PVP, as indicated by the longer enthalpy relaxation time. © 2004 Wiley-Liss, Inc. and the American Pharmacists Association J Pharm Sci 93:2710-2717, 2004

Keywords: solid dispersion; crystallization; calorimetry (DSC); water sorption

### **INTRODUCTION**

The solubility and dissolution-related bioavailability of poorly water-soluble pharmaceuticals can be improved by preparing amorphous solids using spray drying, melt extrusion, melt quenching, milling, and so on. Because amorphous solids are physically unstable, various stabilizing methods have been reported, including the usage of polymer excipients having high glass transition temperature  $(T_{\rm g})$ . Crystallization of amorphous sucrose and indomethacin was inhibited by preparing solid dispersion with a small amount of polyvinylpyrrolidone (PVP). <sup>1-3</sup> Similarly, addition of alginate inhibited the crystallization of

amorphous lactose prepared by spray drying.<sup>4</sup> The stabilizing effect of these excipients was attributed to their antiplasticization effect as well as their ability to interact with sucrose, indomethacin, or lactose. Both antiplasticization and interaction effects of excipients were affected by water molecules.<sup>1–4</sup>

Drug-excipient interactions leading to the stabilization of amorphous drugs have also been reported for the systems of excipients with a pyrrolidone ring (PVP and polyvinylpyrrolidone-co-vinyl acetate) and drugs with hydrogen donor groups (indomethacin, lacidipine, nifedipine, and tolbutamide).<sup>5</sup> To elucidate how drug-excipient interactions contribute to the stabilization of amorphous drugs, it may be necessary to examine the effect of various excipients to stabilize a certain amorphous drug.

In this study, we examined the crystallization of acetaminophen (ACTA) in solid dispersions with PVP and polyacrylic acid (PAA) to gain further

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insight to the role of drug-polymer interaction in the inhibition of crystallization as well as the effect of moisture on the interaction. PVP and PAA, polyvinyl compounds with different side chains, may exhibit different modes of drug-polymer interaction, because the latter can be a proton donor as well as a proton acceptor. Different water-vapor sorption behaviors may also be expected between PVP having a pyrrolidone ring and PAA having a carboxylic group in the molecules. The effect of water on the crystallization of ACTA is discussed based on the physical properties of water absorbed into these polymers determined by dielectric relaxation spectroscopy (DRS) using time domain reflectometry.

### **MATERIALS AND METHODS**

#### Materials

ACTA was obtained from Sigma Chemical Co. PVP with weight average molecular weight of 40,000, and PAA with weight average molecular weight of 25,000 were purchased from Wako Pure Chemical Industries Ltd. Other reagents were of analytical grade.

### Measurement of Isothermal Crystallization Rate of ACTA

Amorphous ACTA was prepared by melt quenching in a cell of a differential scanning calorimeter (DSC2920, TA Instruments) with a dry nitrogen gas purge at 20 mL/min. Indium was used to calibrate the cell constant and the temperature of the instrument. ACTA crystal (2-3 mg) in an aluminum pan was heated to 220°C at a heating rate of 20°C/min, kept at 220°C for 3 min, and then cooled to -70°C at a cooling rate of 35°C/min by pouring liquid nitrogen into the cooling jacket surrounding the cell. The samples were stored at a constant temperature (25-45°C) in desiccators containing P<sub>2</sub>O<sub>5</sub>. After certain periods of time, the sample pans were immediately sealed and the change in heat capacity ( $\Delta C_p$ ) at  $T_g$  was measured with a heating rate of 20°C/min. The ratio of amorphous form remaining at time t, x(t), was calculated according to eq. (1):

$$x(t) = \Delta C_{pt} / \Delta C_{p0} \tag{1}$$

where  $\Delta C_{pt}$  and  $\Delta C_{p0}$  are the changes in  $\Delta C_p$  at time t and initially, respectively. The decrease in x(t) as a function of storage time was analyzed according to the Avrami equation [eq. (2)] to

calculate the time required for 10% of amorphous ACTA to crystallize ( $t_{90}$ ).

$$x(t) = \exp(-kt^{n}) \tag{2}$$

where k is the crystallization rate constant, and n is the Avrami index related to the nucleation mechanism and the dimensionality of the growth process.

Amorphous ACTA/polymer solid dispersions were also prepared by melt quenching in a similar manner as amorphous ACTA samples. ACTA and polymer were dissolved in methanol, and the solvent was evaporated in a Teflon vessel by heating at 60°C on a hot-plate. The obtained mixtures were dried under vacuum at 60°C for 16 h, and then melted. Amorphous ACTA/polymer solid dispersions with moisture were prepared by melting and subsequently cooling the moistened mixture, which had been stored at 25°C under various relative humidities (RHs) for more than 72 h, as listed in Table 1. The aluminum pans containing the moistened mixture were crimped hermetically to avoid vaporization of sorbed water during the heating. The  $T_g$  values of the moist amorphous solid dispersions obtained were reproducible, as shown in Table 1.

Amorphous ACTA/polymer dispersions were stored at a constant temperature within the range of  $25-60^{\circ}$ C. The value of x(t) was calculated from  $\Delta C_p$  at  $T_g$ , then  $t_{90}$  was calculated by the curvefitting of the x(t) time profiles in a similar manner as amorphous ACTA.

#### **Enthalpy Relaxation Measurements**

Amorphous ACTA and amorphous ACTA/polymer solid dispersions were prepared in the same

**Table 1.**  $T_{\rm g}$  of Amorphous ACTA/Polymer Dispersions

	$T_{g}$ (°C)					
RH (%)	ACTA/PVP (9:1)	ACTA/PAA (9:1)				
0 (P <sub>2</sub> O <sub>5</sub> )	$30.3 \pm 0.3$	$31.3 \pm 0.5$				
$11  (\text{LiCl} \cdot \text{H}_2\text{O})$	$23.7 \pm 0.1$					
22 (CH <sub>3</sub> COOK)	******	$16.5 \pm 0.4$				
$33  (MgCl_2 \cdot 6H_2O)$	$18.7 \pm 0.1$	$14.2\pm0.5$				
$57 \text{ (NaBr} \cdot 2\text{H}_2\text{O)}$	$13.8\pm0.2$	$11.2\pm0.3$				
76 (NaCl)	$8.7 \pm 0.3$					
86 (KCl)	$3.2\pm0.2$					

RH was controlled with salts described in parentheses. Data are mean  $\pm$  SD (n > 3).

manner as the samples prepared for the measurement of crystallization rates. Samples were then stored for 0-32 h at  $6^{\circ}\mathrm{C}$  and  $10^{\circ}\mathrm{C}$  (approximately  $20^{\circ}\mathrm{C}$  below each  $T_{\mathrm{g}}$ ), respectively. After cooling to approximately  $100^{\circ}\mathrm{C}$  below the  $T_{\mathrm{g}}$ , endothermic recovery was measured for the stored samples with a heating rate of  $20^{\circ}\mathrm{C/min}$ . Crystallization of ACTA was not observed during the enthalpy relaxation measurement.

### **DRS** of Water Absorbed in Polymers

DRS measurement was performed with lyophilized PVP and PAA. Two grams of 5-10% polymer solutions were frozen in polypropylene sample tubes (20-mm diameter) by immersion in liquid nitrogen for 10 min, and then dried at a vacuum level <5 Pa for 23.3 h in a lyophilizer (Freezvac 1CFS, Tozai Tsusho Co.). The shelf temperature was -40°C for the first hour, 20°C for the subsequent 19 h, and 35°C for the last 3.3 h. The lyophilized polymers were moistened in desiccators with a saturated salt solution (Tables 2 and 3) for >72 h, then the DRS was measured at frequencies between  $10^7$  and  $10^{10}$  Hz at  $25^{\circ}\text{C}$  by the time domain reflectometry method developed by Mashimo et al.<sup>6-9</sup> using a digitizing oscilloscope (54120B, Hewlett Packard). Complex permittivity was calculated using the software developed by Mashimo et al. <sup>6-9</sup> The water content of the samples was determined by the Karl Fischer method (Metrohm E684).

### **RESULTS**

### Nonisothermal Crystallization of Amorphous ACTA and ACTA/Polymer Dispersions

The melting temperature  $(T_{\rm m})$  of the ACTA crystal used was 167°C (Fig. 1a). Amorphous ACTA prepared by melt quenching showed a  $T_{\rm g}$  at 26°C

(inflection point), an exothermic peak at approximately 90°C, and a melting endothermic peak at 155°C (Fig. 1b). These values of  $T_{\rm m}$  and  $T_{\rm g}$  were in agreement with data in the literature.

A single  $T_{\rm g}$  was observed in the amorphous solid dispersions prepared with PVP (Fig. 1c,d) or PAA (Fig. 1e,f,g), indicating complete miscibility of drug and polymer within the sensitivity limit of the differential scanning calorimetry (DSC) method. The exothermic crystallization peak observed for the ACTA/PAA dispersion disappeared in the presence of 5% PAA, whereas the ACTA/PVP solid dispersion showed an exothermic peak even in the presence of 10% PVP (at a heating rate of  $20^{\circ}\text{C/min}$ ).

### Isothermal Crystallization of Amorphous ACTA and ACTA/Polymer Dispersions

Figure 2 shows typical DSC thermograms of amorphous ACTA stored at 40°C. Three polymorphic forms have been reported for ACTA: form I with  $T_{\rm m}$  at 168–169°C (stable form), form II with  $T_{\mathrm{m}}$  at 157–158°C (metastable form), and form III which is unstable and easily transforms into form II at approximately 125°C.  $^{10-12}$  The  $T_{\rm m}$  of the ACTA sample stored at 40°C was 155°C, indicating that form II was formed. Similarly, the ACTA sample containing 10% PVP exhibited a  $T_{\rm m}$  of 154°C corresponding to form II after storage at 40°C (data not shown). However, the amorphous solid dispersions containing 10% PAA exhibited two exothermic peaks (at approximately 100 and 150°C, respectively) and two endothermic melting peaks (127 and 163°C) after a sufficient period of isothermal storage, suggesting that forms III and I were formed. Decreases in both  $\Delta C_p$  at  $T_g$  and exothermic peak at the crystallization temperature indicate that crystallization occurred during storage. The crystallization rate was determined from the changes in  $\Delta C_p$  at  $T_g$ , and not from the

Table 2. Dielectric Relaxation Parameters for Water in PVP at 25°C

	Water	Jatan	Low-frequency Process			High-frequency Process			
	(g/g polymer)	d (g/mL)	$\Delta\epsilon_l$	α	$\log \tau_l$	$\Delta \epsilon_{ m h}$	β	$\log \tau_h$	$\epsilon_{\infty}$
0.33 (MgCl <sub>2</sub> ·6H <sub>2</sub> O)	0.13	1.18	0.24	1.0	-8.9	0.53	1.0	-9.5	1.9
$0.43  (\mathrm{K_2CO_3 \cdot 2H_2O})$	0.18	1.17	0.29	1.0	-8.8	0.63	1.0	-9.5	2.0
$0.57  (\mathrm{NaBr} \cdot 2\mathrm{H}_2\mathrm{O})$	0.25	1.16	0.54	0.76	-8.7	1.3	1.0	-9.7	2.2
0.76 (NaCl)	0.38	1.14	2.1	0.59	-8.8	5.3	0.92	-9.7	3.5
0.86 (KCl)	0.50	1.13	4.6	0.24	-8.6	11	0.86	-9.8	3.8
0.98 (K <sub>2</sub> SO <sub>4</sub> )	0.82	1.11	7.0	0.25	-8.5	19	0.85	-10	3.6

RH was controlled with salts described in parentheses.

Table 3. Dielectric Relaxation Parameters for Water in PPA at 25°C

p/p <sub>0</sub>	Water	d (g/mL)	Low-frequency Process			High-frequency Process			
	(g/g polymer)		$\Delta \epsilon_{l}$	α	$\log \tau_l$	$\Delta \epsilon_{ m h}$	β	$\log \tau_h$	$\epsilon_{\infty}$
$0.43  (K_2 CO_3 \cdot 2H_2 O)$	0.09	1.18	0.66	1.0	-8.6	0.53	1.0	-9.5	1.8
$0.57  (\text{NaBr} \cdot 2\text{H}_2\text{O})$	0.13	1.18	1.0	1.0	-8.4	0.78	1.0	-9.5	2.2
0.76 (NaCl)	0.23	1.16	2.6	0.42	-8.5	2.4	0.79	-9.7	4.0
0.86 (KCl)	0.36	1.15	4.4	0.36	-8.6	5.0	0.57	-9.7	4.3
$0.98  (\mathrm{K_2SO_4})$	0.83	1.11	11	0.25	-8.7	14	0.49	-9.9	5.2

RH was controlled with salts described in parentheses.

heat of crystallization, because no crystallization exothermic peak was observed for the ACTA/PAA dispersion with higher contents of polymer (Fig. 1g).

Figure 3 shows the typical time profiles of ACTA crystallization in amorphous ACTA and amorphous dispersions of ACTA/PVP and ACTA/PAA. The profiles were analyzed according to the Avrami equation [eq. (2)]. All profiles obtained could be fitted with n=3. Because the  $T_g$  of the moist solid dispersions was lowered with increasing extent of crystallization, the  $t_{90}$  was calculated by fitting the data showing x(t) < 0.3.

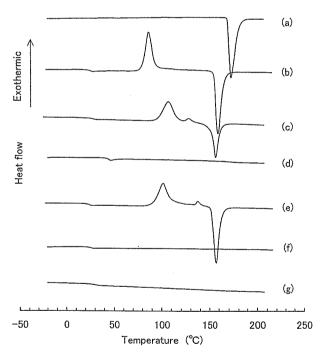
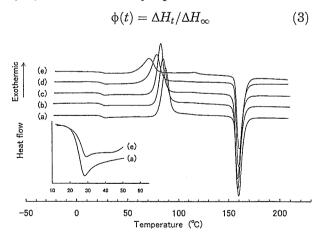


Figure 1. DSC thermograms for ACTA and ACTA/polymer dispersions. (a) ACTA crystal; (b) amorphous ACTA; (c) ACTA/PVP (9:1) dispersion; (d) ACTA/PVP (3:1) dispersion; (e) ACTA/PAA (199:1) dispersion; (f) ACTA/PAA (19:1) dispersion; (g) ACTA/PAA (9:1) dispersion.

Figure 4 shows the  $t_{90}$  versus  $(T_{\rm exp}-T_{\rm g})$  plots according to the Williams-Landel-Ferry equation  $^{13}$   $(T_{\rm exp}$  is the storage temperature). The amorphous solid dispersions with PVP and PAA exhibited a substantially larger  $t_{90}$  than the amorphous ACTA in the dry state (Fig. 4A). Addition of a greater amount of PVP and PAA increased the  $t_{90}$  of the solid dispersions. PAA increased  $t_{90}$  more effectively than PVP at the same polymer mass ratio. The  $t_{90}$  of the solid dispersions was decreased by the presence of moisture (Fig. 4B). The  $(T_{\rm exp}-T_{\rm g})$  dependence of  $t_{90}$  for the ACTA/PAA dispersion obtained under a constant RH at various  $T_{\rm exp}$ 's was different from that obtained under various RHs at a constant  $T_{\rm exp}$ .

### **Enthalpy Relaxation of Amorphous** ACTA/Polymer Dispersions

Figure 5 shows the enthalpy relaxation behavior of amorphous ACTA and ACTA/polymer solid dispersions observed at a temperature 20°C lower than the  $T_{\rm g}$ . The fraction of glass relaxed at time t,  $\phi(t)$ , was calculated by eq. (3):



**Figure 2.** Typical thermograms of amorphous ACTA stored at 40°C for 0 h (a), 1 h (b), 6 h (c), 13 h (d), and 17 h (e).

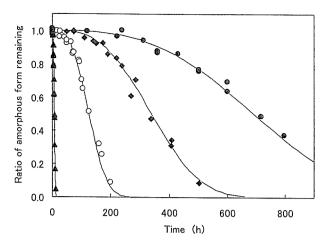


Figure 3. Ratio of the amorphous form remaining in ACTA alone and ACTA/polymer dispersions in the dry state at 40°C. (♠) ACTA, (♠) ACTA/PVP (9:1); (♠) ACTA/PAA (14:1). Solid lines denote the fitting to the Avrami equation.

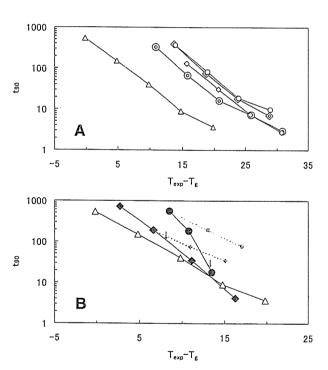
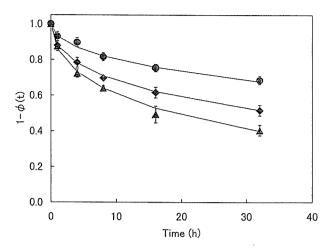


Figure 4.  $t_{90}$  obtained in the dry state at various storage temperatures  $(T_{\rm exp})$  (A) and in the moistened conditions (B). (△) dry ACTA; (♦) dry ACTA/PVP (6:1); (♦) dry ACTA/PVP (9:1); (○) dry ACTA/PAA (9:1); (⊚) dry ACTA/PAA (14:1); (♦) ACTA/PVP (9:1) under 11, 33, 57, and 76% RH at 25°C; (♠) ACTA/PAA (9:1) under 22, 33, and 57% RH at 25°C; (♠) ACTA/PVP (9:1) under 33% RH at 25, 30, and 35°C; (♠) ACTA/PAA-25 (9:1) under 22% RH at 25, 30, and 35°C. Arrows indicate the  $(T_{\rm exp}-T_{\rm g})$  at which water content corresponds to the saturation of tightly binding sites.



**Figure 5.** Enthalpy relaxation behavior of amorphous ACTA and ACTA/polymer dispersions. ( $\blacktriangle$ ) ACTA; ( $\spadesuit$ ) ACTA/PVP (9:1); ( $\spadesuit$ ) ACTA/PAA (9:1). Amorphous ACTA and ACTA/polymer dispersions were stored at 6 and 10°C, respectively. The error bars represent standard deviation (n > 3). The lines indicate the fitting to the Kohlrausch-Williams-Watts equation.

where  $\Delta H_t$  is the enthalpy recovery at time t, and  $\Delta H_{\infty}$  is the maximum enthalpy recovery calculated from  $\Delta C_p$  according to eq. (4):

$$\Delta H_{\infty} = \Delta C_p \times (T_g - T_a) \tag{4}$$

where  $T_{\rm a}$  is the aging temperature. The  $T_{\rm g}$  and  $\Delta C_p$  values observed for the sample before storage were used to calculate the  $\Delta H_{\infty}$  value. The average relaxation times,  $\tau$ , calculated according to the Kohlrausch-Williams-Watts equation [eq. (5)]<sup>14,15</sup> for ACTA, ACTA/PVP (9:1), and ACTA/PAA (9:1) dispersions were 47 h, 84 h, and 247 h, respectively, with a  $\beta$  value of 0.48.

$$1 - \phi(t) = \exp[(-t/\tau)^{\beta}] \tag{5}$$

where  $\beta$  is a parameter representing distribution of the relaxation time.

### Physical Properties of Absorbed Water in Polymers Determined by DRS

Dielectric relaxation spectra of absorbed water have been described by a sum of two or more relaxation processes. <sup>7-9,16,17</sup> The dielectric relaxation spectra obtained for the lyophilized PVP and PAA with various water contents could be analyzed according to eq. (6) assuming two relaxation processes,

$$\epsilon^* = \epsilon_{\infty} + \Delta \epsilon_l / (1 + j \omega \tau_l)^{\alpha_l} + \Delta \epsilon_h / \left(1 + j \omega \tau_h^{\beta_h}\right) \quad (6)$$

where  $\epsilon^*$  is the complex permittivity,  $\epsilon_\infty$  is the limiting high-frequency permittivity, Δε is the relaxation strength,  $\tau$  is the relaxation time, and  $\alpha$ and β are parameters representing the distribution of relaxation times. Subscripts 1 and h represent water with low (----) and high (----) mobility, respectively. Figure 6 shows the analyzed spectra of the lyophilized PVP and PAA preequilibrated at 76% RH. Tables 2 and 3 show the parameters obtained for PVP and PAA, respectively, at various RH values. The lowfrequency process can be attributed to the relaxation of water molecules tightly binding with polymers, because  $\tau_1$  seemed constant regardless of the water content, and similar to that in references. 7-9,16,17 In contrast, the relaxation peak shown in the high-frequency region is considered to be due to the relaxation of water molecules that weakly interact with polymers, because the  $\tau_h$  value was smaller than that of bulk water. These parameters obtained for PVP in the high water content region were similar to those reported for a PVP-water solution system.7 Shinyashiki et al.9 calculated the number of water molecules corresponding to the saturation of tightly binding sites  $(n_1)$  in a collagen-water system from the parameters,  $\Delta \varepsilon_h$  and  $\Delta \varepsilon_l$ , obtained by DRS under the assumption that the ratio of  $\Delta \epsilon_h$  to  $\Delta \epsilon_l$  approximates the ratio of the

amount of water with high mobility to that with low mobility. They measured the values of density needed for the calculation. According to this method, the  $n_1$  of the lyophilized PVP and PAA was calculated. The density of the samples with various water contents used in the calculation was obtained from the fraction of polymer and its assumed value of density (1.2 g/mL). PVP exhibited an  $n_1$  value of 0.5 per monomer unit, which was larger than that obtained for PAA (0.3), indicating that PVP has a greater number of tightly binding sites in the monomer unit.

### **DISCUSSION**

The inhibition effect of a small amount of PVP against crystallization of amorphous sucrose and indomethacin was attributed to the antiplasticization effect of PVP and interaction between PVP and sucrose or indomethacin by Matsumoto and Zografi<sup>2</sup> and Shamblin and Zografi.<sup>3,15</sup> The antiplasticization effect of PVP was confirmed by the finding that the enthalpy relaxation time was prolonged by the presence of PVP. Interaction between PVP and sucrose/indomethacin was confirmed by infrared and Fourier transform-Raman spectroscopy. The authors concluded that formation of indomethacin dimer, which is required for

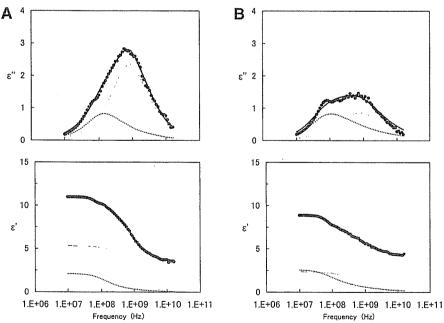


Figure 6. Dielectric absorption  $\epsilon''$  (upper) and dispersion  $\epsilon'$  (lower) spectra observed for PVP (A) and PAA (B) at 25°C, 76% RH. (a) experimental data; (----) relaxation curve for water with low mobility; (—) relaxation curve for water with high mobility; (—) summation of both curves and  $\epsilon_{\infty}$ .

nucleation and crystal growth, was inhibited by interaction between PVP and indomethacin. The present study showed that the enthalpy relaxation time of amorphous ACTA was also prolonged by the presence of PVP and PAA (Fig. 5), indicating the decreased molecular mobility of the amorphous ACTA/PVP and ACTA/PAA dispersions in a similar manner as reported for PVP/sucrose and PVP/indomethacin dispersions. Hydrogen bonding between the hydroxyl group and the carbonyl group or amino group of ACTA, which has been reported for ACTA crystals,12 suggests that the inhibition effect of PVP and PAA against ACTA crystallization can be attributed to the ability of polymers to prevent the association of ACTA molecules in a similar manner as reported for PVP/indomethacin dispersions.<sup>2</sup>

PAA inhibited the crystallization of ACTA more effectively than PVP in the dry state. Nonisothermal crystallization during DSC measurements was not observed in the ACTA/PAA dispersion, but in the ACTA/PVP dispersion with a similar  $T_{\rm g}$ value (Fig. 1c and g). Furthermore, the ACTA/PAA dispersion exhibited a larger  $t_{90}$  of isothermal crystallization than the ACTA/PVP dispersion in the temperature range of 45-60°C (Fig. 4A). This stronger stabilizing effect of PAA may be attributed to the larger decrease in molecular mobility. The amorphous dispersions of ACTA/PAA (9:1) and ACTA/PVP (9:1) exhibited about 5 and 2 times longer relaxation time than ACTA alone, respectively, indicating that PAA decreased the molecular mobility of the dispersions more effectively than PVP. The stronger stabilizing effect of PAA may also be due to the stronger interaction between the hydroxyl group of ACTA and the carboxyl group of PAA, rather than the carbonyl group of PVP.

The effect of water to enhance crystallization of amorphous solids is well known.  $^{3-5,18}$  Shamblin and Zografi<sup>3</sup> and Zhang and Zografi<sup>18</sup> reported that water enhanced the crystallization of sucrose in PVP/sucrose dispersion by plasticizing the amorphous solids and by decreasing PVP–sucrose interaction. The present study also showed that the inhibition effect of PVP against ACTA crystallization was substantially decreased by a small amount of water. The finding that the  $(T_{\rm exp}-T_{\rm g})$  dependence of  $t_{90}$  obtained at various RHs and a constant temperature (25°C) was different from that obtained at a constant RH and various  $T_{\rm exp}$ 's (Fig. 4B) suggests that water in ACTA/polymer dispersion inhibits the drug-polymer interaction. PAA exhibited a substantial

stabilizing effect in the  $(T_{\rm exp}-T_{\rm g})$  range smaller than the  $(T_{exp}-T_g)$  at which water content corresponded to the saturation of tightly binding sites (indicated by the arrows in Fig. 4B), whereas the stabilizing effect of PVP decreased substantially even in the  $(T_{\rm exp}-T_{\rm g})$  range smaller than that corresponding to the saturation of tightly binding sites. The difference between PVP and PAA cannot be explained by the difference in the strength of the interaction between water and polymers, because the  $\tau_1$  values obtained for PVP and PAA were almost the same (Tables 2 and 3). Therefore, the difference in the strength of drug-polymer interaction may be responsible for the difference in the effect of water on the stabilizing effect of polymers. Further water sorption studies with these solid dispersions seem to be required in a similar manner as those reported for sucrose/PVP and indomethacin/PVP solid dispersions, 3,18,19 in order to discuss the difference in interaction behavior between the ATCA/PVP and ACTA/PAA dispersions.

### **CONCLUSIONS**

The crystallization rate of amorphous ACTA was decreased by co-melting with PAA and PVP. The stabilizing effect of these polymers appeared to be attributed to the decreased average molecular mobility, which was confirmed by the increases in  $T_{\rm g}$  and enthalpy relaxation time. In addition to the decreased molecular mobility, interaction between ACTA and polymers appeared to contribute to the stabilizing effect, as suggested by the finding that the ACTA/PAA dispersion exhibited much slower crystallization than the ACTA/PVP dispersion with a similar  $T_g$  value. This stronger effect of PAA may be attributed to the stronger interaction between the hydroxyl group of ACTA and the carboxyl group of PAA, compared with that between the hydroxyl group of ACTA and the carbonyl group of PVP. This explanation is supported by the finding that a small amount of absorbed water decreased the stabilizing effect of PVP. The ability of PAA to decrease the molecular mobility of the amorphous solid dispersion was also larger than that of PVP, as indicated by the longer enthalpy relaxation time.

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# Temperature- and Glass Transition Temperature-Dependence of Bimolecular Reaction Rates in Lyophilized Formulations Described by the Adam-Gibbs-Vogel Equation

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ABSTRACT: Bimolecular reaction rates in lyophilized aspirin-sulfadiazine formulations containing poly(vinylpyrrolidone), dextran, and isomalto-oligomers of different molecular weights were determined in the presence of various water contents, and their temperature- and glass transition temperature  $(T_g)$ -dependence was compared with that of structural relaxation time (τ calculated according to the Adam-Gibbs-Vogel equation, in order to understand how chemical degradation rates of drugs in lyophilized formulations are affected by molecular mobility. The rate of acetyl transfer in poly-(vinylpyrrolidone) K30 and dextran 40k formulations with a constant  $T_{\rm g}$ , observed at various temperatures, exhibited a temperature dependence similar to that of  $\boldsymbol{\tau}$  at temperatures below  $T_{\rm g}$ . Furthermore, the rates of acetyl transfer and the Maillard reaction in formulations containing α-glucose polymers and oligomers increased, as the  $T_{\rm g}$  of formulations decreased, either associated with decreases in molecular weight of excipient or with increases in water content. The observed  $T_{\rm g}$  dependence was similar to that of  $\tau$  in the range of  $T_{\rm g}$  higher than the experimental temperature. The results suggest a possibility that bimolecular reaction rate at temperatures below  $T_{\rm g}$  can be predicted from that observed at the  $T_{\rm g}$  on the basis of temperature dependence of structural relaxation time in amorphous systems, if the degradation rate is proportional to the diffusion rate of reacting compounds. © 2004 Wiley-Liss, Inc. and the American Pharmacists Association J Pharm Sci 93:1062-1069, 2004

**Keywords:** acetyl transfer; lyophilized formulation; glass transition temperature; molecular mobility

### **INTRODUCTION**

The ways in which chemical degradation rates of drugs in lyophilized formulations are affected by molecular mobility largely depend on the degradation mechanism.  $^{1-4}$  Degradation involving translational or rotational motion of the entire molecule is strongly affected by changes in molecular mobility around the glass transition temperature  $(T_{\rm g})$ , whereas the effect of change in molecular mobility is small for degradation that

involves localized motion of specific portions of the molecule. In general, degradation involving bimolecular reactions that require translational motion is largely affected by molecular mobility. Acetyl transfer between aspirin and sulfadiazine in lyophilized formulations containing dextran exhibits a distinct break in temperature dependence, resulting from changes in the translational mobility of the molecules due to glass transition.<sup>5</sup> However, hydrolysis of cephalothin in lyophilized dextran formulations, which is a bimolecular reaction between cephalothin and water, is not significantly affected by changes in molecular mobility, because the diffusion barrier of water molecules is smaller than the activational barrier of hydrolysis.5

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The effect of molecular mobility on chemical degradation rates in the amorphous state can be quantitatively evaluated by comparing degradation rates with structural relaxation time  $\tau$ , which is a useful parameter for indicating molecular mobility. The temperature dependence of  $\tau$  at temperatures above and below  $T_{\rm g}$  can be described by the Vogel-Tammann-Fulcher (VTF, eq. 1) and Adam-Gibbs-Vogel (AGV, eq. 2) equations, respectively. <sup>6–8</sup>

$$\tau(T) = \tau_0 \exp\left(\frac{DT_0}{T - T_0}\right) \tag{1}$$

$$\tau(T,T_{\rm f}) = \tau_0 \exp\biggl(\frac{DT_0}{T-(T/T_{\rm f})T_0}\biggr) \eqno(2)$$

where  $\tau_0$  is relaxation time at the high temperature limit, and  $T_f$  is fictive temperature. D and  $T_0$  are related to the fragility parameter m according to eqs. 3 and 4, respectively.

$$D = 2.303(m_{\min})^2 / (m - m_{\min}) \tag{3}$$

$$T_0 = T_g(1 - m_{\min}/m) \tag{4}$$

 $m_{\rm min}$  is equal to  $\log(\tau_{T_g}/\tau_0)$ , where  $\tau_{T_g}$  is relaxation time at  $T_g$ . Comparison of  $\tau$  and degradation rates has been reported only for chemical degradation of amorphous quinapril hydrochloride<sup>9</sup> and crystallization of amorphous nifedipine. Turther quantitative studies with other amorphous systems are required in order to improve our general understanding of the ways in which chemical degradation rates are affected by molecular mobility.

This article describes the relationship between the temperature dependence of structural relaxation time and that of bimolecular reaction rates in lyophilized aspirin-sulfadiazine formulations containing poly(vinylpyrrolidone) (PVP), dextran, and isomalto-oligomers. The  $T_{\rm g}$  of these formulations was controlled by changing the molecular weights of excipient and water contents. Acetyl transfer reaction between aspirin and sulfadiazine, as well as the Maillard reaction between sulfadiazine and the terminal  $\alpha$ -glucose unit of oligomers were chosen as bimolecular reaction models.

#### **EXPERIMENTAL**

### Materials

Dextran 40k, dextran 10k, PVP K90, and sulfadiazine were purchased from Sigma Chemical Co. (St. Louis, MO). PVP K30, isomalto-oligomer

(090-03485), aspirin (015-10262), salicylic acid (199-00142), and 4-hydroxybenzoic acid (084-04102) were provided by Wako Pure Chemical Industries Ltd. (Osaka, Japan). Isomalto-oligomer was dialyzed against distilled water using a membrane with a pore size of 2000 molecular weight cutoff (Spectrum Laboratories, Inc., Laguna Hills, CA), frozen by immersion in liquid nitrogen, and then dried in a vacuum of <5 Pa for 23.5 h in a lyophilizer (Freezevac C-1; Tozai Tsusho Co., Tokyo, Japan). Shelf temperature was between -35° and -30°C for the first 1 h, 20°C for the subsequent 19 h, and 30°C for the last 3.5 h. Isomalto-oligomer as received is hereafter referred to as isomalto-oligomer A, whereas that after dialysis and freeze-drying is isomaltooligomer B. Freeze-drying of isomalto-oligomer A and B yielded cakes with  $T_{\rm g}$  values of 100° and 152°C, respectively.

### Preparation of Lyophilized Formulations

A 19.5-g portion of aspirin solution (0.0924% w/w) was added to 20.5 g of sulfadiazine and PVP K30 solution [5 mg of sulfadiazine and 250 mg of PVP K30 (or PVP K90) in 19.5 g of distilled water] to give a final ratio of sulfadiazine/aspirin/PVP K30 (or PVP K90) of 1:3.6:50 w/w. The molecular ratio of sulfadiazine to aspirin was 1:5. Three hundred microliters of these solutions was frozen in polypropylene sample tubes (10-mm diameter) by immersion in liquid nitrogen for 10 min, then dried in a lyophilizer as described above. The solutions before freeze-drying were prepared under ice-cooled conditions to inhibit the hydrolysis of aspirin.

Lyophilized formulations containing dextran 40k, dextran 10k, isomalto-oligomer A, and isomalto-oligomer B were prepared from a sulfadiazine-aspirin-excipient solution (1:3.6:200 w/w). A larger ratio of excipient than that for PVP series formulations was used in order to decrease the reaction rate that is larger than that in PVP series formulations at the same ratio.

Lyophilized formulations with various water contents were obtained by storing at 15°C for 24 h in a desiccator with a saturated solution of LiCl  $\rm H_2O$  [12% relative humidity (RH)], potassium acetate (23% RH), MgCl<sub>2</sub> 6H<sub>2</sub>O (33% RH),  $\rm K_2CO_3$  2H<sub>2</sub>O (43% RH), Ca(NO<sub>3</sub>)<sub>2</sub> 4H<sub>2</sub>O (55% RH), NaBr 2H<sub>2</sub>O (60% RH), or NaCl (75% RH). Obtained formulations showed the  $T_{\rm g}$  values listed in Table 1, depending on the humidity conditions.

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Relative humidity (%)	12	23	33	43	55	60	75
Isomalto-olygomer A	70	50	39	31	6		
Isomalto-olygomer B	83	72	58	44	37		
Dextran 10k	_	98	79	68	45	44	
Dextran 40k		_	89	72	57	50	
PVP K30	112	85	66	58	45	34	9
PVP K90		81	72	58	41	41	7

**Table 1.**  $T_g$  of Lyophilized Formulations with Water Contents Adjusted at Various Humidities (°C)

### **Determination of Degradation Rate**

Lyophilized sulfadiazine-aspirin-PVP K30 formulations with  $T_{\rm g}$  values of 112°C and 58°C were stored at temperatures ranging from 20° to 60°C ( $\pm 0.1$ °C) after capped tightly with a screw-cap in order to prevent water elimination. The samples were removed at appropriate intervals to determine the amount of remaining sulfadiazine and aspirin.

Samples were dissolved in 1 mL of 50 mM phosphate buffer (pH 2.5), and 0.7 mL of methanol containing 4-hydroxybenzoic acid as an internal standard was added in the solution. The solution was injected into an high-performance liquid chromatography system consisting of a Shimadzu LC-10AD VP pump (Kyoto, Japan), a Shimadzu variable-wavelength UV detector (SDD-M10A), and a Shimadzu CLASS-VP data system. A Tosoh AS-8010 autoinjector (Tokyo, Japan) delivered 20-μL samples. The sulfadiazine, aspirin, salicylic acid, and acetyl sulfadiazine were separated on a reversed-phase column (Inertsil ODS-3,  $4.6 \, \mathrm{mm} \times$ 150 mm; GL Science Inc., Tokyo, Japan) maintained at 35°C. The detection wavelength was 200 nm. The mobile phase was a mixture of 50 mM phosphate buffer (pH 2.5) and methanol (3:2).

As previously reported,<sup>5</sup> the rate constant of acetyl transfer  $(k_{\rm T})$  and the pseudo-rate constant of hydrolysis  $(k_{\rm H,pseudo})$  were determined by curvefitting of the amount of remaining sulfadiazine [SD] and aspirin [ASA] to the following equations (only the initial data points representing <10% reaction were used for the fitting to minimize the effects of salicylic acid and acetic acid formation).

$$d[SD]/dt = -k_T[SD][ASA]$$
  
 $d[ASA]/dt = -k_T[SD][ASA] - k_{H,pseudo}[ASA]$ 

The time required for 10% acetyl transfer ( $t_{90}$ ) was calculated from the obtained  $k_{\rm T}$  value.

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Lyophilized sulfadiazine-aspirin formulations containing dextran 10k and 40k, isomaltooligomer A and B, and PVP K30 and K90 with various  $T_{\rm g}$  values were stored at 60°C. The samples were removed at appropriate intervals to determine the amount of remaining sulfadiazine by using the high-performance liquid chromatography system described above. Apparent first-order rate constant for decreases in the amount of sulfadiazine was determined by curve-fitting to calculate time required for 10% degradation ( $t_{90}$ ).

### Determination of $T_g$ by Differential Scanning Calorimetry

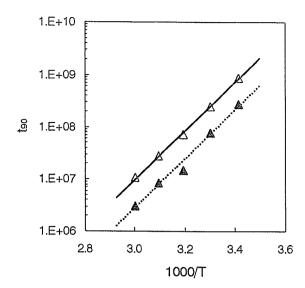
Lyophilized formulations with various water contents adjusted by storing at 15°C under various humidity conditions were put in a hermetic pan. Thermograms were obtained in the temperature range from 40°C lower than the  $T_{\rm g}$  to 40°C higher than the  $T_{\rm g}$  at a scan rate of 20°C/min by differential scanning calorimetry (2920; TA Instruments, New Castle, DE). Temperature calibration was performed using indium.

### **RESULTS**

### Effect of Temperature on $t_{90}$ for Acetyl Transfer in Lyophilized Formulation with a Constant $T_g$

Sulfadiazine and aspirin underwent acetyl transfer in the lyophilized formulation containing PVP K30 in a similar manner as reported for lyophilized formulations containing dextran and methylcellulose. Figure 1 shows the temperature dependence of  $t_{90}$  for acetyl transfer calculated from  $k_{\rm T}$  values observed for PVP K30 formulations with  $T_{\rm g}$  values of 112° and 58°C. A linear temperature dependence of  $t_{90}$  was observed at

<sup>-,</sup> Not determined.



**Figure 1.** Temperature dependence of  $t_{90}$  for acetyl transfer in lyophilized PVP K30 formulations with constant  $T_{\rm g}$  values of 58°C ( $\triangle$ ) and 112°C ( $\triangle$ ).

temperatures substantially lower than the  $T_{\rm g}$  (20–60°C for  $T_{\rm g}$  of 112°C), but there seemed to be a small deviation from the linear line around a temperature approximately 20°C lower than the  $T_{\rm g}$  (35°C for  $T_{\rm g}$  of 58°C).

## Effect of Molecular Weight of Excipient and Water Content on t<sub>90</sub> for Acetyl Transfer and the Maillard Reaction in Lyophilized Formulation

Sulfadiazine underwent only acetyl transfer in the lyophilized sulfadiazine-aspirin formulations containing PVP and dextran, whereas in the lyophilized formulations containing isomaltooligomers A and B, it underwent the Maillard reaction with the terminal α-glucose unit of oligomer chain in addition to acetyl-transfer reaction with aspirin. Initial decreases in sulfadiazine observed during storage of these formulations were describable with first-order kinetics. The time courses of degradation in isomaltooligomer B formulation are shown as examples in Figure 2. The apparent first-order rate constant determined from the initial slope corresponded to the rate constant of acetyl transfer for the PVP K90, K30, dextran 40k, and 10k formulations, whereas it corresponded to the overall rate constant including acetyl transfer and the Maillard reactions for the isomalto-oligomer A and B formulations.

Figure 3 shows the  $t_{90}$  calculated from the apparent first-order rate constant observed at a

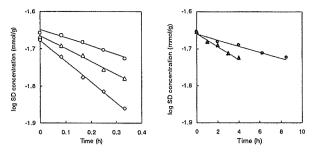
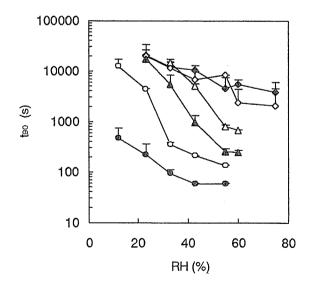


Figure 2. Decrease in the amount of sulfadiazine remaining at 60°C in lyophilized isomalto-oligomer B formulation with  $T_{\rm g}$  values of 83°C (♠), 72°C (♠), 59°C (○), 44°C (△), and 37°C (♦).

constant temperature of  $60^{\circ}$ C in the formulations containing various molecular weights of excipient, plotted against the humidity at which the water content of formulations was adjusted. Significant differences in  $t_{90}$  between different molecular weights of excipients were not observed for the PVP series (PVP K30 and K90) formulations, but for the  $\alpha$ -glucose series (isomalto-oligomers A and B, and dextrans  $10^{\circ}$ k and  $40^{\circ}$ k) formulations. The  $t_{90}$  of the latter formulations was decreased by decreases in the molecular weight of excipient and by increases in humidity (i.e., increases in water content). A rapid change in  $t_{90}$  was observed at a lower humidity, as the molecular weight of excipient decreased. Figure 4 shows the  $t_{90}$  plotted



**Figure 3.** Effect of water content (humidity at which water content was adjusted) on the  $t_{90}$  observed at 60°C with lyophilized isomalto-oligomer A ( ) and B (), dextran 10k ( ) and 40k (), and PVP 30 () and PVP 90 () formulations. SD (n=3).

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(eq. 1). The  $\tau$  value calculated using an m value of 70 according to the VTF equation is just an approximation, because it depended largely on the m value used for the calculation. The temperature dependence of  $t_{90}$  for acetyl transfer in these formulations containing PVP K30 and dextran 40k was similar to that of  $\tau$  calculated based on the AGV equation at temperatures below  $T_{\rm g}$ , although  $t_{90}$  values at temperatures far from  $T_{\rm g}$  tended to diverge from the line.

The similarity of temperature dependence between  $t_{90}$  and  $\tau$  at temperatures below  $T_{\rm g}$  suggests that  $t_{90}$  for acetyl transfer is related to the molecular mobility of lyophilized formulations. In other words, the rate of acetyl transfer is suggested to be proportional to the diffusion rates of the molecules, as reported for the chemical degradation of quinapril hydrochloride.<sup>9</sup>

As reported previously,<sup>5</sup> the temperature dependence of the acetyl-transfer rate in the lyophilized dextran 40k formulation exhibited a break around a temperature approximately 15°C lower than the  $T_{\rm g}$ , namely  $T_{\rm mc}$  at which glass transition began to be detected by nuclear magnetic resonance relaxation measurements.<sup>13</sup> This break is inconspicuous in Figure 5, in which the y-axis is reduced. Similarly, a small divergence from linearity observed in the temperature dependence of  $t_{90}$  for acetyl transfer in the PVP K30 formulation with a  $T_{\rm g}$  of 58°C (Fig. 1) becomes inconspicuous in Figure 5.

## Dependence of $t_{90}$ for Acetyl Transfer and the Maillard Reaction on the $T_{\rm g}$ Controlled by Changing the Molecular Weight of Excipient and Water Content

The  $t_{90}$  for the  $\alpha$ -glucose series formulations tended to decrease as the molecular weight of excipient decreased, when compared at a same value of  $(T - T_g)$  (Fig. 4). These differences in  $t_{90}$ between different molecular weights can be explained by the Maillard reaction, which occurred along with acetyl transfer in α-glucose series formulations. Increases in the number of the reacting compound for the Maillard reaction (i.e., terminal  $\alpha$ -glucose unit) resulted in the decreases in  $t_{90}$ . Both acetyl transfer and the Maillard reaction are expected to be molecular mobility-controlled intermolecular reactions. The  $t_{90}$  of each of the  $\alpha$ -glucose series formulations exhibited a rapid decrease when  $T_g$  approached to the experimental temperature in association with increases in water content (Fig. 4).

To compare the  $t_{90}$  versus  $T_{\rm g}$  relationship between formulations containing different molecular weights of excipients (i.e., different numbers of terminal  $\alpha$ -glucose), the  $t_{90}$  for sulfadiazine degradation in the  $\alpha$ -glucose series formulations was scaled to the  $t_{90}$  value at a point at which  $T_{\rm g}$  is equivalent to the experimental temperature, and is plotted against the  $T_{\rm g}$  value scaled to the experimental temperature in Figure 6. Plots for the PVP series formulations are also included in Figure 6. Figure 6 also shows the  $T_{\rm g}$  dependence of  $\tau$  calculated based on the AGV equation (eq. 2) by assuming that  $\xi=1$ ,  $T_{\rm f}=T_{\rm g}$ , and m=70.

The  $t_{90}$  for sulfadiazine degradation in the  $\alpha$ -glucose series formulations with different  $T_{\rm g}$ values depending on the molecular weight and water content exhibited a similar pattern of  $T_{\rm g}$ dependence to that of  $\tau$  calculated based on the AGV equation in the range of  $T_g$  higher than the experimental temperature, although larger variations were observed compared with Figure 5. This finding indicates that molecular mobility is one of the primary factors that determine the degradation rate. Increases in water content can possibly affect the degradation rate not only by varying the  $T_g$  of formulations, but also by acting as a reacting compound. However, it has been reported that water is involved in the rate-determining process for neither acetyl-transfer reaction 14 nor the Maillard reaction. 15

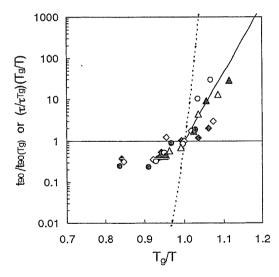


Figure 6. Comparison of the  $T_{\rm g}$  dependence of  $t_{90}$  observed at a constant temperature of 60°C in isomaltooligomer A ( $\textcircled{\bullet}$ ) and B ( $\textcircled{\circ}$ ), dextran 10k ( $\textcircled{\blacktriangle}$ ) and 40k ( $\textcircled{\circ}$ ), and PVP 30 ( $\textcircled{\circ}$ ) and PVP 90 ( $\textcircled{\bullet}$ ) formulations with that for structural relaxation time  $\tau$  calculated according to the AGV equation (solid line) and VTF equation (broken line).

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The  $t_{90}$  for sulfadiazine degradation in the PVP series formulations was much larger than that in the  $\alpha$ -glucose series formulations (Fig. 4). This difference in  $t_{90}$  may be attributed to the difference in the type and extent of interaction between the reacting compounds and excipient. The finding that the  $t_{90}$  for sulfadiazine degradation in the PVP series formulations diverged from the  $\tau$  calculated based on the AGV equation (Fig. 6) also suggests that the effect of PVP on the reaction rate is different from that of  $\alpha$ -glucose series excipients. This may be explained by assuming that the mobility of reacting compounds in the PVP formulations becomes different from that of the whole formulation determined by τ, when formulations have higher  $T_g$  values that resulted from lower water contents. This explanation is supported by the finding that the temperature dependence of  $t_{90}$ observed for the PVP formulation with a constant water content tended to diverge from the line at temperatures far from  $T_g$  (Fig. 5).

### Temperature Dependence of $t_{90}$ in the Range in Which $T_g$ Is Lower Than Experimental Temperature

In the range in which  $T_g$  is lower than the experimental temperature,  $t_{90}$  exhibited a temperature dependence different from that of  $\tau$ calculated based on the VTF equation. This is the case for both  $t_{90}$  determined at various temperatures for formulations with a constant  $T_{g}$ (Fig. 5) and that determined at a constant temperature for formulations with various  $T_{\rm g}$ values depending on the molecular weight of excipient and water content (Fig. 6). Although the  $\tau$  value calculated by the VTF equation is just an approximation, the slope for  $t_{90}$  can be considered to be much smaller than that for  $\tau$ . These findings suggest that the acetyl-transfer rate in the range in which  $T_g$  is lower than the experimental temperature is not controlled by molecular mobility, but by activational barrier of the reaction. In other words, the diffusion barrier of the molecules is smaller than the activational barrier of the reaction.

### **CONCLUSIONS**

The rate of acetyl transfer, a bimolecular reaction, in lyophilized aspirin-sulfadiazine formulations containing PVP K30 and dextran 40k with a constant  $T_{\rm g}$  exhibited a temperature dependence similar to that of  $\tau$  described by the AGV equation

at temperatures below  $T_{\rm g}$ . Furthermore, the rates of acetyl transfer and the Maillard reaction in the  $\alpha$ -glucose series formulations increased with decreases in the  $T_{\rm g}$  of formulations, either associated with decreases in molecular weight of excipient or with increases in water content, and exhibited a similar  $T_{\rm g}$  dependence to that of  $\tau$  calculated based on the AGV equation in the range of  $T_{\rm g}$  higher than the experimental temperature.

The data obtained using the present model lyophilized formulations suggest a possibility that the rates of bimolecular reactions at temperatures below  $T_{\rm g}$  can be predicted from that determined at  $T_{\rm g}$  on the basis of temperature dependence of structural relaxation time in amorphous systems, if the degradation rate is proportional to the diffusion rate of reacting compounds.

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### Molecular Mobility-Based Estimation of the Crystallization Rates of Amorphous Nifedipine and Phenobarbital in Poly(vinylpyrrolidone) Solid Dispersions

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ABSTRACT: The overall crystallization rates and mean relaxation times of amorphous nifedipine and phenobarbital in the presence of poly(vinylpyrrolidone) (PVP) were determined at various temperatures to gain further insight into the effect of molecular mobility on the crystallization rates of amorphous drugs and the possibility of predicting stability from their molecular mobility. Nifedipine-PVP (9:1 w/w) and phenobarbital-PVP (95:5 w/w) solid dispersions were prepared by melting and rapidly cooling mixtures of each drug and PVP. The amount of amorphous nifedipine remaining in the solid dispersion was calculated from the heat of crystallization, which was obtained by differential scanning calorimetry. The amount of amorphous phenobarbital remaining in the solid dispersion was estimated from the change in the heat capacity at its glass transition temperature  $(T_g)$ . The time required for the amount of amorphous drug remaining to fall to 90% ( $t_{90}$ ) was calculated from the profile of time versus the amount of amorphous drug remaining. The  $t_{90}$  values for the solid dispersions studied were 100-1000 times longer than those of pure amorphous drugs when compared at the same temperature. Enthalpy relaxation of the amorphous drugs in the solid dispersions was reduced compared with that in the pure amorphous drugs, indicating that the molecular mobility of the amorphous drugs is reduced in the presence of PVP. The temperature dependence of mean relaxation time (7) for the nifedipine-PVP solid dispersion was calculated using the Adam – Gibbs – Vogel equation. Parameters D and  $T_0$  in this equation were estimated from the heating rate dependence of  $T_{\rm g}$ . Similar temperature dependence was observed for  $t_{90}$  and  $\tau$  values of the solid dispersion, indicating that the information on the temperature dependence of the molecular mobility, along with the crystallization data obtained at around the  $T_{\rm g}$ , are useful for estimating the  $t_{90}$  of overall crystallization at temperatures below  $T_{\rm g}$  in the presence of excipients. © 2004 Wiley-Liss, Inc. and the American Pharmacists Association J Pharm Sci 93:384-391, 2004

Keywords: crystallization; amorphous; stability; solid dispersion; relaxation time

#### INTRODUCTION

To improve their dissolution rates and bioavailability, poorly soluble drugs are utilized in the amorphous form. However, instability during storage, as evidenced by crystallization, is an issue of

concern with amorphous drugs, and prediction of their stability at room temperature is a matter of great interest. Predicting the stability of amorphous drugs at room temperature from data obtained at higher temperatures is generally considered to be difficult because the temperature dependence of the degradation rate usually differs above and below their glass transition temperatures  $(T_g)$ . However, because the temperature dependence of the degradation rate has been reported to be similar to that of the molecular mobility for

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some amorphous drugs,<sup>1,2</sup> it may be possible to predict their stability based on the temperature dependence of the molecular mobility when the stability is governed by molecular mobility.

The crystallization rate, k, of an amorphous solid at temperature T depends on the rate of molecular diffusion across the nuclear—amorphous matrix interface [D(T)] and the nucleation free energy term [f(T)], according to eq. 1.<sup>3-6</sup>

$$k \propto D(T)f(T)$$
 (1)

In a previous paper,<sup>7</sup> we reported that the temperature dependence of the overall crystallization rates of pure amorphous nifedipine and phenobarbital is similar to that of the mean relaxation time (τ) calculated according to the Adam–Gibbs–Vogel (AGV) equation (eq. 2),<sup>8</sup> which is a measure of molecular mobility.

$$\tau = \tau_0 \exp\left\{\frac{DT_0}{T(1 - T_0/T_f)}\right\}$$
 (2)

where D and  $T_0$  are the Vogel-Tammann–Fulcher (VTF) equation parameters, and  $T_f$  is the fictive temperature. When  $T > T_g$ ,  $T_f = T$  and eq. 2 is identical to the VTF equation. When  $T < T_g$ ,  $T_f$  can be approximated by  $T_g$  for freshly prepared amorphous solid,  $^{11}$  and Arrhenius-type temperature dependence of  $\tau$  is observed at these temperatures. This similarity between crystallization rates and mean relaxation times suggests that the temperature dependence of D(T) is much larger than that of f(T) at temperatures  $< T_g$ , and that the crystallization rate of amorphous drugs may be estimated based on molecular mobility.

It would be of interest to expand the relationship between stability during storage and molecular mobility observed for pure amorphous drug systems to amorphous drug-excipient solid dispersion systems. Excipients have been reported to have an effect on the crystallization rates of some amorphous drugs. 9-17 Excipients stabilize amorphous drugs mainly due to (1) the anti-plasticizing effect of high  $T_{g}$  excipients (which results in an increase in the  $T_{\rm g}$ , and therefore a decrease in the molecular mobility), and (2) specific interactions between the drug and the excipient. If the intensity of the specific interaction does not change to any great extent with the temperature, the crystallization rate of the drug in the solid dispersion can be expected to correlate with its molecular mobility.

In this study, the overall crystallization rates of nifedipine and phenobarbital were determined in the presence of poly(vinylpyrrolidone) (PVP) at temperature ranges above and below their  $T_{\rm g}$ s, and were compared with the temperature dependence of their  $\tau$  values, as obtained from the AGV equation.

### **EXPERIMENTAL**

#### Materials

Crystalline nifedipine was purchased from Sigma (St. Louis, MO) and used as received. Crystalline phenobarbital was prepared from sodium phenobarbital (Wako Pure Chemical Industries, Osaka, Japan) according to a previously described method. 18

### Preparation of Nifedipine- and Phenobarbital-PVP Solid Dispersions

Nifedipine-PVP (9:1 w/w) and phenobarbital-PVP (95:5 w/w) solid dispersions were prepared by melting and rapidly cooling mixtures of each drug and PVP. Because the overall crystallization rate of phenobarbital was slower than that of nifedipine, lower PVP content was used for the phenobarbital solid dispersion to follow the crystallization kinetic under usual temperature conditions (25-80°C) within conventional experimental time periods. Crystalline nifedipine or phenobarbital was dissolved in methanol with PVP at w/w ratios of 9:1 and 95:9, respectively. The methanol was then evaporated off using a rotary evaporator under reduced pressure. The precipitate thus obtained was ground in a mortar, and then dried in a vacuum chamber at ~60°C for 1 day. A portion of the dried precipitate (~4 mg) was sealed into an aluminum sample pan with a pinhole in the lid, heated to ~190°C, cooled to -40°C at a cooling rate of -40°C/min, and reheated to room temperature in a differential scanning calorimeter (DSC; model 2920; TA Instrument, New Castle, DE).

To confirm that the prepared samples were amorphous, some of the prepared samples were opened before storage and examined by polarized light microscopy.

### Determination of the Overall Crystallization Rates of Nifedipine and Phenobarbital in PVP Solid Dispersions

The sample pan containing nifedipine— or phenobarbital—PVP solid dispersion was transferred to

a vessel containing  $P_2O_5$  and stored at a constant temperature (25–80°C). At appropriate intervals, samples were withdrawn, and the heat of crystallization (nifedipine) or the change in the heat capacity at  $T_{\rm g}$  (phenobarbital) was measured. The heat of crystallization was measured at a heating rate of 20°C/min. Heat capacity at constant pressure ( $C_{\rm p}$ ) of the phenobarbital–PVP solid dispersion was also determined using a model 2920 modulated DSC equipped with refrigeration system (TA Instrument, New Castle, DE). The modulated temperature program used applied a modulation amplitude of  $\pm 0.5$ °C within 100 s, and had an underlying heating rate of 1°C/min.

Temperature and cell constant calibration of the instrument was carried out using indium, and the heat capacity was calibrated using sucrose. <sup>2,19</sup> High-performance liquid chromatography (HPLC) analysis of the stored samples showed no evidence of chemical degradation of nifedipine and phenobarbital.

### **Determination of the Enthalpy Relaxation Time**

The solid dispersions prepared by the same method just described were stored at  $25^{\circ}$ C in vessels containing  $P_2O_5$ . At appropriate intervals, samples were withdrawn, and the relaxation enthalpy was measured at a heating rate of  $20^{\circ}$ C/min.

### Heating Rate Dependence of $T_g$

The  $T_{\rm g}$  values of the solid dispersions were measured at heating/cooling rates of 40, 20, 10, or 5°C/min. Samples of nifedipine— or phenobarbital—PVP precipitates ( $\sim$ 4 mg) were heated to  $\sim$ 190°C and cooled to -40°C at rates of 40, 20, 10, or 5°C/min, then reheated at the same rates to 200°C. An aluminum cooling can filled with liquid nitrogen was used for cooling at 40 and 20°C/min. For measurements at heating/cooling rates of 10 and 5°C/min, the calorimeter was equipped with a refrigeration system.

Temperature calibration of the instrument was carried out at each heating rate using indium.

## Calculation of the Relaxation Times of Amorphous Nifedipine and Phenobarbital According to the AGV Equation

The mean relaxation times  $(\tau)$  of the nifedipine—and phenobarbital—PVP solid dispersions were

calculated from the AGV equation (eq. 2; see Introduction).  $^{1,2,8,20,21}$  The parameters D and  $T_0$  in eq. 2 were calculated from the fragility, m, according to eqs. 3-5:

$$D = 2.303 (m_{\min})^2 / (m - m_{\min})$$
 (3)

$$m_{\min} = \log(\tau(T_{\rm g})/\tau_0) \cong \log(100/10^{-14}) = 16$$
 (4)

$$T_0 = T_{\rm g}(1 - m_{\rm min}/m) \tag{5}$$

where  $\tau(T_{\rm g})$  and  $\tau_0$  represent the relaxation times at  $T_{\rm g}$  and at the upper temperature limit, which were assumed to be 100 and  $10^{-14}$  s, respectively. The fragility, m, is defined as a temperature change in the relaxation time at  $T_{\rm g}$  (eq. 6).

$$m = \frac{\mathrm{d}(\log \tau)}{\mathrm{d}(T_{\mathrm{g}}/T)} \qquad T = T_{\mathrm{g}} \tag{6}$$

Equation 6 can be approximated by eq. 7, which uses the activation energy  $(\Delta H^*)$  for viscous flow.

$$m \cong \frac{\Delta H^*}{2.303RT_{\rm g}} \tag{7}$$

The value of  $\Delta H^*$  can be obtained from the scanning rate dependence of  $T_g$  as determined by DSC, as shown in eq. 8:

$$\frac{\Delta H^*}{R} = -\frac{\mathrm{d}(\ln q)}{\mathrm{d}(1/T_g)} \tag{8}$$

where R and q are the gas constant and heating rate, respectively. The fictive temperature,  $T_{\rm f}$ , was assumed to be  $T_{\rm g}$  in temperature ranges  $< T_{\rm g}$ .

### **RESULTS AND DISCUSSION**

### Crystallization of Nifedipine and Phenobarbital in PVP Solid Dispersions

Typical thermograms of a nifedipine–PVP solid dispersion (9:1 w/w) stored at  $70^{\circ}$ C are shown in Figure 1. Glass transition was observed at  $\sim 50^{\circ}$ C, and an exothermic peak attributable to the crystallization of amorphous nifedipine during the DSC heating process was observed at  $\sim 120^{\circ}$ C with a freshly prepared solid dispersion. Two endothermic peaks due to melting of metastable and stable nifedipine crystal were observed at  $\sim 165$  and  $175^{\circ}$ C, respectively, indicating that two polymorphs were formed from the amorphous phase. Relative areas of the melting peak for the two polymorphs did not significantly vary with storage time. Therefore, we assumed that the

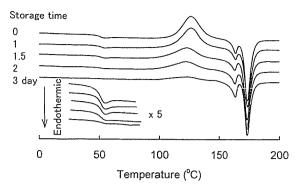


Figure 1. Typical thermograms of a nifedipine-PVP solid dispersion (9:1 w/w) stored at 70°C.

variation of relative amount of two polymorphs with storage time was negligible.

The area under the exothermic peak at  $\sim 120^{\circ}$ C decreased as storage time increased, indicating that amorphous nifedipine crystallizes during storage at 70°C. We assumed that the area under the exothermic peak was proportional to the amount of amorphous nifedipine in the solid dispersion. The amount of amorphous nifedipine remaining [R(t)] was calculated using eq. 9:

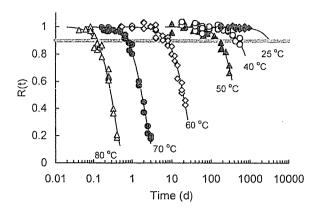
$$R(t) = \Delta H_{\rm c}(t) / \Delta H_{\rm c}(0) \tag{9}$$

where  $\Delta H_{\rm c}(0)$  and  $\Delta H_{\rm c}(t)$  represent the area under the exothermic peak prior to storage and after storage for time t, respectively.

The time profiles of the amount of amorphous nifedipine remaining in the solid dispersion are shown in Figure 2. It has been reported that the crystallization of nifedipine in a 2-hydroxypropyl- $\beta$ -cyclodextrin matrix at temperatures  $>T_g$  can be described by the Avrami–Erofeev equation<sup>16</sup>:

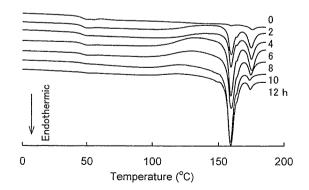
$$\{-\ln(1-\alpha)\}^{1/2} = kt \tag{10}$$

The solid lines in Figure 2 represent the fit to this equation, as calculated by nonlinear regression, and indicate that the profiles of time versus of the amount of amorphous nifedipine remaining at temperatures of 50, 60, 70, and 80°C conform to the equation. It was difficult to determine an appropriate kinetic model from data obtained at lower temperatures because the decrease in the exothermic peak during storage for 2 years was too small. Therefore, we assumed that the same kinetic model could be applied to crystallization at lower temperatures. The time required for the amount of amorphous nifedipine to fall to 90%  $(t_{90})$  was calculated from the rate constant obtained by nonlinear regression as a parameter of the crystallization rate.

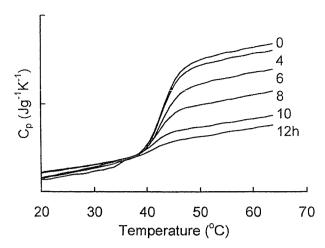


**Figure 2.** Time profiles of the amount of amorphous nifedipine remaining in nifedipine-PVP solid dispersions (9:1 w/w) stored at various temperatures.

Typical thermograms of a phenobarbital-PVP solid dispersion (95:9 w/w) are shown in Figure 3. A freshly prepared phenobarbital-PVP solid dispersion showed small endothermic peaks at  ${\sim}160$ and 175°C. In contrast, a broad exothermic peak appeared at ~130°C with the samples stored at 80°C. This peak initially increased with the storage time, but decreased once the storage time exceeded 6 h. The increase in the exothermic peak suggests that physical changes in solid dispersions may take place during storage at 80°C, and that these changes might induce the crystallization of phenobarbital during the DSC heating process. The decrease in the exothermic peak for samples stored for ≥6 h suggests that crystallization of phenobarbital may occur during storage at 80°C. Endothermic peaks at 160 and 170°C are attributable to the melting of phenobarbital crystals that arose from the amorphous phase during both storage at 80°C and the DSC heating process. These features make it difficult to estimate the amount of amorphous phenobarbital remaining in



**Figure 3.** Typical thermograms of a phenobarbital—PVP solid dispersion (95:5 w/w) stored at 80°C.



**Figure 4.** Changes in the heat capacity at  $T_{\rm g}$  of a phenobarbital-PVP solid dispersion (95:5 w/w) stored at  $80^{\circ}{\rm C}$ 

a solid dispersion from the exothermic peak at 130°C or the endothermic peaks at 160 and 170°C.

Changes in the heat capacity at  $T_{\rm g}$  have been reported to be proportional to the amount of amorphous component in a mixture of an amorphous and a crystal drug. <sup>22</sup> As shown in Figure 4, changes in the heat capacity at  $T_{\rm g}$  ( $\Delta C_{\rm p,Tg}$ ) for the phenobarbital–PVP solid dispersion decreased with the storage time, indicating that  $\Delta C_{\rm p,Tg}$  can be used as a measure of the amount of amorphous phenobarbital remaining.

$$R(t) = \Delta C_{p,Tg}(t) / \Delta C_{p,Tg}(0)$$
 (11)

To confirm the feasibility of using  $\Delta C_{\mathrm{p},T\mathrm{g}}$  as a measure of the amount of amorphous drug remaining during the crystallization process, time profiles of R(t) were calculated for the nifedipine–PVP solid dispersion from  $\Delta C_{\mathrm{p},T\mathrm{g}}$  and  $\Delta H_{\mathrm{c}}$  data. The results are shown in Figure 5. The time profiles of R(t) calculated from  $\Delta C_{\mathrm{p},T\mathrm{g}}$  data were similar to those calculated from  $\Delta H_{\mathrm{c}}$  data, indicating that  $\Delta C_{\mathrm{p},T\mathrm{g}}$  can be used as a measure of the amount of amorphous drug remaining.

The time profiles of R(t) for phenobarbital-PVP solid dispersions stored at various temperatures are shown in Figure 6. The solid lines in the figure represent the fit to eq. 9 by nonlinear regression;  $t_{90}$  was calculated from the rate constant obtained by nonlinear regression.

The solid dispersions studied contained either 10 or 5% w/w of PVP. When crystallization of amorphous nifedipine or phenobarbital in the solid dispersions takes place, PVP is considered to separate from amorphous phase. This separation might affect the  $T_{\rm g}$  of remaining amorphous phase.

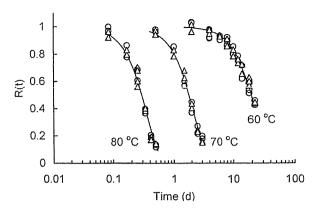
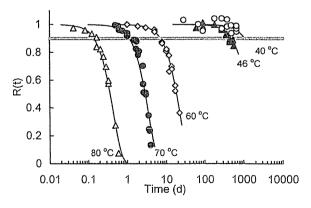


Figure 5. Time profiles of the amount of amorphous nifedipine remaining in nifedipine–PVP solid dispersion (9:1 w/w) stored at various temperatures. Key:  $(\triangle)$  calculated from  $\Delta C_{\rm p}$ ;  $(\bigcirc)$  calculated from  $\Delta H_{\rm c}$ .

The  $T_{\rm g}$  of the solid dispersions, however, did not show any tendency to increase or decrease during storage at temperatures above their  $T_{\rm g}$ , as shown in Figures 1 and 4. Therefore, the effect of the PVP separated from amorphous phase on the  $T_{\rm g}$  of the remaining amorphous phase can be considered negligible.

The temperature dependence of  $t_{90}$  of the solid dispersions is shown in Figure 7. The previously reported  $^{23}$   $t_{90}$  values for pure amorphous nifedipine and phenobarbital are also presented. When compared at the same storage temperatures,  $t_{90}$  values for these solid dispersions were  $\sim 100-1000$  times longer than those for pure amorphous drugs. The  $T_{\rm g}$  values (midpoint) for nifedipine—and phenobarbital—PVP solid dispersions were 51 and 46°C, respectively, at a heating rate of 20°C/min; these values were slightly higher than those



**Figure 6.** Time profiles of the amount of amorphous phenobarbital remaining in phenobarbital—PVP solid dispersion (95:5 w/w) stored at various temperatures.